# PHYS 1441 – Section 002
# Lecture #15

*Monday, Nov. 8, 2010*

*Dr. Jaehoon Yu*

- Elastic Potential Energy
- Mechanical Energy Conservation
- Power
- Linear Momentum
- Linear Momentum and Impulse

Today's homework is homework #9, due 10pm, Tuesday, Nov. 16!!

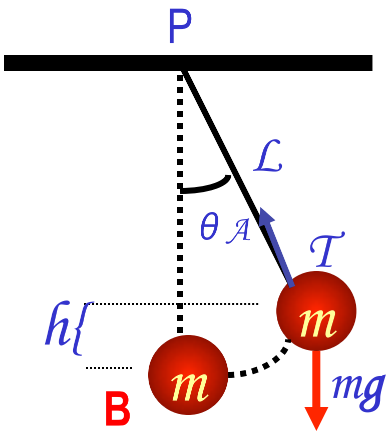
# Announcements

- Quiz #5
  - Beginning of the class, Wednesday, Nov. 17
  - Covers: Ch. 6.5 – what we finish next Monday, Nov. 15

# Special Project

1. A ball of mass $\mathcal{M}$ at rest is dropped from the height $h$ above the ground onto a spring on the ground, whose spring constant is $k$. Neglecting air resistance and assuming that the spring is in its equilibrium, express, in terms of the quantities given in this problem and the gravitational acceleration $g$, the distance $x$ of which the spring is pressed down when the ball completely loses its energy. (10 points)
2. Find the $x$ above if the ball's initial speed is $v_i$. (10 points)
3. Due for the project is Wednesday, Nov. 17.
4. You must show the detail of your OWN work in order to obtain any credit.

# Special Project II




A ball of mass $m$ is attached to a light cord of length L, making up a pendulum. The ball is released from rest when the cord makes an angle $\theta_A$ with the vertical, and the pivoting point P is frictionless.

A) Find the speed of the ball when it is at the lowest point, B, in terms of the quantities given above.

B) Determine the tension T at point B in terms of the quantities given above.

Each of these problem is 10 point. The due date is Wednesday, Nov. 17.

# Elastic Potential Energy

*Potential energy given to an object by a spring or an object with elasticity in the system that consists of an object and the spring.*

*The force spring exerts on an object when it is distorted from its equilibrium by a distance x is*

$$F_s = -kx$$

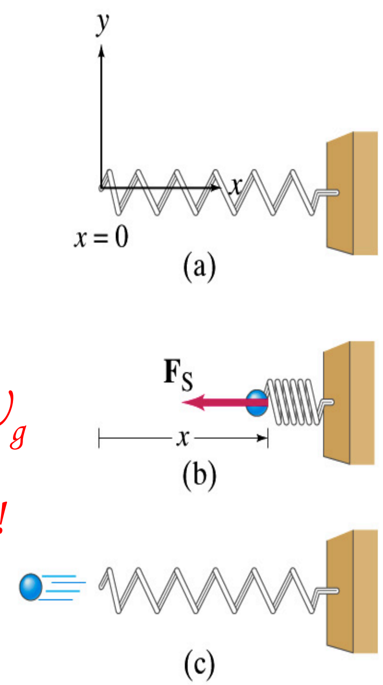
**Hooke's Law**

*The work performed on the object by the spring is*

$$W_s = \int_{x_i}^{x_f} (-kx)dx = \left[-\frac{1}{2}kx^2\right]_{x_i}^{x_f} = -\frac{1}{2}kx_f^2 + \frac{1}{2}kx_i^2 = \frac{1}{2}kx_i^2 - \frac{1}{2}kx_f^2$$

*The potential energy of this system is*

$$U_s \equiv \frac{1}{2}kx^2$$




*What do you see from the above equations?*

*The work done on the object by the spring depends only on the initial and final position of the distorted spring.*

*Where else did you see this trend?*

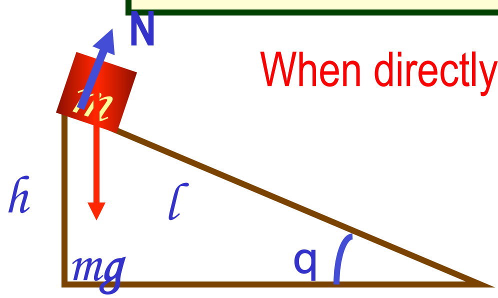
*The gravitational potential energy, $U_g$*

