

PHYS 1441 – Section 001

Lecture #10

Monday, June 29, 2015

*Dr. **Jaehoon** **Yu***

- Centripetal Acceleration
- Unbanked and Banked highways
- Newton's Law of Universal Gravitation
- Work and Energy



Announcements

- Reading Assignments: CH5.4 and 5.9
- Quiz 3
 - Beginning of the class tomorrow, Tuesday, June 30
 - Covers CH4.6 through what we finish today
 - Bring your calculator but DO NOT input formula into it!
 - Your phones or portable computers are NOT allowed as a replacement!
 - You can prepare a one 8.5x11.5 sheet (front and back) of handwritten formulae and values of constants for the exam → no solutions, derivations, word definitions or key methods for solutions
 - No additional formulae or values of constants will be provided!
- Term exam #2
 - In class this Thursday, July 2
 - Non-comprehensive exam
 - Covers CH 4.6 to what we finish this Wednesday, July 1
 - BYOF



Reminder: Special Project #3

- Using the fact that $g=9.80\text{m/s}^2$ on the Earth's surface, find the average density of the Earth.
 - Use ONLY the following information but without computing the value of the volume explicitly
 - The gravitational constant $G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$
 - The radius of the Earth $R_E = 6.37 \times 10^3 \text{ km}$
- 20 point extra credit
- Due: Tomorrow, Tuesday, June 30
- You must show your OWN, detailed work to obtain any credit!!

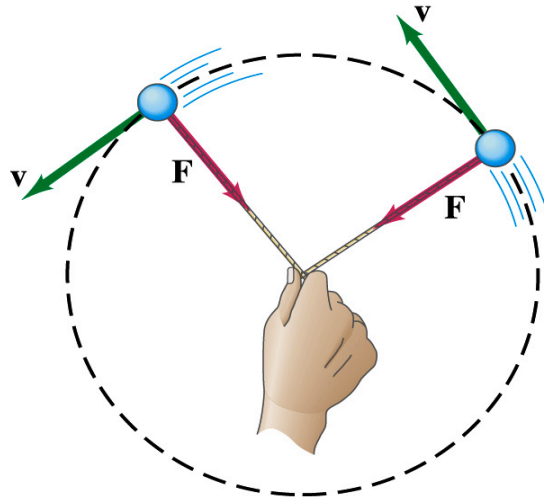


Special Project #4

1. Compute the gravitational force between two protons separated by 1m. (10 points)
 2. Compute the electric force between the two protons separated by 1m. (10 points)
 3. Express the electric force in #2 above in terms of the gravitational force in #1. (5 points)
- You must look up the mass of the proton, the electrical charge of the proton in coulombs, electrical force constant, electric force formula, etc, and clearly write them on your project report
 - You MUST have your own, independent answers to the above three questions even if you worked together with others. All those who share the answers will get 0 credit if copied.
 - Due for the submission is Monday, July 6!



Newton's Second Law & Centripetal Force



The centripetal ^{*} acceleration is always perpendicular to the velocity vector, \mathbf{v} , and points to the center of the axis (radial direction) in a uniform circular motion.

$$a_c = \frac{v^2}{r}$$

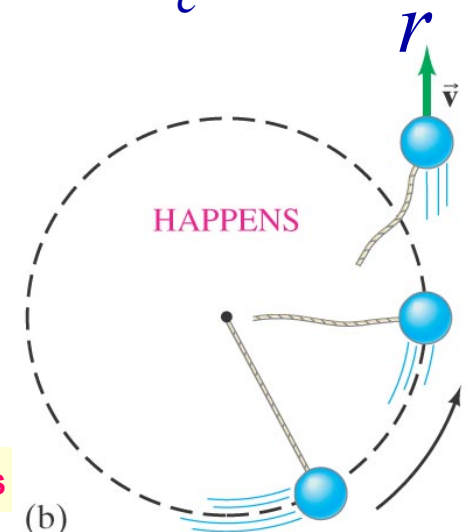
Are there forces in this motion? If so, what do they do?

