

PHYS 1443 – Section 002

Lecture #9

Wednesday, Oct. 1, 2008

Dr. Jaehoon Yu

- Free Body Diagram
- Application of Newton's Laws
 - Motion without friction
- Forces of Friction
 - Motion with friction
- Uniform and Non-uniform Circular Motions



Reminder: Special Project for Extra Credit

- Show that the trajectory of a projectile motion is a parabola!!
 - 20 points
 - Due: Monday, Oct. 6
 - You MUST show full details of computations to obtain any credit
 - Beyond what was covered in the lecture note!!



Some Basic Information

When Newton's laws are applied, *external forces* are only of interest!!

Why?

Because, as described in Newton's first law, an object will keep its current motion unless non-zero net external force is applied.

Normal Force, n :

Reaction force that reacts to action forces due to the surface structure of an object. Its direction is perpendicular to the surface.

Tension, T :

The reactionary force by a stringy object against an external force exerted on it.

Free-body diagram

A graphical tool which is a diagram of external forces on an object and is extremely useful analyzing forces and motion!! Drawn only on an object.



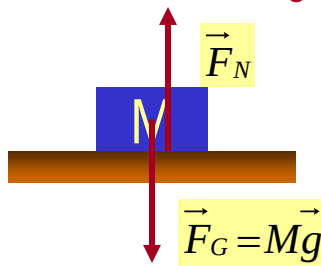
Types of Forces

- Fundamental Forces: Truly unique forces that cannot be derived from any other forces
 - Total of three fundamental forces
 - Gravitational Force
 - Electro-Weak Force
 - Strong Nuclear Force
- Non-fundamental forces: Forces that can be derived from fundamental forces
 - Friction
 - Tension in a rope
 - Normal or support forces



Free Body Diagrams and Solving Problems

- Free-body diagram: A diagram of vector forces acting on an object
- ⇒ A great tool to solve a problem using forces or using dynamics
- 1. Select a point on an object in the problem
- 2. Identify all the forces acting only on the selected object
- 3. Define a reference frame with positive and negative axes specified
- 4. Draw arrows to represent the force vectors on the selected point
- 5. Write down net force vector equation
- 6. Write down the forces in components to solve the problems
- ⇒ No matter which one we choose to draw the diagram on, the results should be the same, as long as they are from the same motion



Which one would you like to select to draw FBD?

What do you think are the forces acting on this object?

Gravitational force

the force supporting the object exerted by the floor

Which one would you like to select to draw FBD?

What do you think are the forces acting on this elevator?

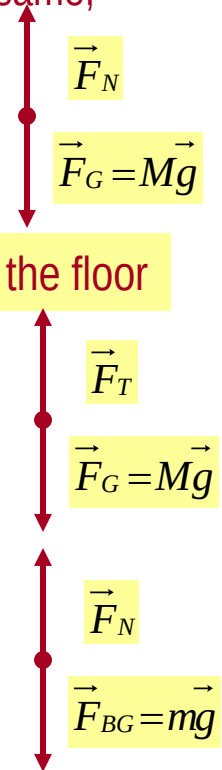
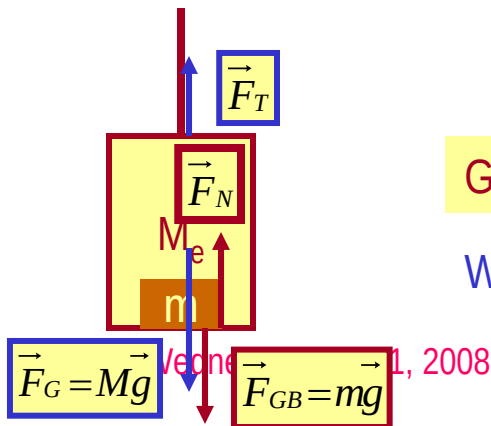
Gravitational force

The force pulling the elevator (Tension)

What about the box in the elevator?

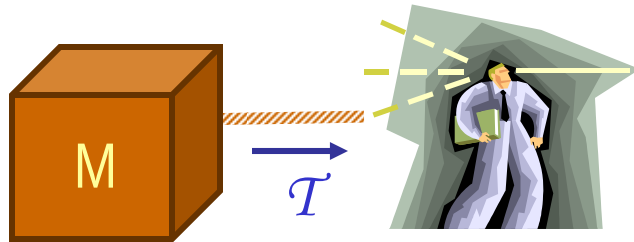
Gravitational force

Normal force



Applications of Newton's Laws

Suppose you are pulling a box on frictionless ice, using a rope.



