

PHYS 1442 – Section 001

Lecture #7

Wednesday, July 1, 2009

Dr. Jaehoon Yu

- Chapter 19
 - EMF and Terminal Voltage
 - Resistors in Series and Parallel
 - Energy losses in Resistors
 - Kirchhoff's Rules
 - EMFs in Series and Parallel
 - Capacitors in Series and Parallel
 - RC Circuits
 - Electric Hazards

Today's homework is #4, due 9pm, Thursday, July 9!!

Wednesday, July 1, 2009



PHYS 1442-001, Summer 2009 Dr.
Jaehoon Yu

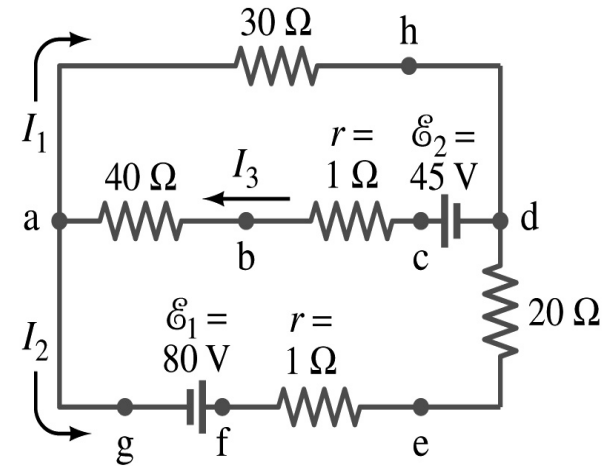
Announcements

- Quiz #3
 - At the beginning of the class next Wednesday, July 8
 - Covers CH19+ What we finish Monday, July 6
- Reading assignments: CH19 – 4, CH19-7 and CH19-8



Special Project

1. Calculate the currents I_1 , I_2 and I_3 in each of the branches of the circuit in the figure. Choose two different junctions for the second rule. (15 points)



2. Do the same as above but this time change the direction of one of the currents I_1 or I_2 and pick yet two other junctions than the ones used above and explain the result. (15 points)

3. You must show your own detailed work. Do not copy from the book or your friend's work! You will get 0 upon any indication of copying.

4. Due for this project is Wednesday, July 8.

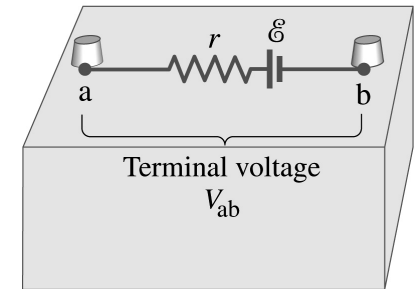


EMF and Terminal Voltage

- What do we need to have current in an electric circuit?
 - A device that provides a potential difference, such as a battery or a generator
 - They normally convert some types of energy into electric energy
 - These devices are called source of the electromotive force (emf)
 - emf does NOT refer to a real “force”.
- Potential difference between terminals of an emf source, when no current flows to an external circuit, is called the emf ($\mathcal{E}$) of the source. What is the unit of the emf? V
- Battery itself has some **internal resistance** (r) due to the flow of charges in the electrolyte
 - Why does the headlight dim when you start the car?
 - The starter needs a large amount of current but the battery cannot provide charge fast enough to supply current to both the starter and the headlight



EMF and Terminal Voltage

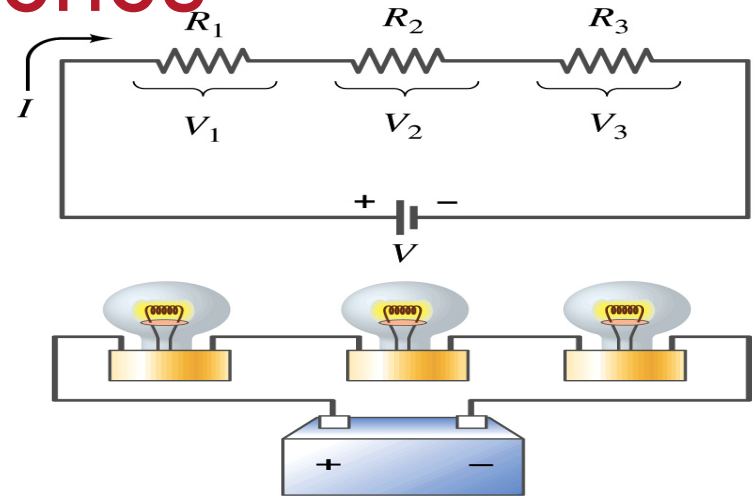


- Since the internal resistance is inside the battery, we can never separate them out.
- So the terminal voltage difference is $V_{ab} = V_a - V_b$.
- When no current is drawn from the battery, the terminal voltage equals the emf which is determined by the chemical reaction; $V_{ab} = \mathcal{E}$.
- However when the current I flows naturally from the battery, there is an internal drop in voltage which is equal to Ir . Thus the actual **delivered** terminal voltage of a battery in a circuit is $V_{ab} = \mathcal{E} - Ir$.

