# PHYS 1441 – Section 002 Lecture #15

Wednesday, Mar. 12, 2008 Dr. Jaehoon Yu

- Work done by a constant force
- Work-Kinetic Energy Theorem
- Work with friction
- Potential Energy



#### Announcements

- Spring break next week
  - Mar. 17 Mar. 21
  - Have a safe break!
- Term exam #2
  - Wednesday, March 26, in class
  - Will cover CH4.1 whatever we finish Monday, Mar. 24
- Colloquium today at 4pm SH101



# Work Done by a Constant Force

A meaningful work in physics is done only when a sum of forces exerted on an object made a motion to the object.



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What does this mean?

Physically meaningful work is done only by the component of the force along the movement of the object.

Work is an <u>energy transfer</u>!!



# Work Done by a Constant Force



W = Fs1 N·m = 1 joule (J)

#### Table 6.1 Units of Measurement for Work

System	Force	$\times$	Distance	=	Work
SI	newton (N)		meter (m)		joule (J)
CGS	dyne (dyn)		centimeter (cm)		erg
BE	pound (lb)		foot (ft)		foot · pound (ft · lb)



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### Work done by a constant force





 $W = (F\cos\theta)s$ 

 $\cos 90^\circ = 0$ 

 $\cos 180^\circ = -1$ 

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# Ex. 1 Pulling A Suitcase-on-Wheel

Find the work done by a 45.0N force in pulling the suitcase in the figure at an angle  $50.0^{\circ}$  for a distance s=75.0m.



$$W = \left(\sum \vec{F}\right) \cdot \vec{d} = \left| \left(\sum \vec{F}\right) \cos \theta \right| \left| \vec{d} \right|$$
$$= \left(45.0 \cdot \cos 50^\circ\right) \cdot 75.0 = 2170J$$

Does work depend on mass of the object being worked on?

Yes

Why don't I see the mass term in the work at all then?

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It is reflected in the force. If an object has smaller mass, it would take less force to move it at the same acceleration than a heavier object. So it would take less work. Which makes perfect sense, doesn't it?

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# Scalar Product of Two Vectors

- Product of magnitude of the two vectors and the cosine of the • angle between them  $\vec{A} \cdot \vec{B} \equiv |\vec{A}| |\vec{B}| \cos \theta$
- Operation is commutative  $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta = |\vec{B}| |\vec{A}| \cos \theta = \vec{B} \cdot \vec{A}$ ٠
- Operation follows the distribution  $\vec{A} \cdot (\vec{B} + \vec{C}) = \vec{A} \cdot \vec{B} + \vec{A} \cdot \vec{C}$ • law of multiplication
- Scalar products of Unit Vectors  $\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$   $\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0$ •
- How does scalar product look in terms of components? ٠

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k} \qquad \vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$
$$\vec{A} \cdot \vec{B} = \left(A_x \hat{i} + A_y \hat{j} + A_z \hat{k}\right) \cdot \left(B_x \hat{i} + B_y \hat{j} + B_z \hat{k}\right) = \left(A_x B_x \hat{i} \cdot \hat{i} + A_y B_y \hat{j} \cdot \hat{j} + A_z B_z \hat{k} \cdot \hat{k}\right) + Cross terms$$
$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$
$$= 0$$
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### Example of Work by Scalar Product

A particle moving on the xy plane undergoes a displacement d=(2.0i+3.0j)m as a constant force F=(5.0i+2.0j)N acts on the particle.

a) Calculate the magnitude of the displacement and that of the force.

$$\left| \vec{d} \right| = \sqrt{d_x^2 + d_y^2} = \sqrt{(2.0)^2 + (3.0)^2} = 3.6m$$

$$\left| \vec{F} \right| = \sqrt{F_x^2 + F_y^2} = \sqrt{(5.0)^2 + (2.0)^2} = 5.4N$$

b) Calculate the work done by the force F.

$$W = \vec{F} \cdot \vec{d} = \left(2.0\hat{i} + 3.0\hat{j}\right) \cdot \left(5.0\hat{i} + 2.0\hat{j}\right) = 2.0 \times 5.0\hat{i} \cdot \hat{i} + 3.0 \times 2.0\hat{j} \cdot \hat{j} = 10 + 6 = 16(J)$$

Can you do this using the magnitudes and the angle between d and F?

$$W = \overrightarrow{F} \cdot \overrightarrow{d} = \left| \overrightarrow{F} \right| \left| \overrightarrow{d} \right| \cos \theta$$



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# Ex. 2 Bench Pressing and The Concept of Negative Work

A weight lifter is bench-pressing a barbell whose weight is 710N a distance of 0.65m above his chest. Then he lowers it the same distance. The weight is raised and lowered at a constant velocity. Determine the work in the two cases.

What is the angle between the force and the displacement?

$$W = (F \cos 0)s = Fs$$
  
= 710 \cdot 0.65 = +460(J)  
$$W = (F \cos 180)s = -Fs$$
  
= -710 \cdot 0.65 = -460(J)  
What does the negative work mean? The gravitational force does the work on the weight lifter!  
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(c)

# Ex. 3 Accelerating Crate

The truck is accelerating at a rate of +1.50  $m/s^2$ . The mass of the crate is 120-kg and it does not slip. The magnitude of the displacement is 65 m. What is the total work done on the crate by all of the forces acting on it?