The force that causes the centripetal acceleration acts toward the center of the circular path and causes the change in the direction of the velocity vector. This force is called the **centripetal force**.

What do you think will happen to the ball if the string that holds the ball breaks?

The external force no longer exist. Therefore, based on Newton's 1st law, the ball will continue its motion without changing its velocity and will fly away following the tangential direction to the circle.

$$\sum F_c = ma_c = m \frac{v^2}{r}$$



^{*}Miriam Webster: Proceeding or acting in the direction toward the center or axis
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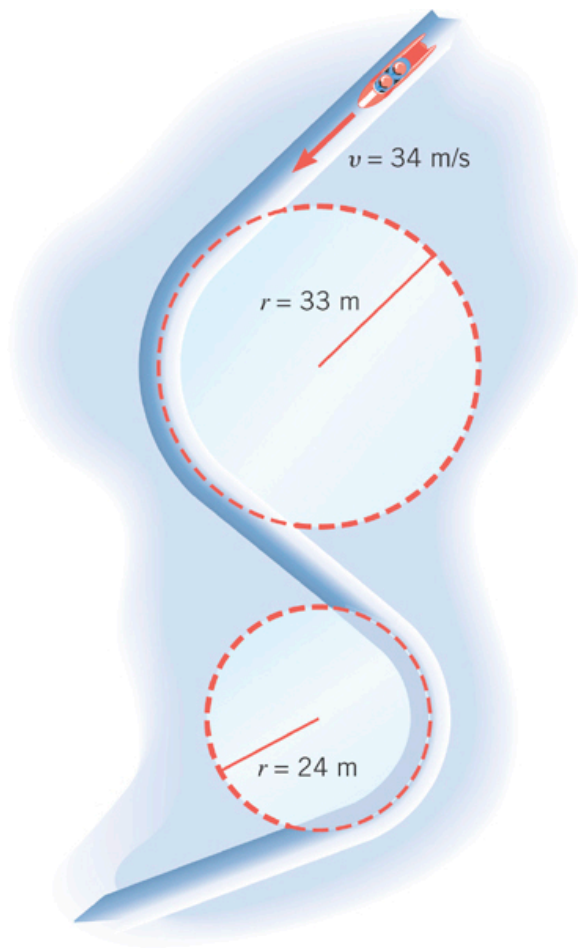


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(b)
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Ex. Effect of Radius on Centripetal Acceleration

The bobsled track at the 1994 Olympics in Lillehammer, Norway, contain turns with radii of 33m and 23m. Find the centripetal acceleration at each turn for a speed of 34m/s, a speed that was achieved in the two-man event. Express answers as multiples of $g=9.8\text{m/s}^2$.



Centripetal acceleration:

$$a_r = \frac{v^2}{r}$$

$$R=33\text{m}$$

$$a_{r=33\text{m}} = \frac{(34)^2}{33} = 35\text{ m/s}^2 = 3.6g$$

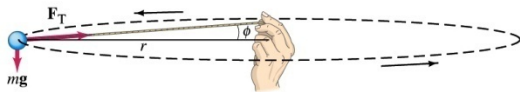
$$R=24\text{m}$$

$$a_{r=24\text{m}} = \frac{(34)^2}{24} = 48\text{ m/s}^2 = 4.9g$$



Example 5.3: Uniform Circular Motion

A ball of mass 0.500kg is attached to the end of a 1.50m long cord. The ball is moving in a horizontal circle. If the string can withstand maximum tension of 50.0 N, what is the maximum speed the ball can attain before the cord breaks?



*Centripetal
acceleration:*

$$a_r = \frac{v^2}{r}$$

*When does the
string break?*

$$\sum F_r = ma_r = m \frac{v^2}{r} > T$$

when the required centripetal force is greater than the sustainable tension.

