## PHYS 1441 – Section 002 Lecture #16

Monday, Mar. 24, 2008 Dr. **Jae**hoon **Yu** 

- Potential Energy
- Conservative and Non-conservative Forces
- Conservation of Mechanical Energy
- Power

Today's homework is homework #8, due 9pm, Monday, Mar. 31!!



### Announcements

- Term exam #2
  - This Wednesday, March 26, in class
  - Will cover CH4.1 CH6.6
  - Mixture of multiple choice problems and numeric problems
  - Practice problems can be found at the URL:
    - <u>http://www-hep.uta.edu/~yu/teaching/spring08-1441-</u> 002/lectures.html
- Reading assignment: CH6.9



### Work and Kinetic Energy

A meaningful work in physics is done only when the sum of the forces exerted on an object made a motion to the object.

What does this mean?

However much tired your arms feel, if you were just holding an object without moving it you have not done any physically meaningful work to the object.

Mathematically, the work is written as the product of magnitudes of the net force vector, the magnitude of the displacement vector and cosine of the angle between them.

$$W = \sum_{i=1}^{n} \left( \overrightarrow{F}_{i} \right) \cdot \overrightarrow{d} = \left| \sum_{i=1}^{n} \left( \overrightarrow{F}_{i} \right) \right| \left| \overrightarrow{d} \right| \cos \theta$$

Kinetic Energy is the energy associated with the motion and capacity to perform work. Work causes change of KE after the completion  $\clubsuit$  Work-Kinetic energy theorem

$$K = \frac{1}{2}mv^2$$

$$\sum W = K_f - K_i = \Delta K$$

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### Potential Energy

Energy associated with a system of objects  $\rightarrow$  Stored energy which has the potential or the possibility to work or to convert to kinetic energy

What does this mean?

In order to describe potential energy, PE, a system must be defined.

The concept of potential energy can only be used under the special class of forces called the conservative force which results in the principle of conservation of mechanical energy.

 $E_{M} \equiv K E_{i} + P E_{i} = K E_{f} + P E_{f}$ 

What are other forms of energies in the universe?

Mechanical Energy Chemical Energy

Biological Energy

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*Electromagnetic Energy* 

Nuclear Energy

These different types of energies are stored in the universe in many different forms!!!

If one takes into account ALL forms of energy, the total energy in the entire universe is conserved. It just transforms from one form to another.

# Gravitational Potential Energy

The potential energy is given to an object by the gravitational field in the system of Earth by virtue of the object's height from an arbitrary zero level

When an object is falling, the gravitational force, Mg, performs the work on the object, increasing the object's kinetic energy. So the potential energy of an object at a height y, which is the potential to do work is expressed as

$$PE = \vec{F}_g \cdot \vec{y} = \left| \vec{F}_g \right| \left| \vec{y} \right| \cos \theta = \left| \vec{F}_g \right| \left| \vec{y} \right| = mgh \qquad PE \equiv mgh$$

The work done on the object by the gravitational force as the brick drops from  $h_i$  to  $h_f$  is:

 $W_g = PE_i - PE_f$  $= mgh_i - mgh_f = -\Delta PE$ 

What doesWork by the gravitational force as the brick drops from h<sub>i</sub> to h<sub>f</sub>this mean?Work by the negative change of the system's potential energy

 $\mathcal{M}$ 

m

 $h_{f}$ 

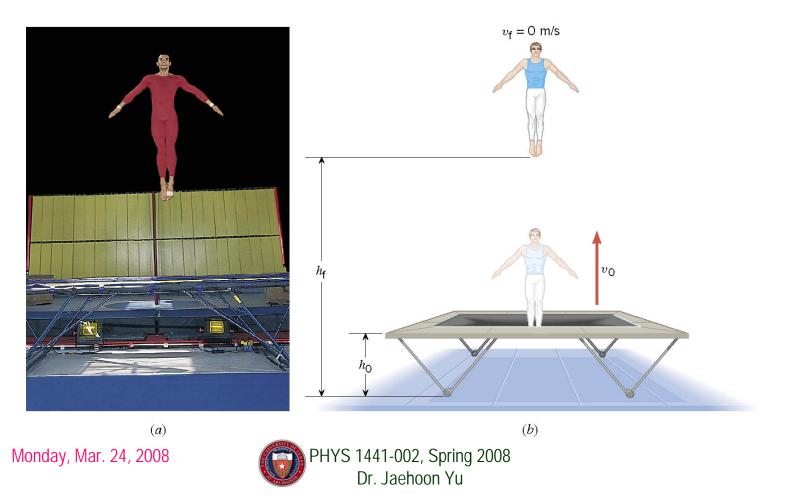
 $h_i$ 

тg

Potential energy was spent in order for the gravitational force to increase the brick's kinetic energy.