*So what does this tell you about the elastic force?*

*A conservative force!!!*

# Conservative and Non-conservative Forces

*The work done on an object by the gravitational force does not depend on the object's path in the absence of a retardation force.*




When directly falls, the work done on the object by the gravitation force is $W_g = mgh$

When sliding down the hill of length $l$, the work is

$$W_g = F_{g-incline} \times l = mg\sin\theta \times l$$
$$= mg(l\sin\theta) = mgh$$

How about if we lengthen the incline by a factor of 2, keeping the height the same??

Still the same amount of work☺

$$\boxed{W_g = mgh}$$

So the work done by the gravitational force on an object is independent of the path of the object's movements. It only depends on the difference of the object's initial and final position in the direction of the force.

Forces like gravitational and elastic forces are called the conservative force

1. If the work performed by the force does not depend on the path.
2. If the work performed on a closed path is 0.

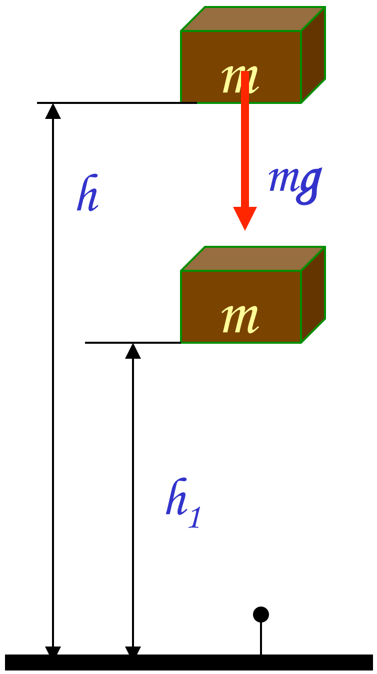
*Total mechanical energy is conserved!!*

$$\boxed{E_M \equiv KE_i + PE_i = KE_f + PE_f}$$

# Conservation of Mechanical Energy

*Total mechanical energy is the sum of kinetic and potential energies*

$$E \equiv KE + PE$$




Let's consider a brick of mass *m* at the height *h* from the ground

*What is the brick's potential energy?*

$$PE = mgh$$

*What happens to the energy as the brick falls to the ground?*

$$\Delta PE = PE_f - PE_i = -Fs$$

*The brick gains speed*

*By how much?*

$$v = gt$$

*So what?*

*The brick's kinetic energy increased*

$$K = \frac{1}{2}mv^2 = \frac{1}{2}mg^2t^2$$

*And?*

*The lost potential energy is converted to kinetic energy!!*

*The total mechanical energy of a system remains constant in any isolated systems of objects that interacts only through conservative forces:* ***Principle of mechanical energy conservation***

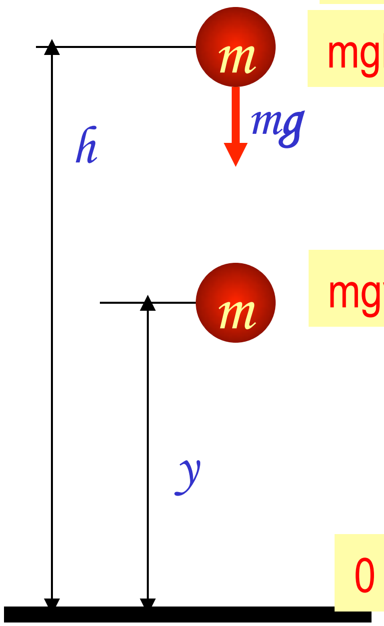
$$E_i = E_f$$

$$KE_i + \sum PE_i = KE_f + \sum PE_f$$

What does this mean?

# Example

A ball of mass $m$ at rest is dropped from the height $h$ above the ground. a) Neglecting the air resistance, determine the speed of the ball when it is at the height $y$ above the ground.




| PE | KE | |
|---|---|---|
| mgh | 0 | $mv_i^2/2$ |
| mgy | $mv^2/2$ | $mv_f^2/2$ |
| 0 | | |

Using the principle of mechanical energy conservation

$$K_i + PE_i = K_f + PE_f \quad 0 + mgh = \frac{1}{2}mv^2 + mgy$$

$$\frac{1}{2}mv^2 = mg(h-y)$$

$$\therefore v = \sqrt{2g(h-y)}$$

b) Determine the speed of the ball at $y$ if it had initial speed $v_i$ at the time of the release at the original height $h$.