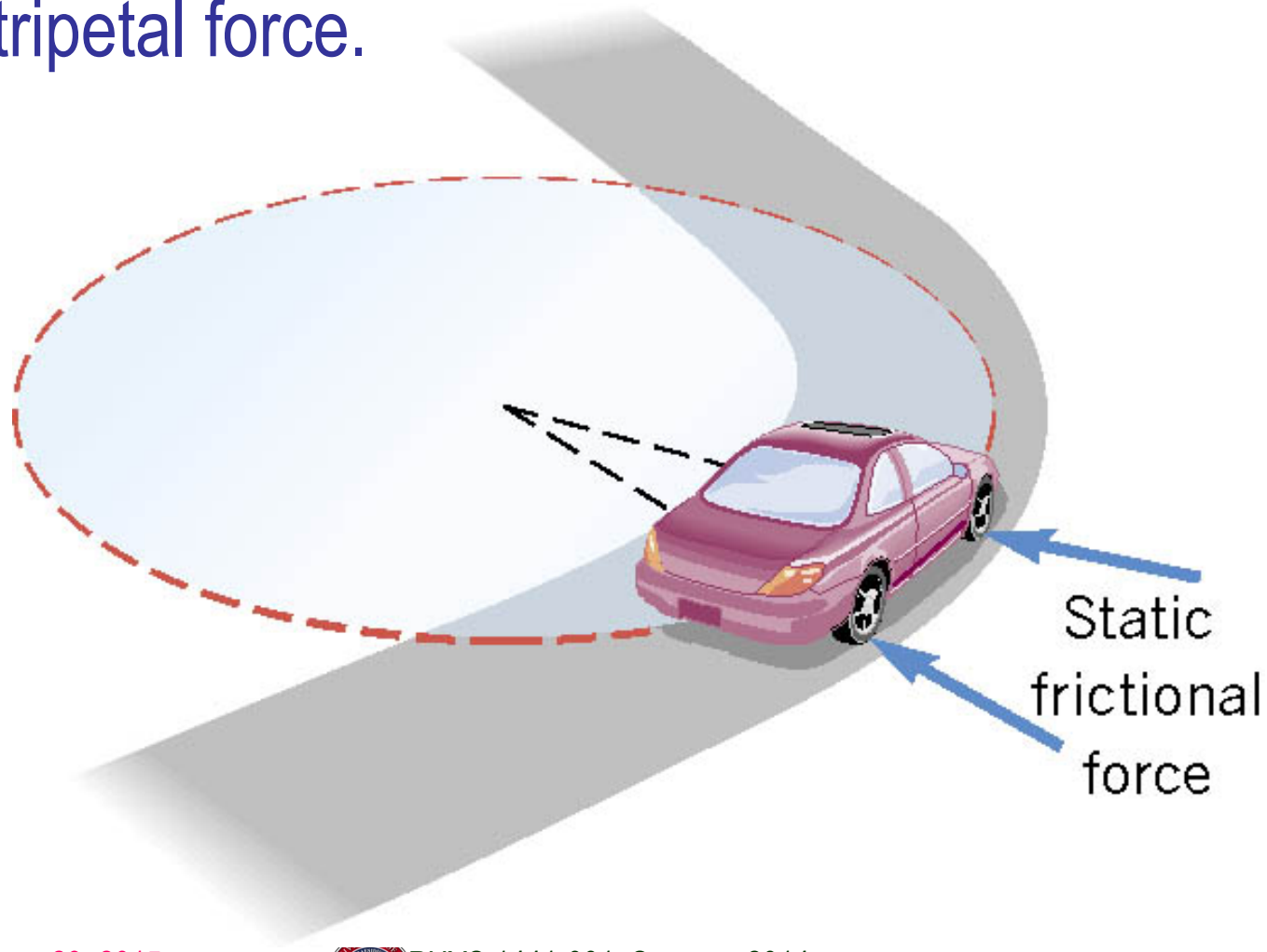
$$m \frac{v^2}{r} = T \quad v = \sqrt{\frac{Tr}{m}} = \sqrt{\frac{50.0 \times 1.5}{0.500}} = 12.2 (m/s)$$

Calculate the tension of the cord when speed of the ball is 5.00m/s.