## Ex. 7 A Gymnast on a Trampoline

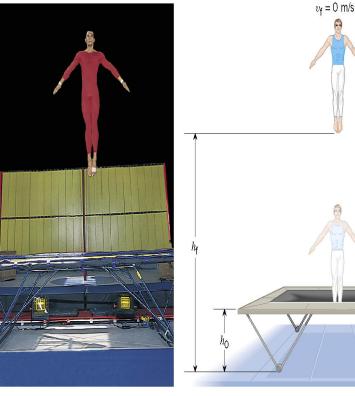
A gymnast leaves the trampoline at an initial height of 1.20 m and reaches a maximum height of 4.80 m before falling back down. What was the initial speed of the gymnast?



## Ex. 7 Continued

From the work-kinetic energy theorem

$$\mathbf{W} = \frac{1}{2}mv_{\rm f}^2 - \frac{1}{2}mv_o^2$$





Work done by the gravitational force

$$W_{\text{gravity}} = mg\left(h_o - h_f\right)$$

Since at the maximum height, the final speed is 0. Using work-KE theorem, we obtain

$$\eta hg\left(h_o - h_f\right) = -\frac{1}{2}\eta hv_o^2$$

$$v_o = \sqrt{-2g\left(h_o - h_f\right)}$$

 $\therefore v_o = \sqrt{-2(9.80 \,\mathrm{m/s^2})(1.20 \,\mathrm{m} - 4.80 \,\mathrm{m})} = 8.40 \,\mathrm{m/s}$ 

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(a)



vo

(b)

### **Example for Potential Energy**

A bowler drops bowling ball of mass 7kg on his toe. Choosing the floor level as y=0, estimate the total work done on the ball by the gravitational force as the ball falls on the toe.

Let's assume the top of the toe is 0.03m from the floor and the hand was 0.5m above the floor.



$$U_{i} = mgy_{i} = 7 \times 9.8 \times 0.5 = 34.3J \quad U_{f} = mgy_{f} = 7 \times 9.8 \times 0.03 = 2.06J$$
$$W_{g} = -\Delta U = -\left(U_{f} - U_{i}\right) = 32.24J \cong 30J$$

b) Perform the same calculation using the top of the bowler's head as the origin.

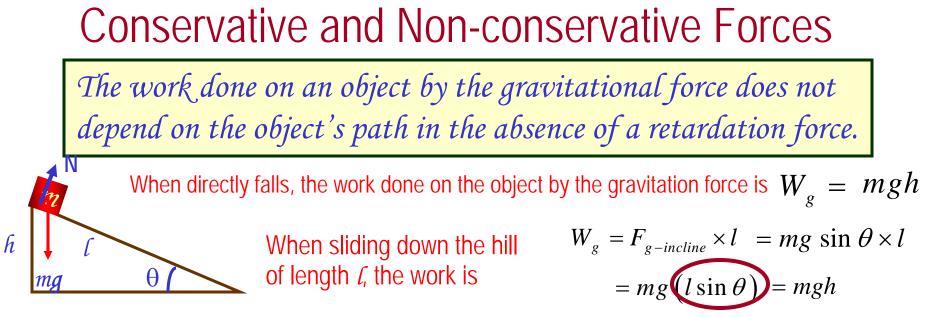
What has to change? First we must re-compute the positions of the ball in his hand and on his toe.

Assuming the bowler's height is 1.8m, the ball's original position is –1.3m, and the toe is at –1.77m.

$$U_{i} = mgy_{i} = 7 \times 9.8 \times (-1.3) = -89.2J \quad U_{f} = mgy_{f} = 7 \times 9.8 \times (-1.77) = -121.4J$$
$$W_{g} = -\Delta U = -(U_{f} - U_{i}) = 32.2J \cong 30J$$

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How about if we lengthen the incline by a factor of 2, keeping the height the same??

 $= mg(l\sin\theta) = mg$ Still the same
amount of work  $\odot$ 

 $W_g = mgh$ 

So the work done by the gravitational force on an object is independent of the path of the object's movements. It only depends on the difference of the object's initial and final position in the direction of the force.

