PHYS 1443 – Section 001 Lecture #22

Monday, May 2, 2011 Dr. **Jae**hoon **Yu**

- Absolute and Gauge Pressure
- Buoyant Force and Archimedes' Principle
- Equation of Continuity
- Bernoulli's Principle



Announcements

- Planetarium extra credit sheets due today!!
- Quiz #5 this Wednesday, May 4
 - Covers from CH. 11 CH13.14
- Final comprehensive exam
 - 11am, Monday, May 9, in SH103
 - Covers: Chapter 1.1 CH13. 14 + appendices
 - Review: Wednesday, May 4th, in the class after the quiz
 - Attendance will be taken
- Colloquium this Wednesday at 4pm



Absolute and Relative Pressure

How can one measure pressure?



One can measure the pressure using an open-tube manometer, where one end is connected to the system with unknown pressure P and the other open to air with pressure P_0 .

The measured pressure of the system is $P = P_0 + \rho g h$

This is called the <u>absolute pressure</u>, because it is the actual value of the system's pressure.

In many cases we measure the pressure difference with respect to the atmospheric pressure to avoid the effect of the changes in P_0 that depends on the environment. This is called **gauge or relative pressure**.

$$P_G = P - P_0 = \rho g h$$

The common barometer which consists of a mercury column with one end closed at vacuum and the other open to the atmosphere was invented by Evangelista Torricelli.

Since the closed end is at vacuum, it does not exert any force. 1 atm of air pressure pushes mercury up 76cm. So 1 atm is $P_0 = \rho g h = (13.595 \times 10^3 kg / m^3)(9.80665m / s^2)(0.7600m)$ $= 1.013 \times 10^5 Pa = 1atm$

If one measures the tire pressure with a gauge at 220kPa the actual pressure is 101kPa+220kPa=303kPa.

Finger Holds Water in Straw



Buoyant Forces and Archimedes' Principle

Why is it so hard to put an inflated beach ball under water while a small piece of steel sinks in the water easily?

The water exerts force on an object immersed in the water. This force is called the **buoyant force**.

How large is the
buoyant force?The magnitude of the buoyant force always equals the weight of the
fluid in the volume displaced by the submerged object.

This is called the Archimedes' principle. What does this mean?



Let's consider a cube whose height is **h** and is filled with fluid and in its equilibrium so that its weight **Mg** is balanced by the buoyant force **B**.

 $B = F_g = Mg$ The pressure at the bottom of the cube is larger than the top by pgh.

Therefore,
$$\Delta P = B / A = \rho g h$$

 $B = \Delta PA = \rho ghA = \rho Vg$

$$B = \rho V g = M g = F_g$$

Where **Mg** is the weight of the fluid in the cube.



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More Archimedes' Principle

Let's consider the buoyant force in two special cases.

Case 1: Totally submerged object Let's consider an object of mass **M**, with density ρ_0 , is fully immersed in the fluid with density ρ_f .

The magnitude of the buoyant force is $B = \rho_f V g$

The weight of the object is $F_g = Mg = \rho_0 Vg$

Therefore total force in the system is $F = B - F_g = (\rho_f - \rho_0)Vg$

What does this tell you?

- The total force applies to different directions depending on the difference of the density between the object and the fluid.
- If the density of the object is <u>smaller</u> than the density of the fluid, the buoyant force will <u>push the object</u> up to the surface.
- 2. If the density of the object is <u>larger</u> than the fluid's, the object will <u>sink to the bottom</u> of the fluid.



More Archimedes' Principle

Case 2: Floating object

Let's consider an object of mass **M**, with density ρ_0 , is in static equilibrium floating on the surface of the fluid with density ρ_f , and the volume submerged in the fluid is V_f

h Mg B

The magnitude of the buoyant force is $B = \rho_f V_f g$ The weight of the object is $F_g = Mg = \rho_0 V_0 g$

Therefore total force of the system is

Since the system is in static equilibrium

$$F = B - F_g = \rho_f V_f g - \rho_0 V_0 g = 0$$

$$\rho_f V_f g = \rho_0 V_0 g$$

$$\frac{\rho_0}{\rho_f} = \frac{V_f}{V_0}$$

What does this tell you?

Since the object is floating, its density is smaller than that of the fluid.

The ratio of the densities between the fluid and the object determines the submerged volume under the surface.



Ex.13 – 10 for Archimedes' Principle

Archimedes was asked to determine the purity of the gold used in the crown. The legend says that he solved this problem by weighing the crown in air and in water. Suppose the scale read 7.84N in air and 6.86N in water. What should he have to tell the king about the purity of the gold in the crown?

In the air the tension exerted by the scale on the object is the weight of the crown In the water the tension exerted by the scale on the object is T_{water}

Therefore the buoyant force B is

Since the buoyant force B is The volume of the displaced

water by the crown is

Therefore the density of the crown is

$$T_{air} = mg = 7.84N$$

$$T_{water} = mg - B = 6.86N$$

$$B = T_{air} - T_{water} = 0.98N$$

$$B = \rho_w V_w g = \rho_w V_c g = 0.98N$$
$$V_c = V_w = \frac{0.98N}{\rho_w g} = \frac{0.98}{1000 \times 9.8} = 1.0 \times 10^{-4} m^3$$

$$\rho_c = \frac{m_c}{V_c} = \frac{m_c g}{V_c g} = \frac{7.84}{V_c g} = \frac{7.84}{1.0 \times 10^{-4} \times 9.8} = 8.0 \times 10^3 kg / m^3$$

Mond Since the density of pure gold is 19.3x10³kg/m³, this crown is not made of pure gold. Br. Jaenoon Yu

Example for Buoyant Force

What fraction of an iceberg is submerged in the sea water?

