### PHYS 1441 – Section 001 Lecture #16 Thursday, July 2, 2020 Dr. Jaehoon Yu

CH 28: Sources of Magnetic Field

- Sources of Magnetic Field
- Magnetic Field Due to Straight Wire
- Magnetic Materials
- Hysteresis

Chapter 29:EM Induction & Faraday's Law

Induced EMF and EM Induction



### Announcements

- Reading Assignments: CH27.6 8 and CH28.6 10
- Course feedback survey
  - Let's take 10 min to fill the survey now
- Special seminar on COVID–19 Monday, July 6
  - Dr. Linda Lee, a frontline doctor
  - The second hour of the class (11:30 12:30)
    - Extra credit for attending the seminar
  - Questions will earn additional extra credit points
- Term 2 results
  - − Class average: 67/102 → Equivalent to: 65.6/100
    - Previous results: 63.6/100 and 54.2/100
  - Top score: 102/102



### Reminder: Special Project #5 – COVID-19

- Make comparisons of COVID-19 statistics between the U.S., South Korea, Italy and Texas from <u>https://coronaboard.com</u> on spreadsheet
  - Total 36 points: 1 point for each of the top 20 cells and 2 points for each of the 8 cells for testing
- What are the 3 fundamental requirements for opening up (2 points each, total 6 points)?
  - Must be quantitative! (e.g. how many tests per capita per day for the present situation of pandemic)
- Assess the readiness of the three fundamental requirements U.S. (2 point each, total 6 points; do NOT just take politician's words!). Must provide the independent scientific entity's reference you took the information from.
- Evaluate quantitatively the success/failure of the US responses to COVID-19 in 5 sentences. <u>Must provide quantitative reasons behind your conclusion!</u> (10 points)
- Assess quantitatively the effectiveness of wearing masks (4 points) and at least 4 reasons for it being effective (1 point each, 0.5 point extra after the first 4).
- Due: the beginning of the class Tuesday, July 7
  - Scan all pages of your special project into the pdf format, including the spreadsheet
  - Save all pages into **one file** with the filename SP5-YourLastName-YourFirstName.pdf
- Spreadsheet has been posted on the class web page. Download ASAP.



### SP5 spreadsheet

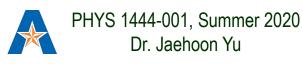
#### PHYS1442-001, Summer 20, Special Project #5, COVID-19

Name:			Date & time of your COVID-19 Data:		
Items		U.S.A	South Korea	Italy	Texas
Total Population					
COVID-19 Confirmed cases	Total				
	Cases per 1M people				
COVID-19 Deaths	Total				
	Death per 1M people				
COVID-19 Testing to date	Total				
	Per 1M people				



# Sources of Magnetic Field

- We have learned so far about the effects of magnetic field on the electric current and the moving charge
- We will now learn about the dynamics of magnetism
  - How do we determine magnetic field strengths in certain situations?
  - How do two wires with electric current interact?
  - What is the general approach to finding the connection between current and magnetic field?



# Magnetic Field due to a Straight Wire

- The magnetic field due to the current flowing through a straight wire forms a circular pattern around the wire
  - What do you imagine the strength of the field is as a function of the distance from the wire? (poll 11)
    - It must be weaker as the distance increases
  - How about as a function of current? (poll 11)
    - Directly proportional to the current
  - Indeed, the above are experimentally verified  $B \propto \frac{I}{-}$ 
    - This is valid as long as r << the length of the wire
  - The proportionality constant is  $\mu_0/2\pi$ , thus the field strength becomes  $\mu_0 I$

$$B = \frac{\mu_0 I}{2\pi r}$$

-  $\mu_0$  is the permeability of free space  $\mu_0 = 4\pi \times 10^{-7} T \cdot m/A$ 



### Example 28 – 1

**Calculation of B near a wire.** A vertical electric wire in the wall of a building carries a DC current of 25A upward. What is the magnetic field at a point 10cm due East of this wire?