$$T = m \frac{v^2}{r} = 0.500 \times \frac{(5.00)^2}{1.5} = 8.33 (N)$$

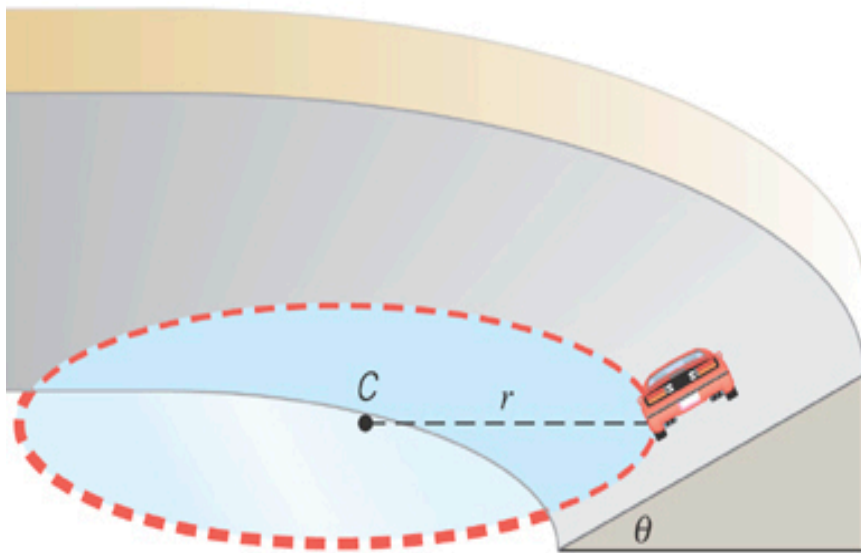
Unbanked Curve and Centripetal Force

On an unbanked curve, the static frictional force provides the centripetal force.

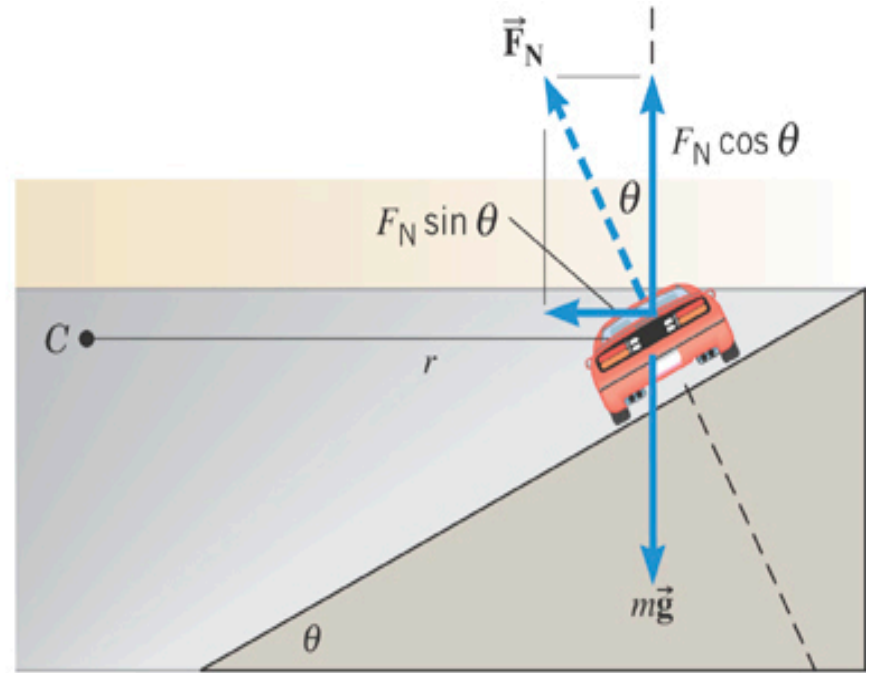


Banked Curves

On a frictionless banked curve, the centripetal force is the horizontal component of the normal force. The vertical component of the normal force balances the car's weight.



