PHYS 1443 – Section 002 Lecture #11

Wednesday, Oct. 10, 2007 Dr. <mark>Jae</mark>hoon <mark>Yu</mark>

- Free Fall Acceleration
- Kepler's Laws
- Motion in Accelerated Frames
- Work done by a Constant Force
- Scalar Product of Vectors
- Work done by a Varying Force
- Work and Kinetic Energy Theorem



Announcements

- Reading assignments
 - CH. 6-6, 6-7 and 6-8
- Quiz next Monday, Oct. 15
- 2nd term exam on Wednesday, Oct. 24
 - Covers from Ch. 4 to what we cover up to Monday, Oct. 22 (Ch 8 or 9)
 - Time: 1 2:20pm in class
 - Location: SH103



Physics Department The University of Texas at Arlington **COLLOQUIUM**

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Jets in the Solar Chromosphere

Dr. Reiner Hammer Kiepenheuer Institute for Solar Physics, Germany

4:00 pm Wednesday October 10, 2007 Room 101 SH

Abstract

The solar chromosphere shows numerous needle-shaped extensions into the overlying corona, in which plasma shoots up at high speeds. These phenomena are variously called spicules, mottles, or dynamic fibrils, depending on where and how they are observed on the Sun. Many different explanations have been suggested for how these phenomena might be generated in the dynamic solar atmosphere. The currently most popular suggestion is that global solar oscillations propagate as longitudinal waves along magnetic flux tubes. These long-period waves suffer from a cutoff restriction, but if the flux tubes are sufficiently inclined to the vertical they can propagate nevertheless.

I will discuss the cutoff behavior of other wave modes, namely kink and torsional flux tube waves, and show that they have better chances to transport energy upward. Such waves must therefore be taken into account in order to understand spicules. Moreover, some observations indicate that not all spicules can be explained by waves, in particular if they are more vertically oriented. Other mechanisms seem to be operating as well, like reconnection or mechanisms that lead to a strong pressure decrease in the upper chromosphere.

Refreshments will be served in the Physics Library at 3:30 pm

Free Fall Acceleration & Gravitational Force

Weight of an object with mass *m* is *mg*. Using the force exerting on a particle of mass *m* on the surface of the Earth, one can obtain

What would the gravitational acceleration be if the object is at an altitude *h* above the surface of the Earth?

$$mg = G \frac{M_E m}{R_E^2}$$

$$g = G \frac{M_E m}{R_E^2}$$

$$F_g = mg' = G \frac{M_E m}{r^2} = G \frac{M_E m}{(R_E + h)^2}$$

$$g' = G \frac{M_E}{(R_E + h)^2}$$
Distance from the center of the Earth

What do these tell us about the gravitational acceleration?

- •The gravitational acceleration is independent of the mass of the object
- •The gravitational acceleration decreases as the altitude increases •If the distance from the surface of the Earth gets infinitely large, the weight of the object approaches 0.



to the object at the

altitude h.

Example for Gravitational Force

The international space station is designed to operate at an altitude of 350km. When completed, it will have a weight (measured on the surface of the Earth) of 4.22x10⁶N. What is its weight when in its orbit?



The total weight of the station on the surface of the Earth is

$$F_{GE} = mg = G \frac{M_E m}{R_E^2} = 4.22 \times 10^6 N$$

Since the orbit is at 350km above the surface of the Earth, the gravitational force at that altitude is

$$F_{O} = mg' = G \frac{M_{E}m}{(R_{E} + h)^{2}} = \frac{R_{E}^{2}}{(R_{E} + h)^{2}} F_{GE}$$

Therefore the weight in the orbit is

$$F_{O} = \frac{R_{E}^{2}}{(R_{E} + h)^{2}} F_{GE} = \frac{(6.37 \times 10^{6})^{2}}{(6.37 \times 10^{6} + 3.50 \times 10^{5})^{2}} \times 4.22 \times 10^{6} = 3.80 \times 10^{6} N$$

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Special Project

- Derive the formula for the gravitational acceleration (g_{in}) at the radius $R_{in} (< R_E)$ from the center, inside of the Earth. (10 points)
- Compute the fractional magnitude of the gravitational acceleration 1km and 500km inside the surface of the Earth with respect to that on the surface. (6 points, 3 points each)
- Due at the beginning of the class Wednesday, Oct. 17



Kepler's Laws & Ellipse



Ellipses have two different axis, major (long) and minor (short) axis, and two focal points, $F_1 \& F_2$ a is the length of the semi-major axis b is the length of the semi-minor axis

Kepler lived in Germany and discovered the law's governing planets' movements some 70 years before Newton, by analyzing data.