Forces like gravitational and elastic forces are called the conservative force

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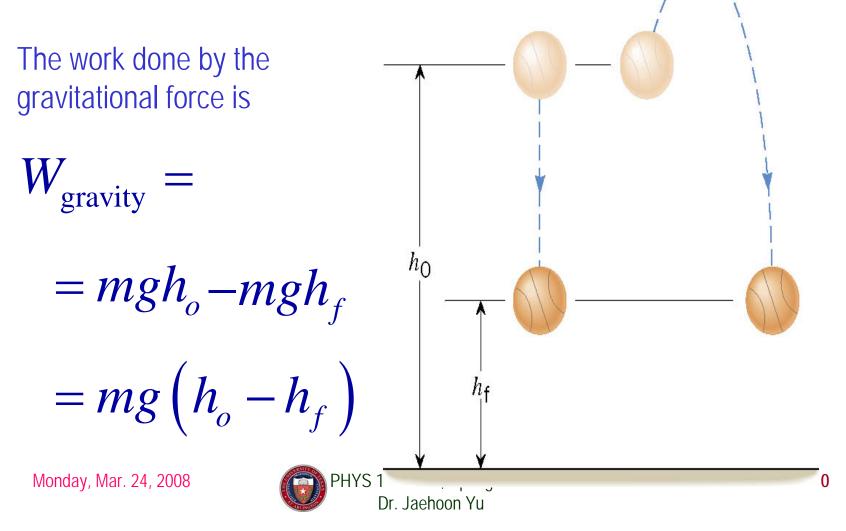
If the work performed by the force does not depend on the path.
 If the work performed on a closed path is 0.

Total mechanical energy is conserved!!

$$E_M \equiv KE_i + PE_i = KE_f + PE_f$$



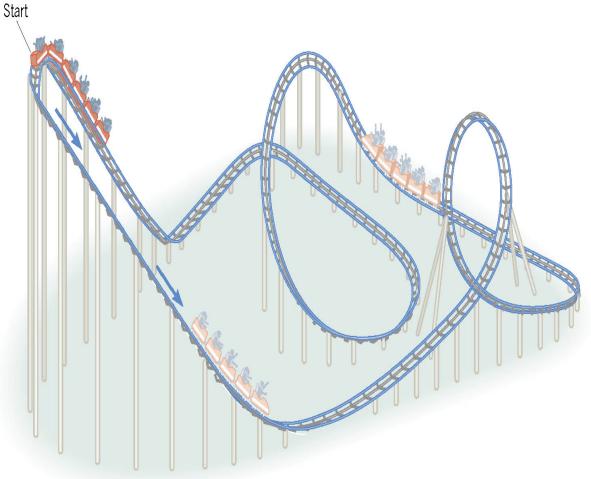
A force is conservative when the work it does on a moving object is independent of the path between the object's initial and final positions.



A force is conservative when it does no work on an object moving around a closed path, starting and finishing at the same point.

The work done by the gravitational force is

 $W_{\text{gravity}} = mg(h_o - h_f)$ since  $h_o = h_f$  $W_{\text{gravity}} = 0$ 



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## So what is the conservative force again?

- A force is conservative when the work it does on a moving object is independent of the path between the object's initial and final positions.
- A force is conservative when it does no work on an object moving around a closed path, starting and finishing at the same point.
- The work is done by a conservative force, the total mechanical energy of the system is conserved!

$$E_M \equiv KE_i + PE_i = KE_f + PE_f$$



Some examples of conservative and non-conservative forces

Table 6.2Some Conservativeand Nonconservative Forces

#### **Conservative** Forces

Gravitational force (Ch. 4) Elastic spring force (Ch. 10) Electric force (Ch. 18, 19)

#### Nonconservative Forces

Static and kinetic frictional forces

Air resistance

Tension

Normal force

Propulsion force of a rocket



## Non-conservative force

An example of a non-conservative force is the kinetic frictional force.

$$W = (F\cos\theta)s = f_k\cos 180^\circ s = -f_ks$$

The work done by the kinetic frictional force is always negative. Thus, it is impossible for the work it does on an object that moves around a closed path to be zero.

The concept of potential energy is not defined for a nonconservative force.