Again using the principle of mechanical energy conservation but with non-zero initial kinetic energy!!!

$$K_i + PE_i = K_f + PE_f$$

$$\frac{1}{2}mv_i^2 + mgh = \frac{1}{2}mv_f^2 + mgy$$

$$\frac{1}{2}m\left(v_f^2 - v_i^2\right) = mg(h-y)$$

$$\therefore v_f = \sqrt{v_i^2 + 2g(h-y)}$$

This result look very similar to a kinematic expression, doesn't it? Which one is it?

# Power

- Rate at which the work is done or the energy is transferred
  - What is the difference for the same car with two different engines (4 cylinder and 8 cylinder) climbing the same hill?
  - ➔ The time… 8 cylinder car climbs up the hill faster!

Is the total amount of work done by the engines different? NO

Then what is different? The rate at which the same amount of work performed is higher for 8 cylinders than 4.

Average power $$\boxed{\overline{P} \equiv \frac{\Delta W}{\Delta t} = \frac{Fs}{\Delta t} = F\frac{s}{\Delta t} = F\overline{v}}$$

**Scalar quantity**

Unit? $\boxed{J/s = Watts}$ $\boxed{1HP \equiv 746\,Watts}$

What do power companies sell? $1kWH = 1000Watts \times 3600s = 3.6 \times 10^{6}J$

**Energy**

# Energy Loss in Automobile

*Automobile uses only 13% of its fuel to propel the vehicle.*

*Why?*

67% in the engine:
- Incomplete burning
- Heat
- Sound

*16% in friction in mechanical parts*

*4% in operating other crucial parts such as oil and fuel pumps, etc*

*13% used for balancing energy loss related to moving the vehicle, like air resistance and road friction to tire, etc*

*Two frictional forces involved in moving vehicles*

$$m_{car} = 1450kg \quad Weight = mg = 14200N$$

*Coefficient of Rolling Friction;* m=0.016

$$\mu n = \mu mg = 227N$$

*Air Drag*

$$f_a = \frac{1}{2} D\rho A v^2 = \frac{1}{2} \times 0.5 \times 1.293 \times 2v^2 = 0.647v^2$$

*Total Resistance*

$$f_t = f_r + f_a$$

*Total power to keep speed v=26.8m/s=60mi/h*

$$P = f_t v = (691N) \cdot 26.8 = 18.5kW$$

*Power to overcome each component of resistance*

$$P_r = f_r v = (227) \cdot 26.8 = 6.08kW$$

$$P_a = f_a v = (464.7) \cdot 26.8 = 12.5kW$$

# Human Metabolic Rates

| Activity | Rate (watts) |
|---|---|
| Running (15 km/h) | 1340 W |
| Skiing | 1050 W |
| Biking | 530 W |
| Walking (5 km/h) | 280 W |
| Sleeping | 77 W |

[a]For a young 70-kg male.

# Ex. The Power to Accelerate a Car

A $1.10 \times 10^3$kg car, starting from rest, accelerates for 5.00s. The magnitude of the acceleration is $a=4.60m/s^2$. Determine the average power generated by the net force that accelerates the vehicle.

What is the force that accelerates the car?

$$F = ma = \left(1.10\times10^3\right)\cdot\left(4.60\, m/s^2\right) = 5060N$$

Since the acceleration is constant, we obtain

$$\overline{v} = \frac{v_0 + v_f}{2} = \frac{0 + v_f}{2} = \frac{v_f}{2}$$

From the kinematic formula

$$v_f = v_0 + at = 0 + \left(4.60\, m/s^2\right)\cdot\left(5.00s\right) = 23.0\, m/s$$

Thus, the average speed is

$$\frac{v_f}{2} = \frac{23.0}{2} = 11.5\, m/s$$

And, the average power is

$$\overline{P} = F\overline{v} = \left(5060N\right)\cdot\left(11.5\, m/s\right) = 5.82\times10^4 W$$
$$= 78.0hp$$