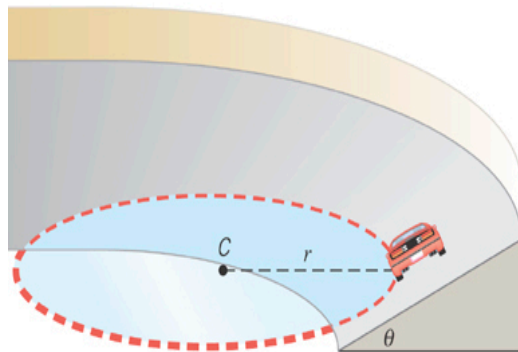
(a)



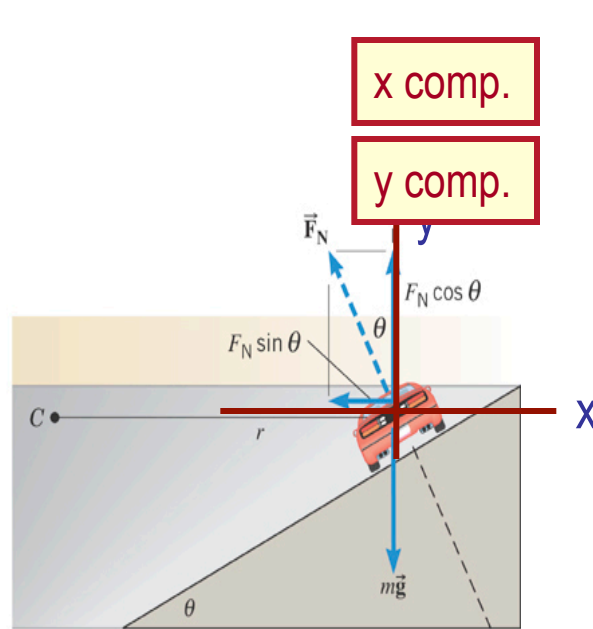
(b)

Ex. The Daytona 500

The Daytona 500 is the major event of the NASCAR season. It is held at the Daytona International Speedway in Daytona, Florida. The turns in this oval track have a maximum radius (at the top) of $r=316\text{m}$ and are banked steeply, with $\theta=31^\circ$. Suppose these maximum radius turns were frictionless. At what speed would the cars have to travel around them?



(a)



(b)

x comp.

$$\sum F_x = F_N \sin \theta - m \frac{v^2}{r} = 0$$

y comp.

$$\sum F_y = F_N \cos \theta - mg = 0$$

$$\tan \theta = \frac{mv^2}{mgr} = \frac{v^2}{gr}$$

$$v^2 = gr \tan \theta$$

$$v = \sqrt{gr \tan \theta} =$$

$$\sqrt{9.8 \cdot 316 \tan (31^\circ)} = 43 \text{ m/s} = 96 \text{ mi/hr}$$

Newton's Law of Universal Gravitation

People have been very curious about the stars in the sky, making observations for a long~ time. The data people collected, however, have not been explained until Newton has discovered the law of gravitation.

Every object in the Universe attracts every other object with a force that is directly proportional to the product of their masses and inversely proportional to the square of the distance between them.

How would you write this law mathematically?

$$F_g \propto \frac{m_1 m_2}{r_{12}^2}$$

With G

$$F_g = G \frac{m_1 m_2}{r_{12}^2}$$

G is the universal gravitational constant, and its value is

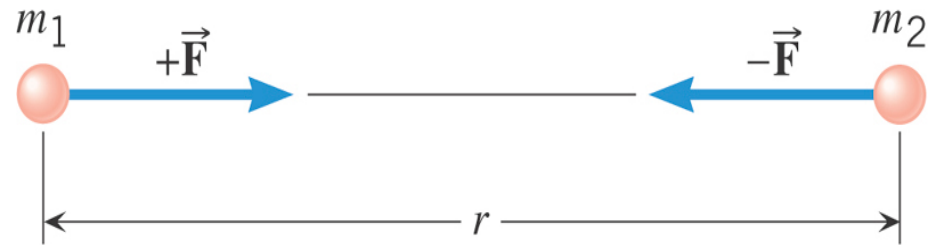
$$G = 6.673 \times 10^{-11} \text{ Unit? } N \cdot m^2 / kg^2$$

This constant is not given by the theory but must be measured by experiments.