- 1. All planets move in elliptical orbits with the Sun at one focal point.
- 2. The radius vector drawn from the Sun to a planet sweeps out equal area in equal time intervals. (*Angular momentum conservation*)
- 3. The square of the orbital period of any planet is proportional to the cube of the semi-major axis of the elliptical orbit.

Newton's laws explain the cause of the above laws. Kepler's third law is a direct consequence of the law of gravitation being inverse square law.



The Law of Gravity and Motions of Planets
Newton assumed that the law of gravitation applies the same whether it is the apple on the surface of the Moon or on the surface of the Earth.
The interacting bodies are assumed to be point like particles.



Newton predicted that the ratio of the Moon's acceleration $a_{\mathcal{M}}$ to the apple's acceleration g would be

$$\frac{a_M}{g} = \frac{\left(1/r_M\right)^2}{\left(1/R_E\right)^2} = \left(\frac{R_E}{r_M}\right)^2 = \left(\frac{6.37 \times 10^6}{3.84 \times 10^8}\right)^2 = 2.75 \times 10^{-4}$$

Therefore the centripetal acceleration of the Moon, $a_{\mathcal{M}}$ is $a_M = 2.75 \times 10^{-4} \times 9.80 = 2.70 \times 10^{-3} \, m \, / \, s^2$

Newton also calculated the Moon's orbital acceleration $a_{\mathcal{M}}$ from the knowledge of its distance from the Earth and its orbital period, T=27.32 days=2.36x10⁶s

$$a_{M} = \frac{v^{2}}{r_{M}} = \frac{\left(2\pi r_{M}/T\right)^{2}}{r_{M}} = \frac{4\pi^{2}r_{M}}{T^{2}} = \frac{4\pi^{2}\times3.84\times10^{8}}{\left(2.36\times10^{6}\right)^{2}} = 2.72\times10^{-3}\,m/s^{2} \approx \frac{9.80}{\left(60\right)^{2}}$$

This means that the distance to the Moon is about 60 times that of the Earth's radius, and its acceleration is reduced by the square of the ratio. This proves that the inverse square law is valid.

Kepler's Third Law

It is crucial to show that Keper's third law can be predicted from the inverse square law for circular orbits.

Since the gravitational force exerted by the Sun is radially directed toward the Sun to keep the planet on a near circular path, we can apply Newton's second law $\frac{GM_{s}M_{P}}{r^{2}} = \frac{M_{p}v^{2}}{r^{2}}$ Since the orbital speed, v, of the planet with period T is $v = \frac{2\pi r}{T}$ The above can be written $\frac{GM_sM_p}{r^2} = \frac{M_p(2\pi r/T)^2}{2\pi r^2}$ Solving for T one can obtain $T^2 = \left(\frac{4\pi^2}{GM_s}\right)r^3 = K_s r^3$ and $K_s = \left(\frac{4\pi^2}{GM_s}\right) = 2.97 \times 10^{-19} s^2 / m^3$

This is Kepler's third law. It's also valid for the ellipse with r as the length of the semi-major axis. The constant K_s is independent of mass of the planet.

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Example of Kepler's Third Law

Calculate the mass of the Sun using the fact that the period of the Earth's orbit around the Sun is 3.16×10^7 s, and its distance from the Sun is 1.496×10^{11} m.

Using Kepler's third law.

$$T^{2} = \left(\frac{4\pi^{2}}{GM_{s}}\right)r^{3} = K_{s}r^{3}$$
The mass of the Sun, M_s, is

$$M_{s} = \left(\frac{4\pi^{2}}{GT^{2}}\right)r^{3}$$

$$= \left(\frac{4\pi^{2}}{6.67 \times 10^{-11} \times (3.16 \times 10^{7})^{2}}\right) \times (1.496 \times 10^{11})^{3}$$

$$= 1.99 \times 10^{30} kg$$

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Motion in Accelerated Frames

Newton's laws are valid only when observations are made in an inertial frame of reference. What happens in a non-inertial frame?

