

PHYS 1444 – Section 002

Lecture #16

Wednesday, Nov. 1, 2017

Dr. Jaehoon Yu

- Chapter 26
 - ReKirchhoff's Rules
 - EMFs in Series and Parallel
- Chapter 27: Magnetism & Magnetic Field
 - Electric Current and Magnetism
 - Magnetic Forces on Electric Current



Announcements

- Reading assignments
 - CH26.5, 6 and 7
- Quiz #3
 - At the beginning of the class Monday, Nov. 6
 - Covers CH25.5 to what we learn today (CH26+ maybe CH27.1?)
 - Bring your calculator but DO NOT input formula into it!
 - Cell phones or any types of computers cannot replace a calculator!
 - BYOF: You may bring a one 8.5x11.5 sheet (front and back) of **handwritten** formulae and values of constants
 - No derivations, word definitions or solutions of any kind!
 - No additional formulae or values of constants will be provided!
- Colloquium today
 - 4pm in SH100, Prof. F. Calaprice of Princeton Univ.

Wednesday, Nov. 1, 2017



PHYS 1444-002, Fall 2017
Dr. Jaehoon Yu

Physics Department
The University of Texas at Arlington
COLLOQUIUM

**New Measurements of Solar Neutrinos with the Borexino
Detector**

Professor Frank Calaprice
Department of Physics, Princeton University

**Wednesday November 1, 2017
4:00 p.m. Room 100 Science Hall**

Abstract

Borexino is a 300-ton liquid scintillator detector located in the Gran Sasso Underground Laboratory in Italy. This detector has been taking solar neutrino data for the past ten years and recently completed new measurements of the pp, pep, ^7Be , and ^8B neutrinos. These neutrinos are produced in the pp-chain of nuclear fusion reactions that produce the Sun's energy, as proposed by H. Bethe in 1939. Now, 78 years after Bethe's paper, we have direct experimental confirmation of his theory of the nuclear reactions that power the Sun. The new data also explore neutrino oscillations and provide evidence for the transition from "vacuum oscillations" for low energy pp and ^7Be neutrinos, to "matter effect oscillations" for high energy ^8B neutrinos, as predicted in the MSW theory. Experimental methods that achieved the ultra-low backgrounds that made these results possible will be described. Ongoing research toward lower backgrounds and a possible measurement of solar CNO neutrinos will also be presented.

Refreshments will be served at 3:30 p.m. in the Physics Library

Reminder: Special Project #5

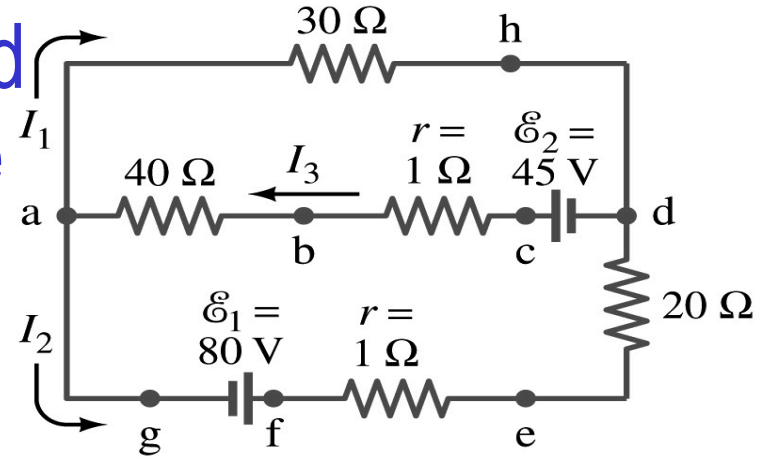
- Make a list of the power consumption and the resistance of all electric and electronic devices at your home and compiled them in a table. (5 points total for the first 10 items and 0.25 points each additional item.)
- Estimate the cost of electricity for each of the items on the table using your own electric cost per kWh (if you don't find your own, use \$0.12/kWh) and put them in the relevant column. (2 points total for the first 10 items and 0.1 points each additional items)
- Estimate the the total amount of energy in Joules and the total electricity cost per day, per month and per year for your home. (6 points)
- Due: Beginning of the class coming Monday, Nov. 6



Kirchhoff's Rules – 1st Rule

- Some circuits are very complicated to do the analysis using the simple combinations of resistors

- G. R. Kirchhoff devised two rules to deal with complicated circuits.