This form of forces is known as the inverse-square law, because the magnitude of the force is inversely proportional to the square of the distance between the objects.

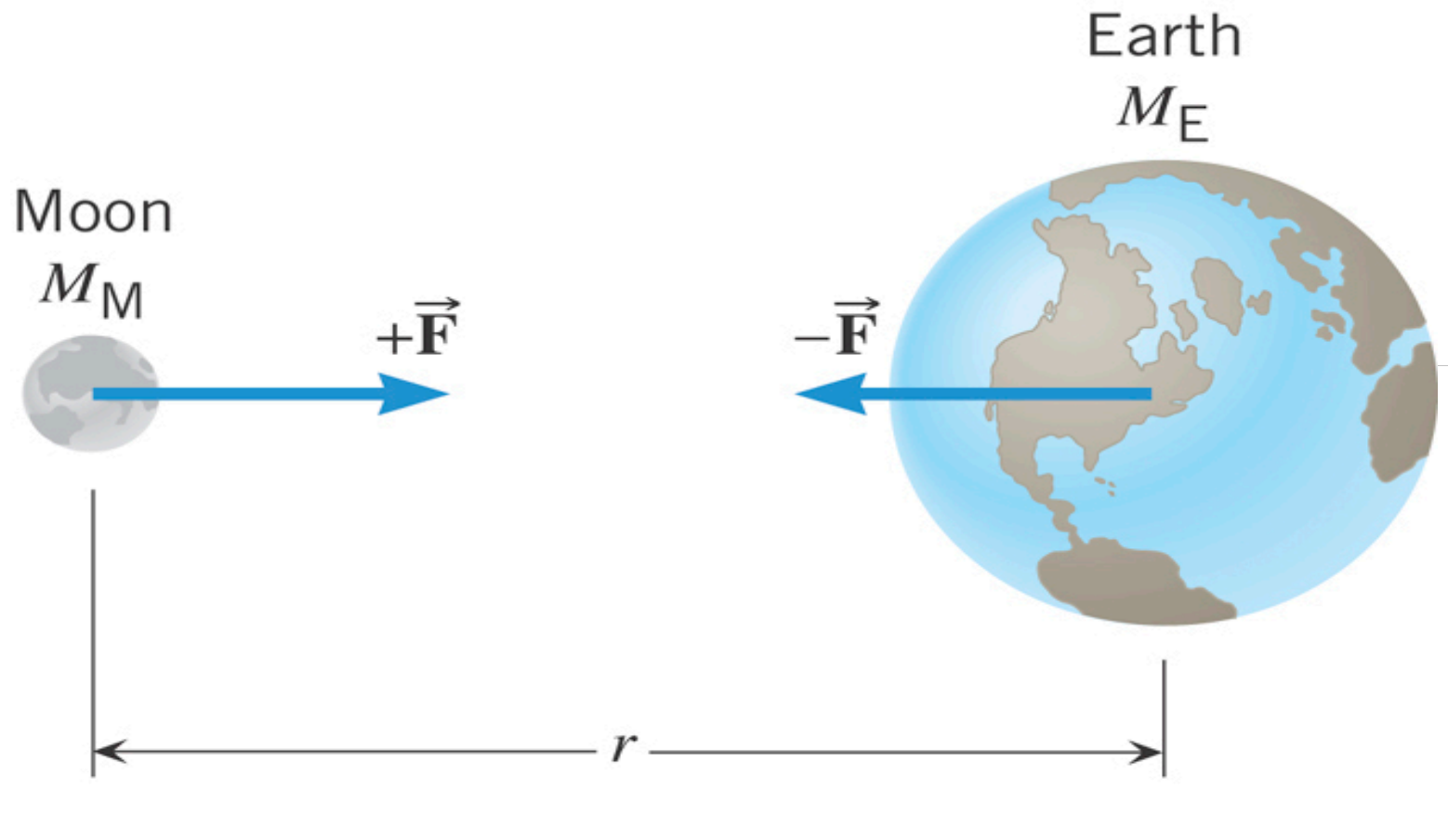
Ex. Gravitational Attraction

What is the magnitude of the gravitational force that acts on each particle in the figure, assuming $m_1=12\text{kg}$, $m_2=25\text{kg}$, and $r=1.2\text{m}$?



$$\begin{aligned} F &= G \frac{m_1 m_2}{r^2} \\ &= \left(6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2 \right) \frac{(12 \text{ kg})(25 \text{ kg})}{(1.2 \text{ m})^2} \\ &= 1.4 \times 10^{-8} \text{ N} \end{aligned}$$

Why does the Moon orbit the Earth?