Resisters in Series

- Resisters are in series when two or more resisters are connected end to end

- These resisters represent simple resisters in circuit or electrical devices, such as light bulbs, heaters, dryers, etc



- What is the same in a circuit connected in series?
 - Current is the same through all the elements in series
- Potential difference across every element in the circuit is
 - $V_1=IR_1$, $V_2=IR_2$ and $V_3=IR_3$
- Since the total potential difference is V , we obtain
 - $V=IR_{eq}=V_1+V_2+V_3=I(R_1+R_2+R_3)$
 - Thus, $R_{eq}=R_1+R_2+R_3$

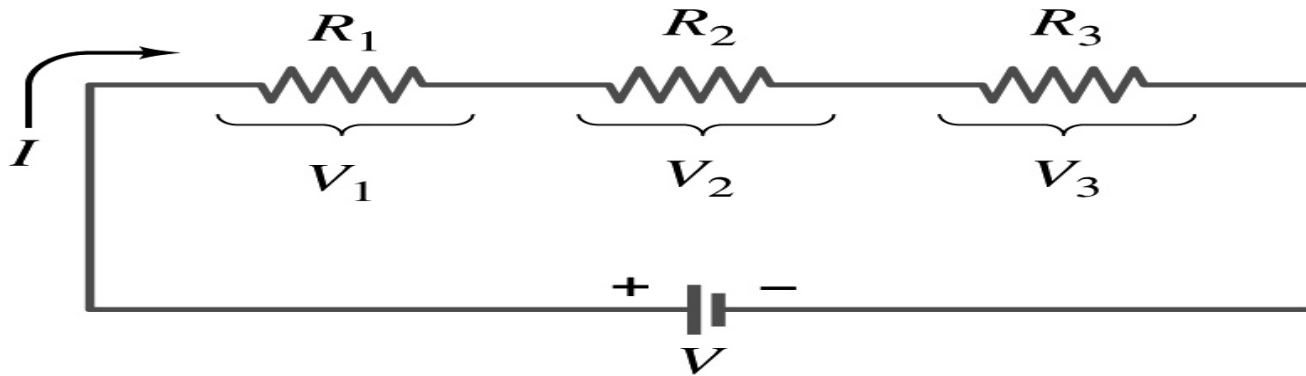
$$R_{eq} = \sum_i R_i$$

Resisters
in series

When resisters are connected in series, the total resistance increases and the current decreases.

Energy Losses in Resistors

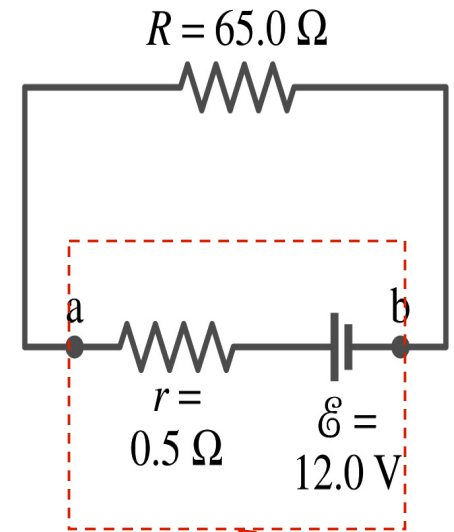
- Why is it true that $V=V_1+V_2+V_3$?



- What is the potential energy loss when charge q passes through the resistor R_1 , R_2 and R_3 ?
 - $\Delta U_1=qV_1$, $\Delta U_2=qV_2$, $\Delta U_3=qV_3$
- Since the total energy loss should be the same as the energy provided to the system, we obtain
 - $\Delta U=qV=\Delta U_1+\Delta U_2+\Delta U_3=q(V_1+V_2+V_3)$
 - Thus, $V=V_1+V_2+V_3$

Example 19 – 1

Battery with internal resistance. A $65.0\text{-}\Omega$ resistor is connected to the terminals of a battery whose emf is 12.0V and whose internal resistance is $0.5\text{-}\Omega$. Calculate (a) the current in the circuit, (b) the terminal voltage of the battery, V_{ab} , and (c) the power dissipated in the resistor R and in the battery's internal resistor.