## Work-Energy Theorem

In normal situations both conservative and non-conservative forces act simultaneously on an object, so the work done by the net external force can be written as

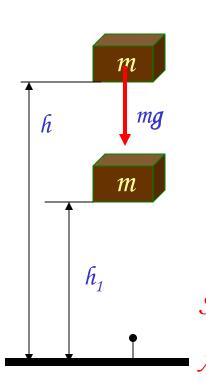
 $W = W_{c} + W_{nc}$   $W = KE_{f} - KE_{o} = \Delta KE$   $W_{c} = W_{gravity} = mgh_{o} - mgh_{f} = PE_{o} - PE_{f} =$   $= -(PE_{f} - PE_{o}) = -\Delta PE$   $\Delta KE = -\Delta PE + W_{nc}$   $W_{nc} = \Delta KE + \Delta PE \text{ THE WORK-ENERGY THEOREM}$ 

Work done by a non-conservative force causes changes in kinetic energy as well as the potential energy (or the total mechanical energy) of an object in motion.

### Conservation of Mechanical Energy

Total mechanical energy is the sum of kinetic and potential energies

$$E \equiv KE + PE$$



Let's consider a brick of mass *m* at the height *h* from the ground

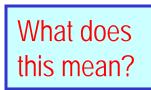
What is the brick's potential energy?  $PE_{o} = mgh$ 

 $E_i = E_f$ 

What happens to the energy as the brick falls to the ground?  $\Delta PE = PE_f - PE_0$ 

v = gtThe brick gains speed By how much? So what? The brick's kinetic energy increased  $K = \frac{1}{2}mv^2 = \frac{1}{2}m(gt)^2$ 

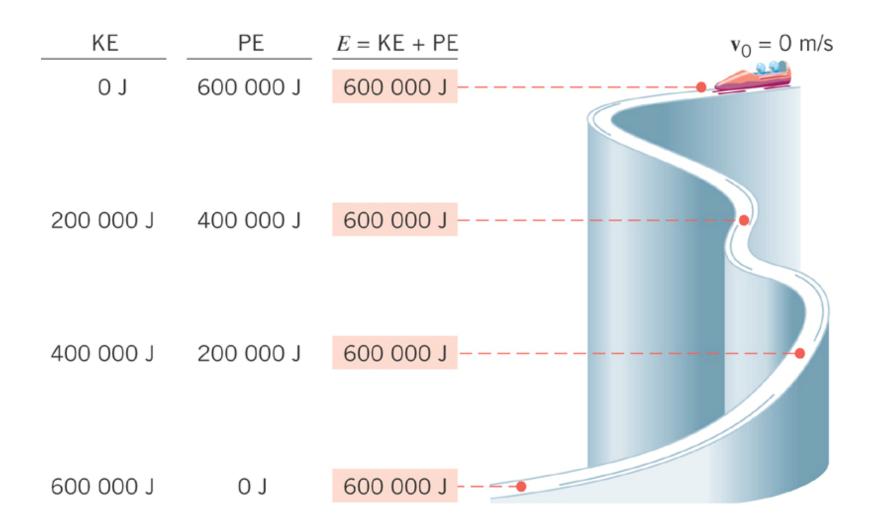
The lost potential energy is converted to kinetic energy!! And?

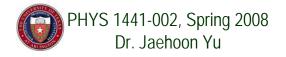


The total mechanical energy of a system remains constant in any isolated system of objects that interacts only through *conservative forces*:  $K_i + \sum PE_0 = K_f + \sum PE_f$ Principle of mechanical energy conservation 02, Spring 2008

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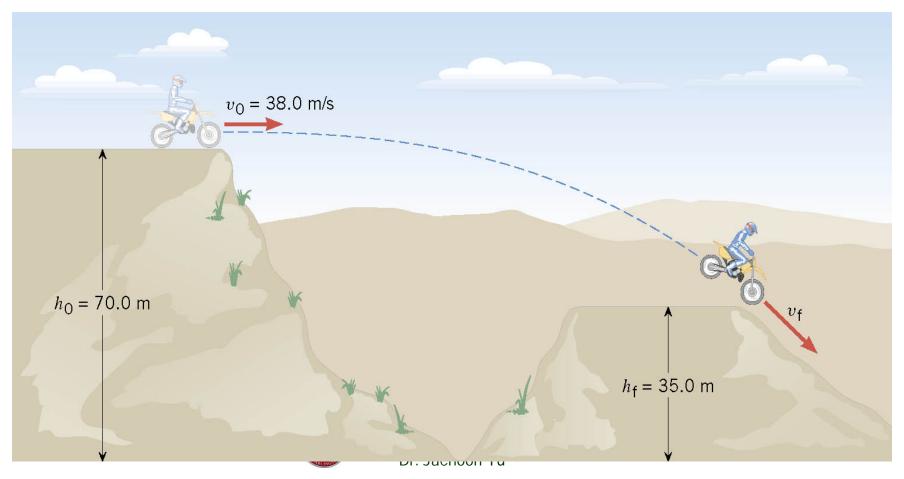
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## Ex.8: Daredevil Motorcyclist

A motorcyclist is trying to leap across the canyon by driving horizontally off a cliff 38.0 m/s. Ignoring air resistance, find the speed with which the cycle strikes the ground on the other side.