- Kirchhoff's rules are based on conservation of charge and energy

- Kirchhoff's 1st rule: The junction rule, charge conservation.

- At any junction point, the sum of all currents entering the junction must be equal to the sum of all currents leaving the junction.
 - In other words, what goes in must come out.
 - At junction *a* in the figure, I_3 comes into the junction while I_1 and I_2 leaves: $I_3 = I_1 + I_2$

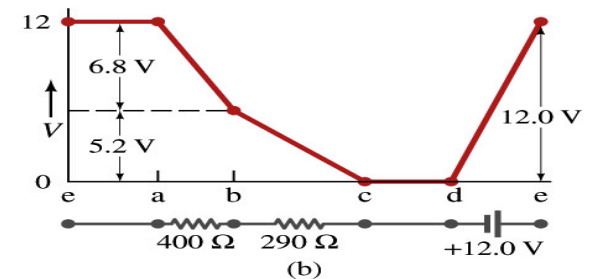
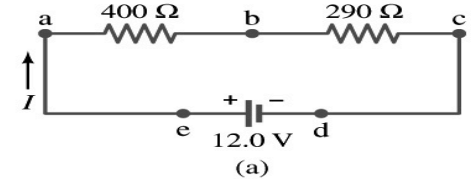
Kirchhoff's Rules – 2nd Rule

- Kirchhoff's 2nd rule: The loop rule, uses **conservation of energy**.

- The sum of the changes in potential in any closed path of a circuit must be zero.

- The current in the circuit in the figure is $I=12/690=0.017\text{A}$.

- Point e is the high potential point while point d is the lowest potential.
- When the test charge starts at e and returns to e , the total potential change is 0.
- Between point e and a , no potential change since there is no source of potential nor any resistance.
- Between a and b , there is a 400Ω resistance, causing $IR=0.017*400=6.8\text{V}$ drop.
- Between b and c , there is a 290Ω resistance, causing $IR=0.017*290=5.2\text{V}$ drop.
- Since these are voltage drops, we use negative sign for these, -6.8V and -5.2V .
- No change between c and d while from d to e there is $+12\text{V}$ change.
- Thus the total change of the voltage through the loop is: $-6.8\text{V}-5.2\text{V}+12\text{V}=0\text{V}$.



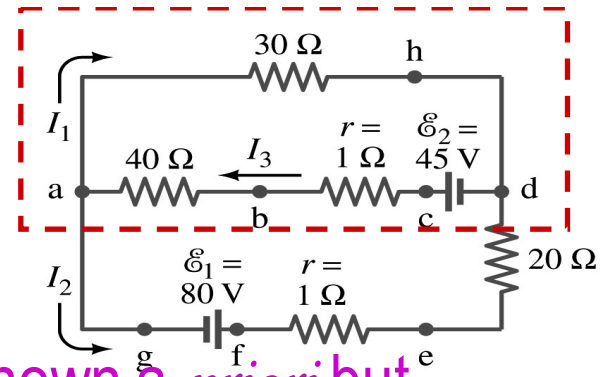
How to use Kirchhoff's Rules??

1. Determine the flow of currents at the junctions and label each and everyone of the currents.
 - It does not matter which direction, you decide but keep it!
 - You cannot have all current coming in or going out of a junction, though!
 - If the value of the current after completing the calculations is negative, you just need to flip the direction of the current flow.
2. Write down the current equation based on Kirchhoff's 1st rule at various junctions.
 - Be sure to see if any of them are the same.
3. Choose closed loops in the circuit
4. Write down the potential in each interval of the junctions, keeping the proper signs as you decided in step 1 above.
5. Write down the potential equations for each loop.
6. Solve the equations for unknowns.



Example 26 – 9

Use Kirchhoff's rules. Calculate the currents I_1 , I_2 and I_3 in each of the branches of the circuit in the figure.



The directions of the current through the circuit is not known *a priori* but since the current tends to move away from the positive terminal of a battery, we arbitrarily choose the direction of the currents as shown.

We have three unknowns so we need three equations.

Using Kirchhoff's junction rule at point a , we obtain $I_3 = I_1 + I_2$

This is the same for junction d as well, so no additional information.

