## PHYS 1444 – Section 501 Lecture #18

Monday, Apr. 10, 2006 Dr. Jaehoon Yu

- Induced EMF and Electromagnetic Induction
- Faraday's Law of Induction
- Magnetic Flux
- Lenz's Law
- Electric Generators
- DC Generator
- Eddy Currents



## Announcements

- Reading assignments
  - CH29 5
- How was the exam?
  - We will have a exam solution session Wednesday, Apr.
    12 for the first half of the class
  - We will then have a mid-term grade discussion in the remainder of the class Wednesday.
  - I strongly suggest you all to be at the class Wednesday!!



## Induced EMF

- It has been discovered by Oersted and company in early 19<sup>th</sup> century that
  - Magnetic field can be produced by the electric current
  - Magnetic field can exert force on electric charge
- So if you were scientists at that time, what would you wonder?
  - Yes, you are absolutely right. You would wonder if the magnetic field can create the electric current.
  - An American scientist Joseph Henry and an English scientist Michael Faraday independently found that it was possible
    - Though, Faraday was given the credit since he published his work before Henry did
      - He also did a lot of detailed studies on magnetic induction



## **Electromagnetic Induction**



- Despite his hope he did not see steady current induced on the other side when the switch is thrown
- But he did see that the needle on the Galvanometer turns strongly when the switch is initially thrown and is opened
  - When the magnetic field through coil Y changes, a current flows as if there were a source of emf
- Thus he concluded that <u>an induced emf is produced by a</u> <u>changing magnetic field</u> → <u>Electromagnetic Induction</u>



## **Electromagnetic Induction**

- Further studies on electromagnetic induction taught
  - If magnet is moved quickly into a coil of wire, a current is induced in the wire.
  - If the magnet is removed from the coil, a current is induced in the wire in the opposite direction
  - By the same token, current can also be induced if the magnet stays put but the coil moves toward or away from the magnet
  - Current is also induced if the coil rotates.
- In other words, it does not matter whether the magnet or the coil moves. It is the relative motion that counts.







## Magnetic Flux

- So what do you think is the induced emf proportional to?
  - The rate of changes of the magnetic field?
    - the higher the changes the higher the induction
  - Not really, it rather depends on the rate of change of the magnetic flux,  $\Phi_{B}$ .
  - Magnetic flux is defined as (just like the electric flux)

$$- \Phi_B = B_\perp A = BA\cos\theta = \vec{B}\cdot\vec{A}$$

- θ is the angle between **B** and the area vector **A** whose direction is perpendicular to the face of the loop based on the right-hand rule
- What kind of quantity is the magnetic flux?
  - Scalar. Unit?

• 
$$T \cdot m^2$$
 or weber  $1Wb = 1T \cdot m^2$ 

• If the area of the loop is not simple or B is not uniform, the magnetic flux can be written as Monday, Apr. 10, 2006 PHYS 1444-501, Spring 2006  $\Phi_B = \int \vec{B} \cdot d\vec{A}$ 

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 $\mathbf{B} = \begin{bmatrix} B_{\parallel} & A \\ \theta & B_{\perp} \\ A = l^2 \\ l \end{bmatrix}$ 

# Faraday's Law of Induction

- In terms of magnetic flux, we can formulate Faraday's findings
  - The emf induced in a circuit is equal to the rate of change of <u>magnetic flux</u> through the circuit

 $\varepsilon = -\frac{d\Phi_B}{dt}$ 

Faraday's Law of Induction

• If the circuit contains N closely wrapped loops, the total induced emf is the sum of emf induced in each

loop

$$\varepsilon = -N \frac{d\Phi_B}{dt}$$

- Why negative?

• Has got a lot to do with the direction of induced emf...



# Lenz's Law

- It is experimentally found that
  - An induced emf gives rise to a current whose magnetic field opposes the original change in flux → This is known as <u>Lenz's</u> <u>Law</u>
  - In other words, an induced emf is always in a direction that opposes the original change in flux that caused it.
  - We can use Lenz's law to explain the following cases in the figures
    - When the magnet is moving into the coil
      - Since the external flux increases, the field inside the coil takes the opposite direction to minimize the change and causes the current to flow clockwise
    - When the magnet is moving out
      - Since the external flux decreases, the field inside the coil takes the opposite direction to compensate the loss, causing the current to flow counter-clockwise
- Which law is Lenz's law result of?
  - Energy conservation. Why?

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## Induction of EMF

- How can we induce emf?
- Let's look at the formula for magnetic flux

• 
$$\Phi_B = \int \vec{B} \cdot d\vec{A} = \int B \cos \theta dA$$

- What do you see? What are the things that can change with time to result in change of magnetic flux?
  - Magnetic field
  - The area of the loop



- The angle  $\theta$  between the field and the area vector

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		Maximum flux									Zero flux									

Flux through coil is decreased

#### Example 29 – 2

Pulling a coil from a magnetic field. A square coil of wire with side 5.00cm contains 100 loops and is positioned perpendicular to a uniform 0.600-T magnetic field. It is quickly and uniformly pulled from the field (moving perpendicular to B) to a region where B drops abruptly to zero. At t=0, the right edge of the coil is at the edge of the field. It takes 0.100s for the whole coil to reach the field-free region. Find (a) the rate of change in flux through the coil, (b) the emf and current induced, and (c) how much energy is dissipated in the coil if its resistance is  $100\Omega$ . (d) what was the

average force required?

What should be computed first? The initial flux at t=0.