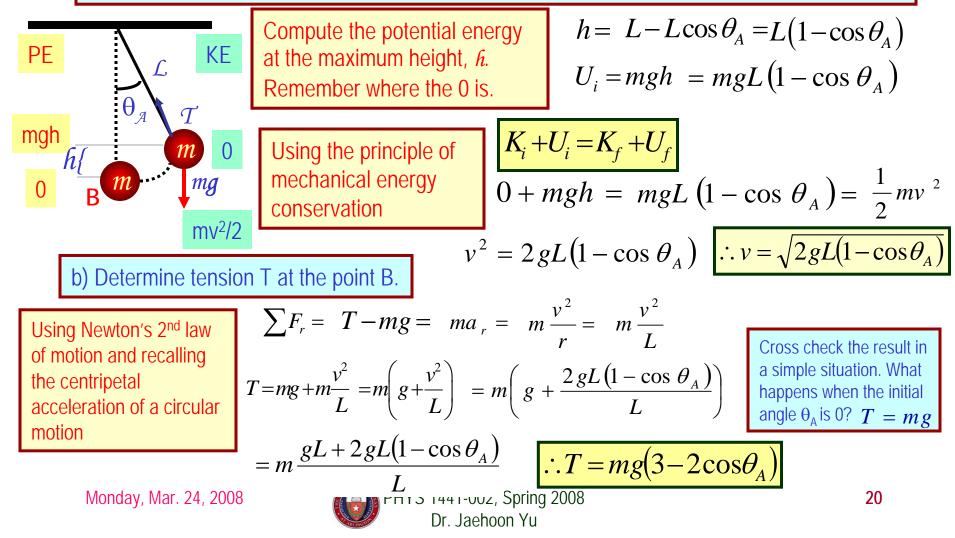
Using Mechanical Energy Conservation			
	v <sub>0</sub> = 38.0 m/s		$\eta hgh_o + \frac{1}{2}\eta hv_o^2 = \eta hgh_f + \frac{1}{2}\eta hv_f^2$
			$gh_o + \frac{1}{2}v_o^2 = gh_f + \frac{1}{2}v_f^2$
$h_0 = 70.0 \text{ m}$ $v_f$ $h_f = 35.0 \text{ m}$			$v_f^2 = 2g\left(h_o - h_f\right) + v_0^2$
			Solve for v <sub>f</sub>
PE	$mgh_o$	$mgh_{f}$	
κ <sup>+</sup> ΚΕ	$\frac{1}{2}mv_o^2$	$\frac{1}{2}mv_f^2$	$v_f = \sqrt{2g\left(h_o - h_f\right) + v_o^2}$
ME	$mgh_o + \frac{1}{2}mv_o^2$	$mgh_f + \frac{1}{2}mv_f^2$	$v_f = \sqrt{2(9.8 \mathrm{m/s^2})(35.0 \mathrm{m}) + (38.0 \mathrm{m/s})^2} =$
$E_{o} = E_{f} = mgh_{o} + \frac{1}{2}mv_{o}^{2} = mgh_{f} + \frac{1}{2}mv_{f}^{2}$			$= 46.2 \mathrm{m/s}$

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### Example

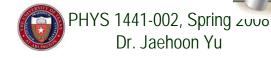
A ball of mass *m* is attached to a light cord of length L, making up a pendulum. The ball is released from rest when the cord makes an angle  $\theta_A$  with the vertical, and the pivoting point P is frictionless. Find the speed of the ball when it is at the lowest point, B.



## Ex. 12 Fireworks

A 0.2kg rocket in a fireworks display is launched from rest and follows an erratic flight path to reach the point P in the figure. Point P is 29m above the starting point. In the process, 425J of work is done on the rocket by the nonconservative force generated by the burning propellant. Ignoring air resistance and the mass lost due to the burning propellant, what is the final speed of the rocket?

$$W_{nc} = ME_f - ME_0$$
$$= \left(mgh_f + \frac{1}{2}mv_f^2\right)$$
$$-\left(mgh_o + \frac{1}{2}mv_o^2\right)$$



P

 $\vec{\mathbf{v}}_{\mathbf{0}} = 0 \text{ m/s}$ 

29 m

ho

hf