Now the second rule on the loop $ahdcba$.

$$V_{ah} = -I_1 30 \quad V_{hd} = 0 \quad V_{dc} = +45 \quad V_{cb} = -I_3 \quad V_{ba} = -40I_3$$

The total voltage change in the loop $ahdcba$ is.

$$V_{ahdcba} = -30I_1 + 45 - 1 \cdot I_3 - 40I_3 = 45 - 30I_1 - 41I_3 = 0$$

Example 26 – 9, cnt'd

Now the second rule on the other loop *agfedcba*.

$$V_{ag} = 0 \quad V_{gf} = +80 \quad V_{fe} = -I_2 \cdot 1 \quad V_{ed} = -I_2 \cdot 20$$

$$V_{dc} = +45 \quad V_{cb} = -I_3 \cdot 1 \quad V_{ba} = -40 \cdot I_3$$

The total voltage change in loop *agfedcba* is. $V_{agfedcba} = -21I_2 + 125 - 41I_3 = 0$

So the three equations become

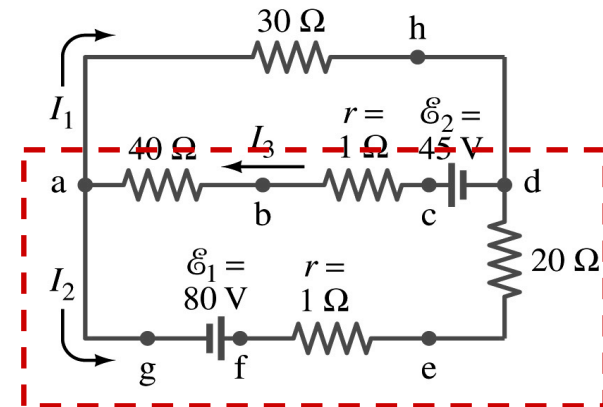
$$I_3 = I_1 + I_2$$

$$45 - 30I_1 - 41I_3 = 0$$

$$125 - 21I_2 - 41I_3 = 0$$

We can obtain the three current by solving these equations for I_1 , I_2 and I_3 .

Do this yourselves!!



EMFs in Series and Parallel: Charging a Battery

- When two or more sources of emfs, such as batteries, are connected in series

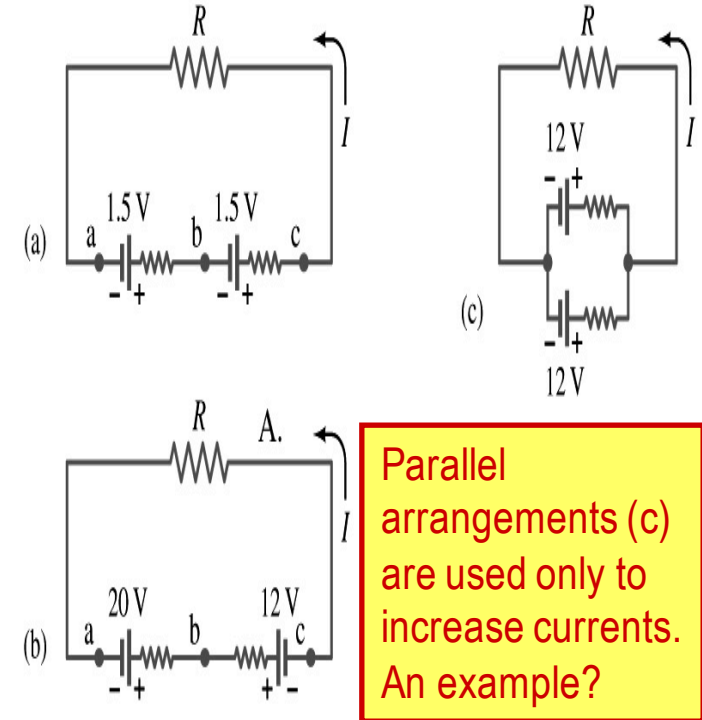
- The total voltage is the algebraic sum of their voltages, if their direction is the same

- $V_{ab} = 1.5 + 1.5 = 3.0\text{V}$ in figure (a).