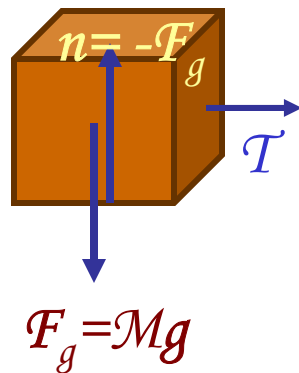
What are the forces being exerted on the box?

Gravitational force: F_g

Normal force: n

Tension force: T

Free-body diagram



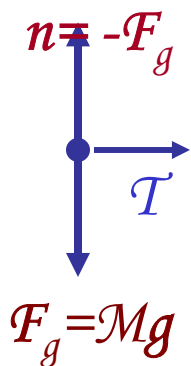
*Total force:
 $F = F_g + n + T = T$*

$$\sum F_x = T = Ma_x$$

$$a_x = \frac{T}{M}$$

$$\sum F_y = -F_g + n = Ma_y = 0$$

$$a_y = 0$$



If T is a constant force, a_x is constant

$$v_{xf} = v_{xi} + a_x t = v_{xi} + \left(\frac{T}{M} \right) t$$

$$\Delta x = x_f - x_i = v_{xi} t + \frac{1}{2} \left(\frac{T}{M} \right) t^2$$

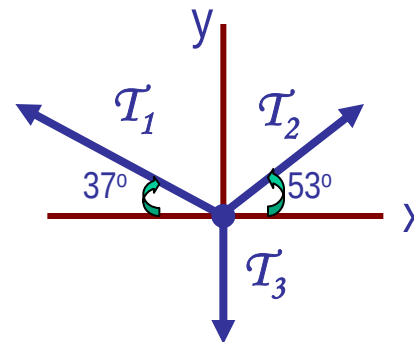
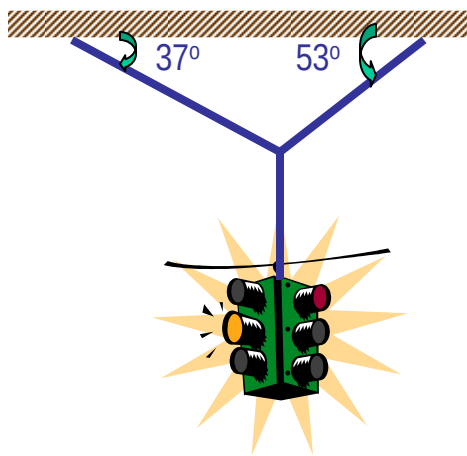
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What happened to the motion in y-direction?

Example for Using Newton's Laws

A traffic light weighing 125 N hangs from a cable tied to two other cables fastened to a support. The upper cables make angles of 37.0° and 53.0° with the horizontal. Find the tension in the three cables.



$$\vec{F} = \vec{T}_1 + \vec{T}_2 + \vec{T}_3 = m\vec{a} = 0 \quad \text{Newton's 2nd law}$$

x-comp. of
net force

$$F_x = \sum_{i=1}^{i=3} T_{ix} = 0 \quad -T_1 \cos(37^\circ) + T_2 \cos(53^\circ) = 0 \therefore T_1 = \frac{\cos(53^\circ)}{\cos(37^\circ)} T_2 = 0.754 T_2$$

y-comp. of
net force

$$F_y = \sum_{i=1}^{i=3} T_{iy} = 0$$

$$T_1 \sin(37^\circ) + T_2 \sin(53^\circ) - mg = 0$$

$$T_2 [\sin(53^\circ) + 0.754 \times \sin(37^\circ)] = 1.25 T_2 = 125 \text{ N}$$

$$T_2 = 100 \text{ N}; \quad T_1 = 0.754 T_2 = 75.4 \text{ N}$$

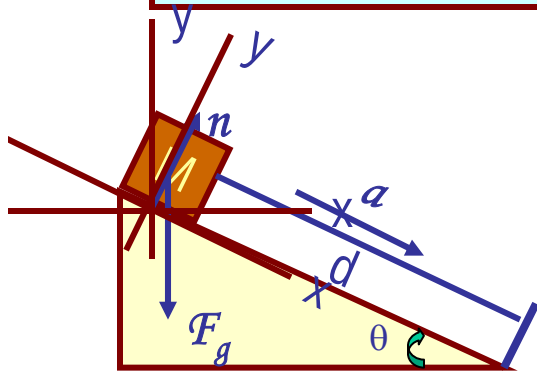
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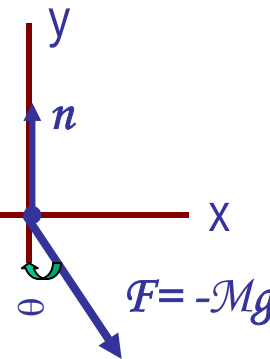
Example w/o Friction

A crate of mass M is placed on a frictionless inclined plane of angle θ .

a) Determine the acceleration of the crate after it is released.