What is this?

A battery or a source of emf.

(a) Since $V_{ab} = \varepsilon - Ir$ We obtain $V_{ab} = IR = \varepsilon - Ir$

Solve for I

$$I = \frac{\varepsilon}{R + r} = \frac{12.0\text{V}}{65.0\Omega + 0.5\Omega} = 0.183\text{A}$$

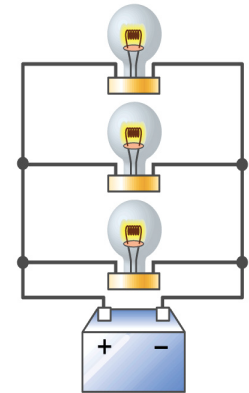
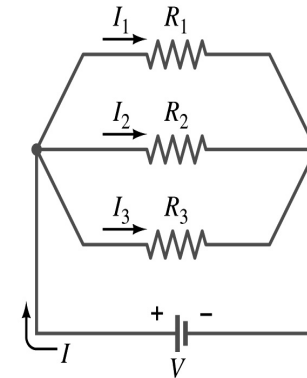
(b) The terminal voltage V_{ab} is $V_{ab} = \varepsilon - Ir = 12.0\text{V} - 0.183\text{A} \cdot 0.5\Omega = 11.9\text{V}$

(c) The power dissipated in R and r are $P = I^2 R = (0.183\text{A})^2 \cdot 65.0\Omega = 2.18\text{W}$

$$P = I^2 r = (0.183\text{A})^2 \cdot 0.5\Omega = 0.02\text{W}$$

Resisters in Parallel

- Resisters are in parallel when two or more resisters are connected in separate branches
 - Most the house and building wirings are arranged this way.
- What is the same in a circuit connected in parallel?
 - The voltage is the same across all the resisters.
 - The total current that leaves the battery, is however, split through the branches.
- The current that passes through every element is
 - $I_1 = V/R_1$, $I_2 = V/R_2$, $I_3 = V/R_3$
- Since the total current is I , we obtain
 - $I = V/R_{eq} = I_1 + I_2 + I_3 = V(1/R_1 + 1/R_2 + 1/R_3)$
 - Thus, $1/R_{eq} = 1/R_1 + 1/R_2 + 1/R_3$



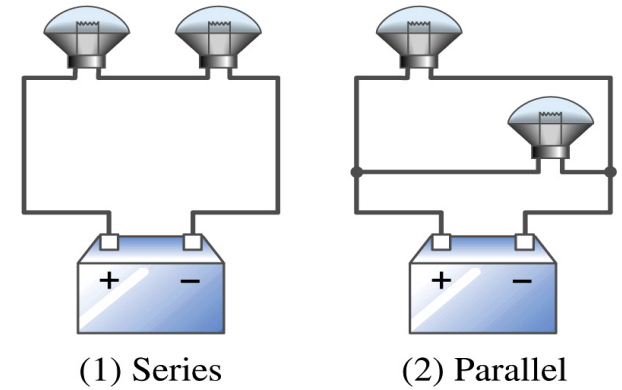
$$\frac{1}{R_{eq}} = \sum_i \frac{1}{R_i}$$

Resisters
in parallel

When resisters are connected in parallel, the total resistance decreases and the current increases.

Example 19 – 2

Series or parallel? (a) The light bulbs in the figure are identical and have identical resistance R . Which configuration produces more light? (b) Which way do you think the headlights of a car are wired?



(a) What are the equivalent resistances for the two cases?

Series $\Rightarrow R_{eq} = 2R$

Parallel $\Rightarrow \frac{1}{R_{eq}} = \frac{2}{R}$

So $\Rightarrow R_{eq} = \frac{R}{2}$

The bulbs get brighter when the total power transformed is larger.

series $P_S = IV = \frac{V^2}{R_{eq}} = \frac{V^2}{2R}$

parallel $P_P = IV = \frac{V^2}{R_{eq}} = \frac{2V^2}{R} = 4P_S$

So parallel circuit provides brighter lighting.