- If the batteries are arranged in an opposite direction, the total voltage is the difference between them

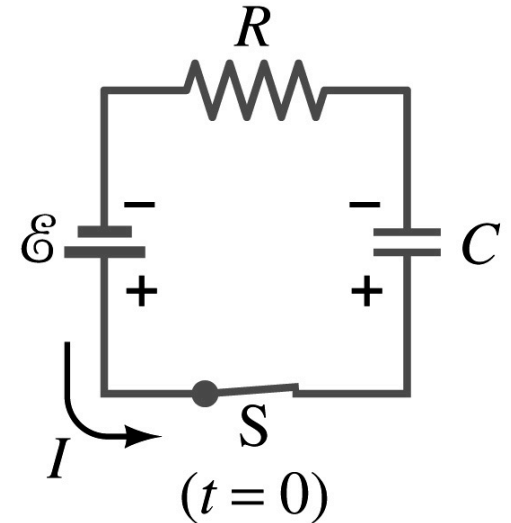
- $V_{ac} = 20 - 12 = 8.0\text{V}$ in figure (b)

- Connecting batteries in opposite direction is wasteful.
- This, however, is the way a battery charger works.
- Since the 20V battery is at a higher voltage, it forces charges into 12V battery
- Some battery are rechargeable since their chemical reactions are reversible but most the batteries do not reverse their chemical reactions



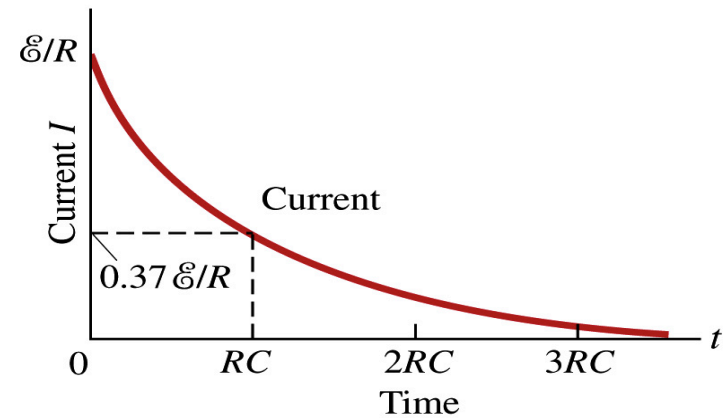
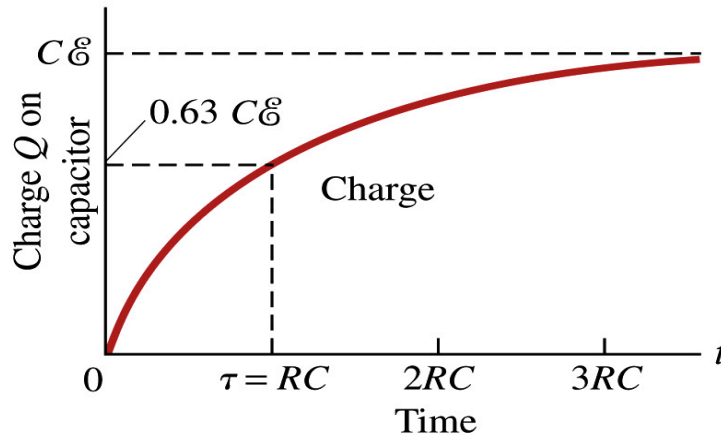
RC Circuits

- Circuits containing both resistors and capacitors
 - RC circuits are used commonly in everyday life
 - Control windshield wiper
 - Timing of traffic light from red to green
 - Camera flashes and heart pacemakers
- How does an RC circuit look?
- There should be a source of emf, capacitors and resistors
- What happens when the switch S is closed?
- Current immediately starts flowing through the circuit.
- Electrons flow out of negative terminal of the emf source, through the resistor R and accumulates on the upper plate of the capacitor.
- The electrons from the bottom plate of the capacitor will flow into the positive terminal of the battery, leaving only positive charge on the bottom plate.
- As the charge accumulates on the capacitor, the potential difference across it increases
- The current reduces gradually to 0 till the voltage across the capacitor is the same as emf.
- The charge on the capacitor increases till it reaches to its maximum $C\mathcal{E}$.



RC Circuits

- How does all this look like in graphs?
 - The charge and the current on the capacitor as a function of time



- From energy conservation (Kirchhoff's 2nd rule), the emf \mathcal{E} must be equal to the voltage drop across the capacitor and the resistor
 - $\mathcal{E} = IR + Q/C$
 - R includes all resistance in the circuit, including the internal resistance of the battery, I is the current in the circuit at any instance, and Q is the charge of the capacitor at that same instance.