Free-body
Diagram



$$\vec{F} = \vec{F}_g + \vec{n} = m\vec{a}$$

$$F_x = Ma_x = F_{gx} = Mg \sin \theta$$

$$a_x = g \sin \theta$$

$$F_y = Ma_y = n - F_{gy} = n - mg \cos \theta = 0$$

Supposed the crate was released at the top of the incline, and the length of the incline is d . How long does it take for the crate to reach the bottom and what is its speed at the bottom?

$$d = v_{ix}t + \frac{1}{2}a_x t^2 = \frac{1}{2}g \sin \theta t^2$$

$$\therefore t = \sqrt{\frac{2d}{g \sin \theta}}$$

$$v_{xf} = v_{ix} + a_x t = g \sin \theta \sqrt{\frac{2d}{g \sin \theta}} = \sqrt{2dg \sin \theta}$$

$$\therefore v_{xf} = \sqrt{2dg \sin \theta}$$

Forces of Friction

Resistive force exerted on a moving object due to viscosity or other types frictional property of the medium in or surface on which the object moves.

These forces are either proportional to the velocity or the normal force.

Force of static friction, f_s : *The resistive force exerted on the object until just before the beginning of its movement*

Empirical
Formula

$$|\vec{f}_s| \leq \mu_s |\vec{n}|$$

What does this formula tell you?

Frictional force increases till it reaches the limit!!

Beyond the limit, the object moves, and there is NO MORE static friction but kinetic friction takes it over.

Force of kinetic friction, f_k *The resistive force exerted on the object during its movement*

$$|\vec{f}_k| = \mu_k |\vec{n}|$$

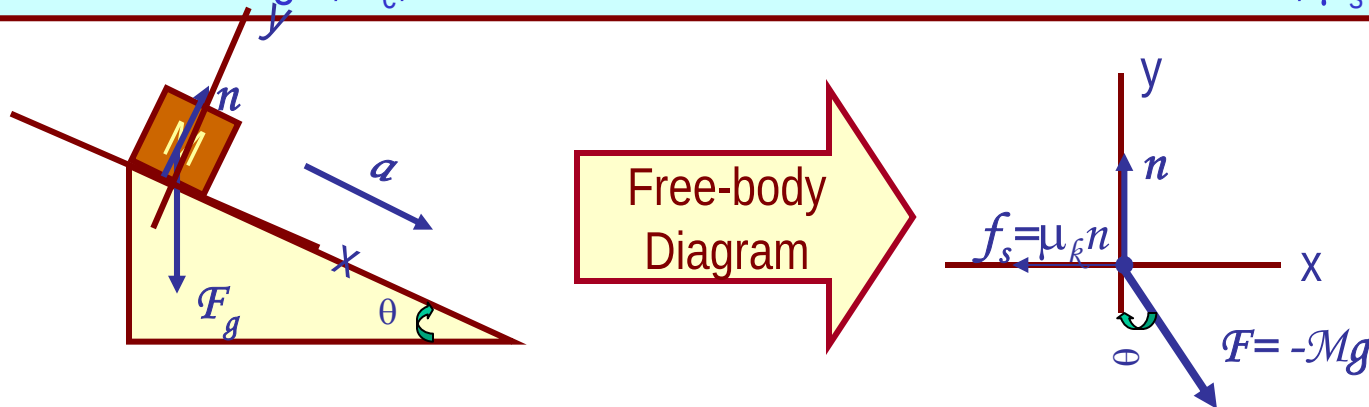
Which direction does kinetic friction apply?

Opposite to the motion!



Example w/ Friction

Suppose a block is placed on a rough surface inclined relative to the horizontal. The inclination angle is increased till the block starts to move. Show that by measuring this critical angle, θ_c , one can determine coefficient of static friction, μ_s .



Net force

$$\vec{F} = M \vec{a} = \vec{F}_g + \vec{n} + \vec{f}_s$$

x comp.

$$F_x = F_{gx} - f_s = Mg \sin \theta - f_s = 0 \quad f_s = \mu_s n = Mg \sin \theta_c$$

y comp.

$$F_y = Ma_y = n - F_{gy} = n - Mg \cos \theta_c = 0 \quad n = F_{gy} = Mg \cos \theta_c$$

$$\mu_s = \frac{Mg \sin \theta_c}{n} = \frac{Mg \sin \theta_c}{Mg \cos \theta_c} = \tan \theta_c$$