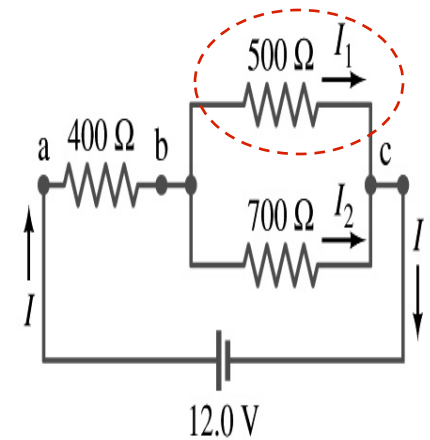
(b) Car's headlights are in parallel to provide brighter lighting and also to prevent both lights going out at the same time when one burns out.

So what is bad about parallel circuits? Uses more energy in a given time.

Example 19 – 5

Current in one branch. What is the current flowing through the 500- Ω resistor in the figure?

What do we need to find first? We need to find the total current.



To do that we need to compute the equivalent resistance.

R_{eq} of the small parallel branch is: $\frac{1}{R_P} = \frac{1}{500} + \frac{1}{700} = \frac{12}{3500}$ $R_P = \frac{3500}{12}$

R_{eq} of the circuit is: $R_{eq} = 400 + \frac{3500}{12} = 400 + 292 = 692\Omega$

Thus the total current in the circuit is $I = \frac{V}{R_{eq}} = \frac{12}{692} = 17mA$

The voltage drop across the parallel branch is $V_{bc} = IR_P = 17 \times 10^{-3} \cdot 292 = 4.96V$

The current flowing across 500- Ω resistor is therefore

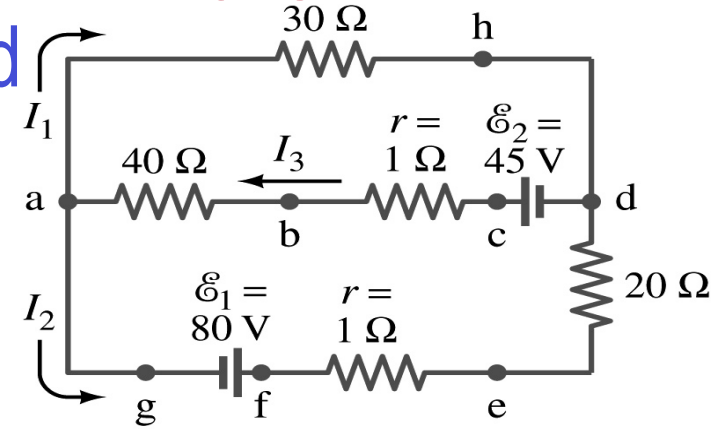
$$I_{500} = \frac{V_{bc}}{R} = \frac{4.96}{500} = 9.92 \times 10^{-3} = 9.92mA$$

What is the current flowing thru 700- Ω resistor?

$$I_{700} = I - I_{500} = 17 - 9.92 = 7.08mA$$

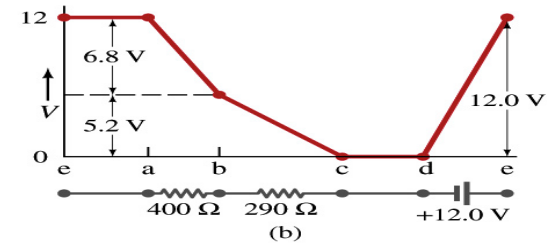
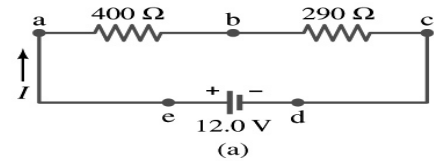
Kirchhoff's Rules – 1st Rule

- Some circuits are very complicated to analyze using the simple combinations of resistors
 - G. R. Kirchhoff devised two rules to deal with complicated circuits.
- Kirchhoff's rules are based on conservation of charge and energy
 - Kirchhoff's 1st rule: Junction rule, charge conservation.
 - At any junction point, the sum of all currents entering the junction must equal to the sum of all currents leaving the junction.
 - In other words, what goes in must come out.
 - At junction a in the figure, I_3 comes into the junction while I_1 and I_2 leaves: $I_3 = I_1 + I_2$



Kirchhoff's Rules – 2nd Rule

- Kirchoff's 2nd rule: Loop rule, uses conservation of energy.
 - The sum of the changes in potential around any closed path of a circuit must be zero.