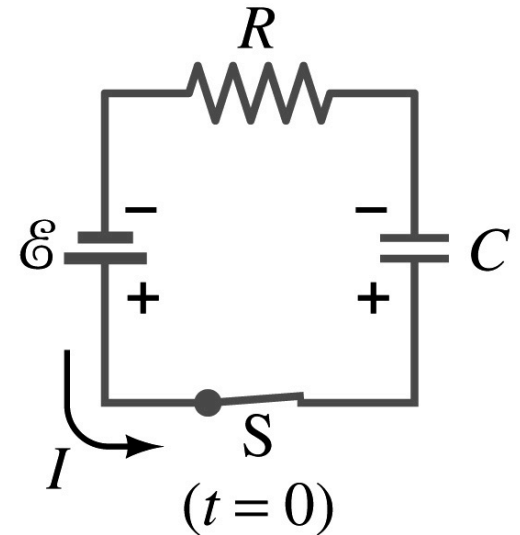
Analysis of RC Circuits

- In an RC circuit $Q = C\varepsilon(1 - e^{-t/RC})$ and $V_C = \varepsilon(1 - e^{-t/RC})$
- What can we see from the above equations?
 - Q and V_C increase from 0 at $t=0$ to maximum value
 $Q_{\max} = C\varepsilon$ and $V_C = \varepsilon$.
- In how much time?
 - The quantity RC is called the **time constant** of the circuit, τ
 - $\tau = RC$, What is the unit? **Sec.**
 - What is the physical meaning?
 - The time required for the capacitor to reach $(1 - e^{-1}) = 0.63$ or 63% of the full charge
- The current is $I = \frac{dQ}{dt} = \frac{\varepsilon}{R} e^{-t/RC}$



Example 26 – 12

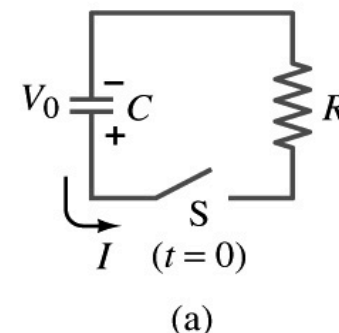
RC circuit, with emf. The capacitance in the circuit of the figure is $C=0.30\mu\text{F}$, the total resistance is $20\text{k}\Omega$, and the battery emf is 12V . Determine (a) the time constant, (b) the maximum charge the capacitor could acquire, (c) the time it takes for the charge to reach 99% of this value, (d) the current I when the charge Q is half its maximum value, (e) the maximum current, and (f) the charge Q when, the current I is 0.20 its maximum value.



- (a) Since $\tau = RC$ We obtain $\tau = 20 \times 10^3 \cdot 0.30 \times 10^{-6} = 6.0 \times 10^{-3} \text{ sec}$
- (b) Maximum charge is $Q_{\text{max}} = C\mathcal{E} = 0.30 \times 10^{-6} \cdot 12 = 3.6 \times 10^{-6} \text{ C}$
- (c) Since $Q = C\mathcal{E}(1 - e^{-t/RC})$ For 99% we obtain $0.99C\mathcal{E} = C\mathcal{E}(1 - e^{-t/RC})$
 $e^{-t/RC} = 0.01$; $-t/RC = -2 \ln 10$; $t = RC \cdot 2 \ln 10 = 4.6RC = 28 \times 10^{-3} \text{ sec}$
- (d) Since $\mathcal{E} = IR + Q/C$ We obtain $I = (\mathcal{E} - Q/C)/R$
 The current when Q is $0.5Q_{\text{max}}$ $I = (12 - 1.8 \times 10^{-6}/0.30 \times 10^{-6})/20 \times 10^3 = 3 \times 10^{-4} \text{ A}$
- (e) When is I maximum? when $Q=0$: $I = 12/20 \times 10^3 = 6 \times 10^{-4} \text{ A}$
- (f) What is Q when $I=120\text{mA}$? $Q = C(\mathcal{E} - IR) =$

Discharging RC Circuits

- When a capacitor is already charged, it is allowed to discharge through a resistance R .
 - When the switch S is closed, the voltage across the resistor at any instant equals that across the capacitor. Thus $IR=Q/C$.
 - The rate at which the charge leaves the capacitor equals the negative the current flows through the resistor
 - $I = -dQ/dt$
 - Since the current is leaving the capacitor
 - Thus the voltage equation becomes a differential equation



$$-\frac{dQ}{dt} R = \frac{Q}{C} \quad \xrightarrow{\text{Rearrange terms}} \quad \frac{dQ}{Q} = -\frac{dt}{RC}$$