Gravitational Force and Weight

Gravitational Force, \vec{F}_g

The attractive force exerted on an object by the Earth

$$\vec{F}_G = m\vec{a} = m\vec{g}$$

Weight of an object with mass M is

$$W = \left| \vec{F}_G \right| = M \left| \vec{g} \right| = Mg$$

What is the SI unit of weight?

N

Since weight depends on the magnitude of gravitational acceleration, g , it varies depending on geographical location.

By measuring the forces one can determine masses. This is why you can measure mass using the spring scale.

Gravitational Acceleration

$$W = G \frac{M_E m}{r^2}$$

$$W = mg$$

$$\cancel{m}g = G \frac{M_E \cancel{m}}{r^2}$$

$$g = G \frac{M_E}{r^2}$$

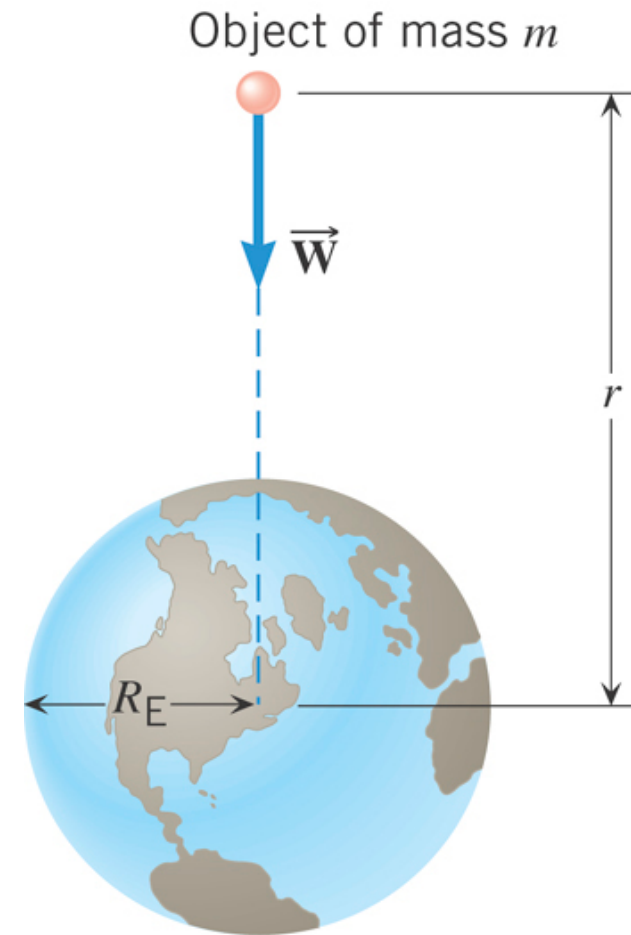
Gravitational acceleration at distance r from the center of the earth!

What is the SI unit of g ? m/s^2

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Mass of earth = M_E

Magnitude of the gravitational acceleration on the surface of the Earth

Gravitational force on
the surface of the earth:

$$F_G = G \frac{M_E m}{r^2} = G \frac{M_E \cancel{m}}{R_E^2} \\ = \cancel{m} g$$

$$g = G \frac{M_E}{R_E^2}$$

$$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$$

$$M_E = 5.98 \times 10^{24} \text{ kg}; \quad R_E = 6.38 \times 10^6 \text{ m}$$

$$= \left(6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2 \right) \frac{\left(5.98 \times 10^{24} \text{ kg} \right)}{\left(6.38 \times 10^6 \text{ m} \right)^2} \\ = 9.80 \text{ m/s}^2$$