Let's assume that the total volume of the iceberg is V_i . Then the weight of the iceberg F_{gi} is

$$F_{gi} = \rho_i V_i g$$

Let's then assume that the volume of the iceberg submerged in the sea water is V_w. The buoyant force B $B = \rho_w V_w g$ caused by the displaced water becomes

Since the whole system is at its static equilibrium, we obtain Therefore the fraction of the volume of the iceberg submerged under the surface of

$$\rho_i V_i g = \rho_w V_w g$$
$$\frac{V_w}{V_i} = \frac{\rho_i}{\rho_w} = \frac{917 kg / m^3}{1030 kg / m^3} = 0.890$$

About 90% of the entire iceberg is submerged in the water!!!

the sea water is



Flow Rate and the Equation of Continuity

Study of fluid in motion: Fluid Dynamics

If the fluid is water: Water dynamics?? Hydro-dynamics

Streamline or Laminar flow: Each particle of the fluid follows a smooth path, a streamline
 Turbulent flow: Erratic, small, whirlpool-like circles called eddy current or eddies which absorbs a lot of energy

Flow rate: the mass of fluid that passes the given point per unit time $\Delta m / \Delta t$



Ex. 13 – 14 for Equation of Continuity

How large must a heating duct be if air moving at 3.0m/s through it can replenish the air in a room of 300m³ volume every 15 minutes? Assume the air's density remains constant.



Using equation of continuity

 $\rho_1 A_1 v_1 = \rho_2 A_2 v_2$

Since the air density is constant

 $A_1v_1 = A_2v_2$ Now let's imagine the room as the large section of the duct

$$A_{1} = \frac{A_{2}v_{2}}{v_{1}} = \frac{A_{2}l_{2}/t}{v_{1}} = \frac{V_{2}}{v_{1}} = \frac{V_{2}}{v_{1}} = \frac{300}{3.0 \times 900} = 0.11m^{2}$$
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Bernoulli's Principle

Bernoulli's Principle: Where the velocity of fluid is high, the pressure is low, and where the velocity is low, the pressure is high.



Bernoulli's Equation cont'd

The total amount of the work done on the fluid is

 $W = W_1 + W_2 + W_3 = P_1 A_1 \Delta l_1 - P_2 A_2 \Delta l_2 - mgy_2 + mgy_1$

From the work-energy principle

 $\frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2 \neq P_1A_1\Delta l_1 - P_2A_2\Delta l_2 - mgy_2 + mgy_1$

Since the mass m is contained in the volume that flowed in the motion

$$A_1 \Delta l_1 = A_2 \Delta l_2$$
 and $m = \rho A_1 \Delta l_1 = \rho A_2 \Delta l_2$

hus,
$$\frac{1}{2}\rho A_2 \Delta l_2 v_2^2 - \frac{1}{2}\rho A_1 \Delta l_1 v_1^2$$

 $= P_1 A_1 \Delta l_1 - P_2 A_2 \Delta l_2 - \rho A_2 \Delta l_2 g y_2 + \rho A_1 \Delta l_1 g y_1$

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Since

$$\frac{1}{2}\rho A A_{l_2}v_2^2 - \frac{1}{2}\rho A A_{l_1}v_1^2 = P_1AA_{l_1} - P_2AA_{l_2} - \rho A A_{l_2}gy_2 + \rho A A_{l_1}gy_1$$
We
obtain

$$\frac{1}{2}\rho v_2^2 - \frac{1}{2}\rho v_1^2 = P_1 - P_2 - \rho gy_2 + \rho gy_1$$
Re-
organize

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho gy_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho gy_2$$
Bernoulli's
Equation
Thus, for any two
points in the flow

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho gy_1 = const.$$
For static fluid

$$P_2 = P_1 + \rho g (y_1 - y_2) = P_1 + \rho g h$$
Pascal's
Law
For the same heights

$$P_2 = P_1 + \frac{1}{2}\rho (v_1^2 - v_2^2)$$

The pressure at the faster section of the fluid is smaller than slower section.

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Ex. 13 – 15 for Bernoulli's Equation

Water circulates throughout a house in a hot-water heating system. If the water is pumped at the speed of 0.5m/s through a 4.0cm diameter pipe in the basement under a pressure of 3.0atm, what will be the flow speed and pressure in a 2.6cm diameter pipe on the second 5.0m above? Assume the pipes do not divide into branches.

Using the equation of continuity, flow speed on the second floor is

$$v_2 = \frac{A_1 v_1}{A_2} = \frac{\pi r_1^2 v_1}{\pi r_2^2} = 0.5 \times \left(\frac{0.020}{0.013}\right)^2 = 1.2 \, m \, / \, s$$

Using Bernoulli's equation, the pressure in the pipe on the second floor is

$$P_{2} = P_{1} + \frac{1}{2} \rho \left(v_{1}^{2} - v_{2}^{2} \right) + \rho g \left(y_{1} - y_{2} \right)$$

= 3.0×10⁵ + $\frac{1}{2}$ 1×10³ (0.5² - 1.2²)+1×10³×9.8×(-5)
= 2.5×10⁵ N/m²

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Congratulations!!!! You all are impressive and have done very well!!! I certainly had a lot of fun with ya'll and am truly proud of you! Good luck with your exam!!!

Have safe holidays!!