Discharging RC Circuits

- Now, let's integrate from $t=0$ when the charge is Q_0 to t when the charge is Q

$$\int_{Q_0}^Q \frac{dQ}{Q} = - \int_0^t \frac{dt}{RC}$$

- The result is $\ln Q \Big|_{Q_0}^Q = \ln \frac{Q}{Q_0} = - \frac{t}{RC}$

- Thus, we obtain

$$Q(t) = Q_0 e^{-t/RC}$$

- What does this tell you about the charge on the capacitor?

- It decreases exponentially w/ time at the time constant RC
- Just like the case of charging

What is this?

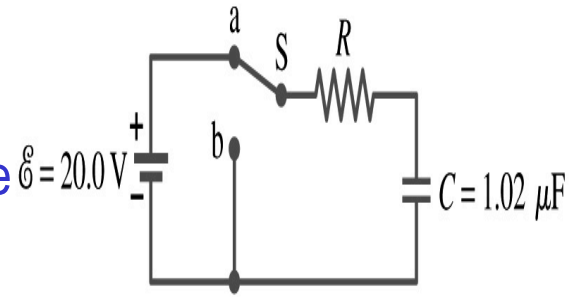
- The current is: $I = - \frac{dQ}{dt} = \frac{Q_0}{RC} e^{-t/RC}$

$$I(t) = I_0 e^{-t/RC}$$

- The current also decreases exponentially w/ time w/ the constant RC

Example 26 – 13

Discharging RC circuit. In the RC circuit shown in the figure the battery has fully charged the capacitor, so $Q_0 = C\mathcal{E}$. Then at $t=0$, the switch is thrown from position a to b. The battery emf is 20.0V, and the capacitance $C=1.02\mu\text{F}$. The current I is observed to decrease to 0.50 of its initial value in $40\mu\text{s}$. (a) what is the value of R ? (b) What is the value of Q , the charge on the capacitor, at $t=0$? (c) What is Q at $t=60\mu\text{s}$?



(a) Since the current reaches to 0.5 of its initial value in $40\mu\text{s}$, we can obtain

$$I(t) = I_0 e^{-t/RC} \xrightarrow{\text{For } 0.5 I_0} 0.5 I_0 = I_0 e^{-t/RC} \xrightarrow{\text{Rearrange terms}} -t/RC = \ln 0.5 = -\ln 2$$

$$\xrightarrow{\text{Solve for R}} R = t / (C \ln 2) = 40 \times 10^{-6} / (1.02 \times 10^{-6} \cdot \ln 2) = 56.6 \Omega$$

(b) The value of Q at $t=0$ is

$$Q_0 = Q_{\max} = C\mathcal{E} = 1.02 \times 10^{-6} \cdot 20.0 = 20.4 \mu\text{C}$$

(c) What do we need to know first for the value of Q at $t=60\mu\text{s}$?

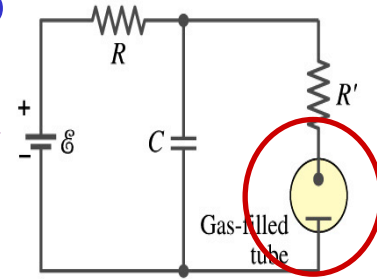
The RC time $\tau = RC = 56.6 \cdot 1.02 \times 10^{-6} = 57.7 \mu\text{s}$

Thus $Q(t = 60 \mu\text{s}) = Q_0 e^{-t/RC} = 20.4 \times 10^{-6} \cdot e^{-60 \mu\text{s} / 57.7 \mu\text{s}} = 7.2 \mu\text{C}$

Application of RC Circuits

- What do you think the charging and discharging characteristics of RC circuits can be used for?

- To produce voltage pulses at a regular frequency
- How?



- The capacitor charges up to a particular voltage and discharges
- A simple way of doing this is to use breakdown of voltage in a gas filled tube

- The discharge occurs when the voltage breaks down at V_0
- After the completion of discharge, the tube no longer conducts
- Then the voltage is at V_0' and it starts charging up
- How do you think the voltage as a function of time look?

» A sawtooth shape

- Pace maker, intermittent windshield wiper, etc