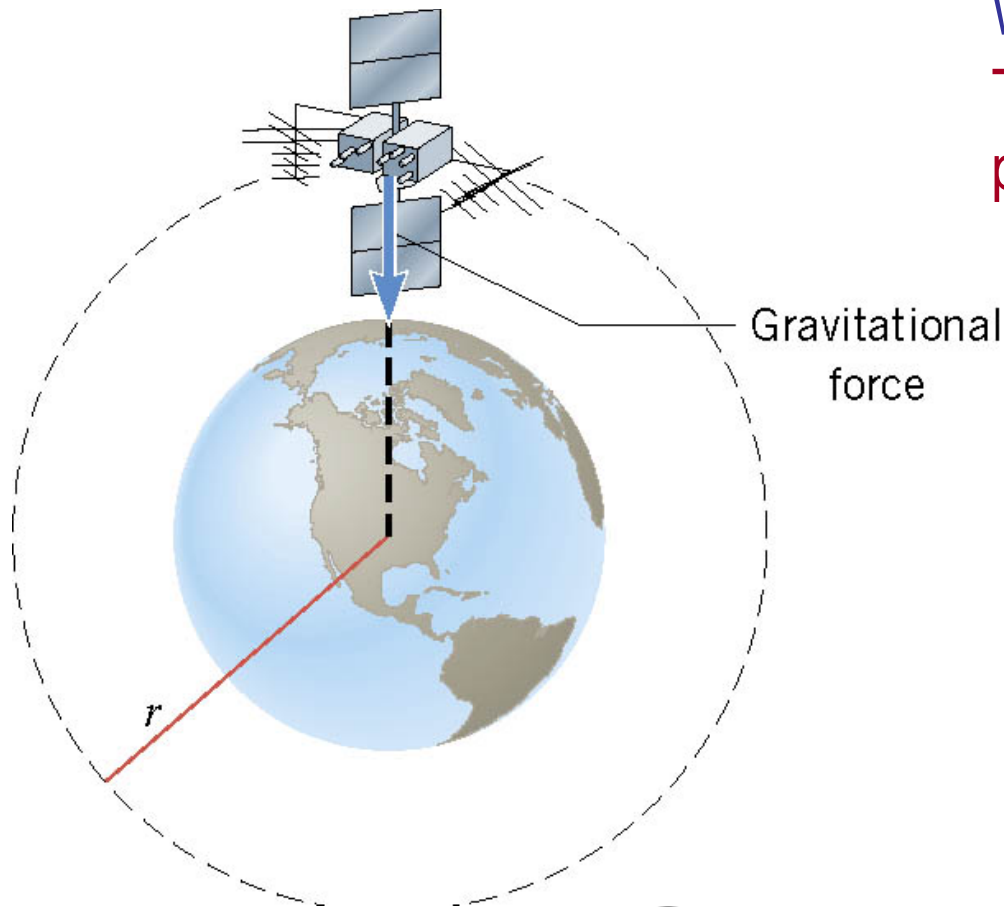


Satellite in Circular Orbits

There is only one speed that a satellite can have if the satellite is to remain in an orbit with a fixed radius.

What acts as the centripetal force?

The gravitational force of the earth pulling the satellite!



$$F_c = G \frac{mM_E}{r^2} = m \frac{v^2}{r}$$

$$v^2 = \frac{GM_E}{r}$$

$$v = \sqrt{\frac{GM_E}{r}}$$

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Ex. Orbital Speed of the Hubble Space Telescope

Determine the speed of the Hubble Space Telescope orbiting at a height of 598 km above the earth's surface.

$$\begin{aligned} v &= \sqrt{\frac{GM_E}{r}} \\ &= \sqrt{\frac{(6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2)(5.98 \times 10^{24} \text{ kg})}{6.38 \times 10^6 \text{ m} + 598 \times 10^3 \text{ m}}} \\ &= 7.56 \times 10^3 \text{ m/s} \quad (16900 \text{ mi/h}) \end{aligned}$$