Fictitious forces are needed to apply Newton's second law in an accelerated frame.

This force does not exist when the observations are made in an inertial reference frame.



Example of Motion in Accelerated Frames

A ball of mass m is hung by a cord to the ceiling of a boxcar that is moving with an acceleration *a*. What do the inertial observer at rest and the non-inertial observer traveling inside the car conclude? How do they differ?



Work Done by a Constant Force

A meaningful work in physics is done only when a sum of forces exerted on an object made a motion to the object.





PHYS 1443-002, Fall 2007 Dr. Jaehoon Yu Work is an energy transfer!!

Example of Work w/ Constant Force

A man cleaning a floor pulls a vacuum cleaner with a force of magnitude F=50.0N at an angle of 30.0° with East. Calculate the work done by the force on the vacuum cleaner as the vacuum cleaner is displaced by 3.00m to East.

$$W = \left(\sum \vec{F}\right) \cdot \vec{d} = \left| \left(\sum \vec{F}\right) \right| \left| \vec{d} \right| \cos \theta$$

 $W = 50.0 \times 3.00 \times \cos 30^{\circ} = 130J$

Does work depend on mass of the object being worked on?

Yes

Why don't I see the mass term in the work at all then?

d

M

Μ

It is reflected in the force. If an object has smaller mass, it would take less force to move it at the same acceleration than a heavier object. So it would take less work. Which makes perfect sense, doesn't it?



Scalar Product of Two Vectors

- Product of magnitude of the two vectors and the cosine of the • angle between them $\vec{A} \cdot \vec{B} \equiv |\vec{A}| |\vec{B}| \cos \theta$
- Operation is commutative $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta = |\vec{B}| |\vec{A}| \cos \theta = \vec{B} \cdot \vec{A}$
- Operation follows the distribution $\vec{A} \cdot (\vec{B} + \vec{C}) = \vec{A} \cdot \vec{B} + \vec{A} \cdot \vec{C}$ law of multiplication
- Scalar products of Unit Vectors $\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$ $\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0$ •
- How does scalar product look in terms of components? ٠

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k} \qquad \vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$
$$\vec{A} \cdot \vec{B} = \left(A_x \hat{i} + A_y \hat{j} + A_z \hat{k}\right) \cdot \left(B_x \hat{i} + B_y \hat{j} + B_z \hat{k}\right) = \left(A_x B_x \hat{i} \hat{g} \hat{i} + A_y B_y \hat{j} \hat{g} \hat{j} + A_z B_z \hat{k} \hat{g} \hat{k}\right) + cross terms$$
$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$
$$= 0$$
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Example of Work by Scalar Product

A particle moving on the xy plane undergoes a displacement d=(2.0i+3.0j)m as a constant force F=(5.0i+2.0j) N acts on the particle.

a) Calculate the magnitude of the displacement and that of the force.

$$\left| \vec{d} \right| = \sqrt{d_x^2 + d_y^2} = \sqrt{(2.0)^2 + (3.0)^2} = 3.6m$$

$$\left| \vec{F} \right| = \sqrt{F_x^2 + F_y^2} = \sqrt{(5.0)^2 + (2.0)^2} = 5.4N$$

b) Calculate the work done by the force F.

$$W = \vec{F} \cdot \vec{d} = \left(2.0\hat{i} + 3.0\hat{j}\right) \cdot \left(5.0\hat{i} + 2.0\hat{j}\right) = 2.0 \times 5.0\hat{i} \cdot \hat{i} + 3.0 \times 2.0\hat{j} \cdot \hat{j} = 10 + 6 = 16(J)$$

Can you do this using the magnitudes and the angle between d and F?

$$W = \overrightarrow{F} \cdot \overrightarrow{d} = \left| \overrightarrow{F} \right| \left| \overrightarrow{d} \right| \cos \theta$$

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