- The current in the circuit in the figure is $I=12/690=0.017\text{A}$.
 - Point e is the highest potential point while point d is the lowest potential.
 - When the test charge starts at e and returns to e , the total potential change is 0.
 - Between point e and a , no potential change since there is no source of potential or any resistance.
 - Between a and b , there is a 400Ω resistance, causing $IR=0.017*400=6.8\text{V}$ drop.
 - Between b and c , there is a 290Ω resistance, causing $IR=0.017*290=5.2\text{V}$ drop.
 - Since these are voltage drops, we use negative sign for these, -6.8V and -5.2V .
 - No change between c and d while from d to e there is $+12\text{V}$ change.
 - Thus the total change of the voltage through the loop is: $-6.8\text{V}-5.2\text{V}+12\text{V}=0\text{V}$.

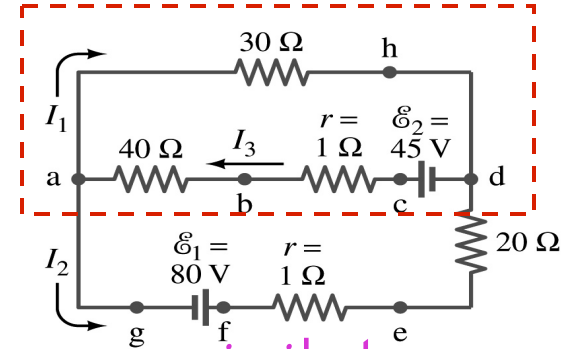
Using Kirchhoff's Rules

1. Determine the flow of currents at the junctions.
 - It does not matter which direction of the current you choose.
 - If the value of the current after completing the calculations are negative, you just flip the direction of the current flow.
2. Write down the current equation based on Kirchhoff's 1st rule at various junctions.
 - Be sure to see if any of them are the same.
3. Choose independent closed loops in the circuit
4. Write down the potential in each interval of the junctions, keeping the signs properly.
5. Write down the potential equations for each loop.
6. Solve the equations for unknowns.



Example 19 – 8

Using Kirchhoff's rules. Calculate the currents I_1 , I_2 and I_3 in each of the branches of the circuit in the figure.



The directions of the current through the circuit is not known *a priori* but since the current tends to move away from the positive terminal of a battery, we arbitrarily choose the direction of the currents as shown.

We have three unknowns so we need three equations.

Using Kirchhoff's junction rule at point a , we obtain $I_3 = I_1 + I_2$

This is the same for junction d as well, so no additional information.

Now the second rule on the loop $ahdcba$.

$$V_{ah} = -I_1 30 \quad V_{hd} = 0 \quad V_{dc} = +45 \quad V_{cb} = -I_3 \cdot 1 \quad V_{ba} = -40I_3$$

The total voltage change in loop $ahdcba$ is.

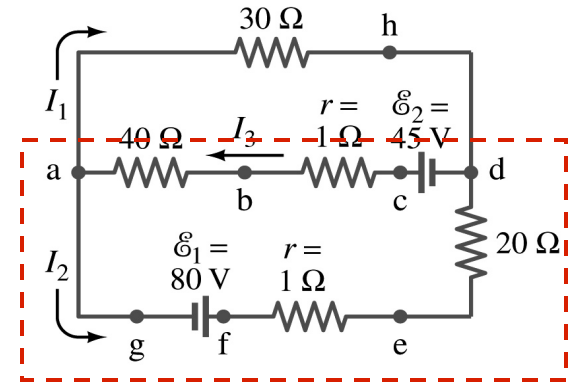
$$V_{ahdcba} = -30I_1 + 45 - I_3 - 40I_3 = 45 - 30I_1 - 41I_3 = 0$$

Example 19 – 8, cnt'd

Now the second rule on the other loop *agfedcba*.

$$V_{ag} = 0 \quad V_{gf} = +80 \quad V_{fe} = -I_2 \cdot 1 \quad V_{ed} = -I_2 20$$

$$V_{dc} = +45 \quad V_{cb} = -I_3 \cdot 1 \quad V_{ba} = -40I_3$$



The total voltage change in loop *agfedcba* is. $V_{agfedcba} = -21I_2 + 125 - 41I_3 = 0$

So the three equations become $I_3 = I_1 + I_2$

$$45 - 30I_1 - 41I_3 = 0$$

$$125 - 21I_2 - 41I_3 = 0$$

We can obtain the three current by solving these equations for I_1 , I_2 and I_3 .