What are the forces acting in this motion?

Gravitational force on the crate, weight, W or F<sub>a</sub>

Normal force force on the crate,  $F_{N}$ 

Static frictional force on the crate,  $f_s$ 





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# Ex. 3 Continued...

Let's figure what the work done by each force in this motion is.

Work done by the gravitational force on the crate, W or F<sub>q</sub>

$$W = \left(F_g \cos\left(-90^o\right)\right)s = 0$$

Work done by Normal force force on the crate,  ${\bf F}_{\rm N}$ 

$$W = \left(F_g \cos\left(+90^o\right)\right)s = 0$$

Work done by the static frictional force on the crate,  $f_s$ 

$$f_s = ma = (120 \text{ kg})(1.5 \text{ m/s}^2) = 180\text{N}$$
  
 $W = f_s \cdot s = [(180\text{N})\cos 0](65 \text{ m}) = 1.2 \times 10^4 \text{J}$ 

Which force did the work? Static frictional force on the crate,  $f_s$ 

How? By holding on to the crate so that it moves with the truck!

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(b) Free-body diagram

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for the crate

#### Kinetic Energy and Work-Kinetic Energy Theorem

- Some problems are hard to solve using Newton's second law
  - If forces exerting on an object during the motion are complicated
  - Relate the work done on the object by the net force to the change of the speed of the object







When a net external force by the jet engine does work on and object, the kinetic energy of the object changes according to

$$W = KE_{f} - KE_{o} = \frac{1}{2}mv_{f}^{2} - \frac{1}{2}mv_{o}^{2}$$

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# Ex. 4 Deep Space 1

The mass of the space probe is 474-kg and its initial velocity is 275 m/s. If the 56.0-mN force acts on the probe parallel through a displacement of  $2.42 \times 10^{9}$ m, what is its final speed?



#### Ex. 6 Satellite Motion and Work By the Gravity

A satellite is moving about the earth in a circular orbit and an elliptical orbit. For these two orbits, determine whether the kinetic energy of the satellite changes during the motion.

For a circular orbit No change! Why not?

Gravitational force is the only external force but it is perpendicular to the displacement. So no work.

For an elliptical orbit Changes! Why? Gravitational force is the only external force but its angle with respect to the displacement varies. So it performs work.





#### Work and Energy Involving Kinetic Friction

- What do you think the work looks like if there is friction?
  - Static friction does not matter! Why? It isn't there when the object is moving.
  - Then which friction matters? Kinetic Friction

 $\mathcal{F}_{fr}$  M M  $\mathcal{V}_i$   $\mathcal{V}_f$  d Friction force  $\mathcal{F}_{fr}$  works on the object to slow down

The work on the object by the friction  $\mathcal{F}_{fr}$  is

$$W_{fr} = F_{fr} d \cos(180) = -F_{fr} d \quad \Delta K E = F_{fr} d$$

The negative sign means that the work is done on the friction!!

The final kinetic energy of an object, taking into account its initial kinetic energy, friction force and other source of work, is

$$KE_{f} = KE_{i} + \sum W - F_{fr}d$$

$$t=0, KE_{i}$$

$$Friction, t=T, KE_{f}$$
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$$Friction, t=T, KE_{f}$$

$$Friction, t=T, KE_{f}$$

#### Ex. 5 Downhill Skiing

A 58kg skier is coasting down a 25° slope. A kinetic frictional force of magnitude  $f_k$ =70N opposes her motion. Neat the top of the slope, the skier's speed is  $v_0=3.6$  m/s. Ignoring air resistance, determine the speed  $v_f$  at the point that is displaced 57m downhill.

What are the forces in this motion?

Gravitational force: F<sub>a</sub>

mg sin 25° mg cos 25° (b) Free-body diagram for the skier (a)

What are the X and Y component of the net force in this motion?

Y component  $\sum F_{y} = F_{gy} + F_{N} = -mg \cos 25^{\circ} + F_{N} = 0$ From this we obtain  $F_N = mg \cos 25^\circ = 58 \cdot 9.8 \cdot \cos 25^\circ = 515N$ What is the coefficient of kinetic friction?  $f_k = \mu_k F_N$   $\mu_k = \frac{f_k}{F_{...}} = \frac{70}{515} = 0.14$ 

Normal force:  $F_N$  Kinetic frictional force:  $f_k$ 

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#### **Example of Work Under Friction**

A 6.0kg block initially at rest is pulled to East along a horizontal surface with coefficient of kinetic friction  $\mu_k$ =0.15 by a constant horizontal force of 12N. Find the speed of the block after it has moved 3.0m.

Using work-kinetic energy theorem and the fact that initial speed is 0, we obtain

$$W = W_F + W_k = \frac{1}{2} m v_f^2$$
Solving the equation  
for  $v_{f}$  we obtain
$$v_f = \sqrt{\frac{2W}{m}} = \sqrt{\frac{2 \times 10}{6.0}} = 1.8m/s$$
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