The flux at t=0 is  $\Phi_B = \vec{B} \cdot \vec{A} = BA = 0.600T \cdot (5 \times 10^{-2} m)^2 = 1.50 \times 10^{-3} Wb$ 

The change of flux is  $\Delta \Phi_{R} = 0 - 1.50 \times 10^{-3} Wb = -1.50 \times 10^{-3} Wb$ 

Thus the rate of change of the flux is

$$\frac{\Delta \Phi_B}{\Delta t} = \frac{-1.50 \times 10^{-3} Wb}{0.100 s} = -1.50 \times 10^{-2} Wb/s$$

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#### Example 29 – 2, cnt'd

Thus the total emf induced in this period is

$$\varepsilon = -N \frac{d\Phi_B}{dt} = -100 \cdot (-1.50 \times 10^{-2} Wb/s) = 1.5V$$

The induced current in this period is

$$I = \frac{\varepsilon}{R} = \frac{1.5V}{100\Omega} = 1.50 \times 10^{-2} A = 15.0 mA$$

Which direction would the induced current flow? Clockwise

$$E = Pt = I^2 Rt = (1.50 \times 10^{-2} A)^2 \cdot 100\Omega \cdot 0.100s =$$

Force for each coil is  $\vec{F} = I\vec{l} \times \vec{B}$  Force for N coil is  $\vec{F} = NI\vec{l} \times \vec{B}$ 

$$F = NIlB = 100 \cdot (1.50 \times 10^{-2} A) \cdot (4 \times 5 \times 10^{-2}) \cdot 0.600T = 0.045N$$

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 $2.25 \times 10^{-3} J$ 

## EMF Induced on a Moving Conductor

- Another way of inducing emf is using a U shaped conductor with a movable rod resting on it.
- As the rod moves at a speed  $v_i$  it travels vdt in time dt, changing the area of the loop by dA = lvdt.
- time dt, changing the area of the loop by dA = lvdt.  $O O B_{B(outward)}$ • Using Faraday's law, the induced emf for this loop is

$$\left|\varepsilon\right| = \frac{d\Phi_{B}}{dt} = \frac{BdA}{dt} = \frac{Blvdt}{dt} = Blv$$

- This equation is valid as long as B, I and v are perpendicular to each other. What do we do if not?
  - Use the scalar product of vector quantities
- An emf induced on a conductor moving in a magnetic field is called a <u>motional emf</u>



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(a)

## **Electric Generators**

- What does a generator do?
  - Transforms mechanical energy into the electrical energy
  - What does this look like?
    - An inverse of an electric motor which transforms electrical energy to mechanical energy
  - An electric generator is also called a dynamo



- Whose law does the generator based on?
  - Faraday's law of induction



## How does an Electric Generator work?

- An electric generator consists of
  - Many coils of wires wound on an armature that can rotate by mechanical means in a magnetic field
- An emf is induced in the rotating coil
- Electric current is the output of a generator



- Which direction does the output current flow when the armature rotates counterclockwise?
  - The conventional current flows outward on wire A toward the brush
  - After half the revolution the wire A will be where the wire C is and the current flow on A is reversed
- Thus the current produced is alternating its direction



## How does an Electric Generator work?

 Let's assume the loop is rotating in a uniform B field w/ constant angular velocity  $\omega$ . The induced emf is

• 
$$\varepsilon = -\frac{d\Phi_B}{dt} = -\frac{d}{dt}\int \vec{B} \cdot d\vec{A} = -\frac{d}{dt}[BA\cos\theta]$$

- What is the variable that changes above?
  - The angle  $\theta$ . What is  $d\theta/dt$ ?
    - The angular speed  $\omega$ .
  - So  $\theta = \theta_0 + \omega t$

  - If we choose  $\theta_0 = 0$ , we obtain  $\varepsilon = -BA \frac{d}{dt} [\cos \omega t] = BA \omega \sin \omega t$  If the coil contains N loops:  $\varepsilon = -N \frac{d\Phi_B}{dt} = NBA \omega \sin \omega t = \varepsilon_0 \sin \omega t$
  - What is the shape of the output?
    - Sinusoidal w/ amplitude  $\varepsilon_0$ =NBA $\omega$
- US ac frequency is 60Hz. Europe is at 50Hz
  - Most the U.S. power is generated at steam plants





#### Example 29 – 5

An AC generator. The armature of a 60-Hz AC generator rotates in a 0.15-T magnetic field. If the area of the coil is  $2.0x10^{-2}m^2$ , how many loops must the coil contain if the peak output is to be  $\varepsilon_0$ =170V?

The maximum emf of a generator is  $\mathcal{E}_0 = NBA\varpi$ 

Solving for N  

$$N = \frac{\varepsilon_0}{BA\varpi}$$
Since  $\varpi = 2\pi f$  We obtain  

$$N = \frac{\varepsilon_0}{2\pi BAf} = \frac{170V}{2\pi \cdot (0.15T) \cdot (2.0 \times 10^{-2} m^2) \cdot (60s^{-1})} = 150turns$$

N



#### A DC Generator

 A DC generator is almost the same as an ac generator except the slip rings are replaced by splitring commutators



- Output can be smoothed out by placing a capacitor on the output
  - More commonly done using many armature windings



# Eddy Currents (read more in 29-5)

- Induced currents are not always confined to welldefined path
- In some cases where a conductor is moving in and out of the magnetic field, the Lenz's law causes flow of electrons that opposes the change in magnetic flux
  - This change is in the direction that impedes the production of emf
  - And thus causes energy losses
- These currents are called eddy currents
  - Just like the eddy currents in the water that pulls the boat in the opposite direction of the movement

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