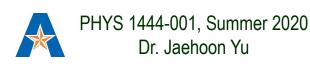
Using the formula for the magnetic field near a straight wire

$$B = \frac{\mu_0 I}{2\pi r}$$

So we can obtain the magnetic field at 10cm away as

$$B = \frac{\mu_0 I}{2\pi r} = \frac{\left(4\pi \times 10^{-7} \ T \cdot m/A\right) \cdot \left(25A\right)}{\left(2\pi\right) \cdot \left(0.01m\right)} = 5.0 \times 10^{-5} \ T$$

Thursday, July 2, 2020



 $10 \text{ cm} \rightarrow$ 

# Force Between Two Parallel Wires

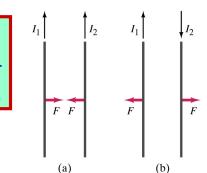
- We have learned that a wire carrying the electric current produces magnetic field
- Now what do you think will happen if we place two current carrying wires next to each other?
  - They will exert force onto each other. Repel or attract?
  - Depending on the direction of the currents
- This was first pointed out by Ampére.
- Let's consider two long parallel conductors separated by a distance d, carrying currents I<sub>1</sub> and I<sub>2</sub>.
- At the location of the second conductor, the magnitude of the magnetic field produced by  $I_1$  is  $R = \frac{\mu_0 I_1}{R}$



### Force Between Two Parallel Wires

- The force F by a magnetic field  $B_1$  on a wire of length l, carrying the current  $I_2$  when the field and the current are perpendicular to each other is:  $F = I_2 B_1 l$ 
  - So the force per unit length is  $\frac{F}{l} = I_2 B_1 = I_2 \frac{\mu_0}{2\pi} \frac{I_1}{d}$
  - This force is only due to the magnetic field generated by the wire carrying the current  $I_1$ 
    - There is the force exerted on the wire carrying the current  $I_1$ by the wire carrying current  $I_2$  of the same magnitude but in opposite direction (poll 13)
- So the force per unit length is

$$\frac{F}{l} = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{d}$$



How about the direction of the force?

If the currents are in the same direction, the attractive force. If opposite, repulsive.

#### Example 28 – 5 Suspending a wire with current. A horizontal wire carries

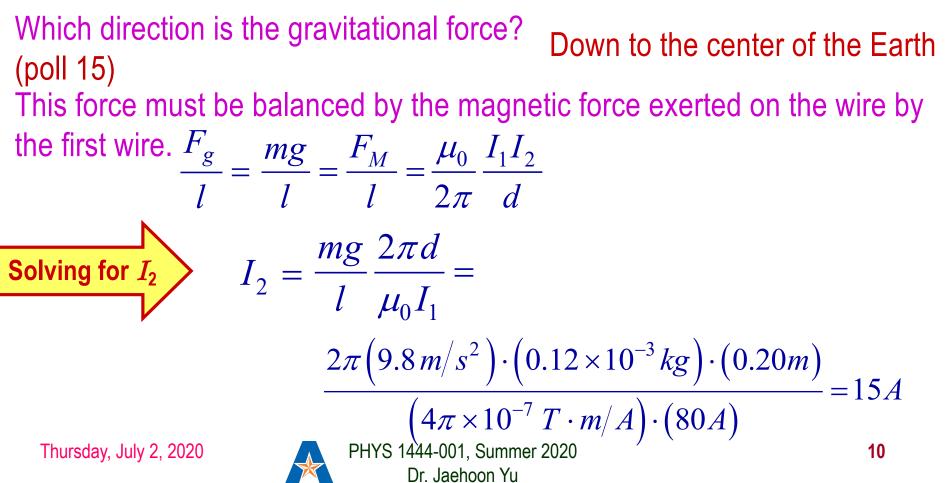
 $I_1 = 80 \text{A}$ 

 $I_2 = ?$ 

**F**<sub>B</sub>

mg

Suspending a wire with current. A horizontal wire carries a current  $I_1$ =80A DC. A second parallel wire 20cm below it must carry how much current  $I_2$  so that it doesn't fall due to the gravity? The lower has a mass of 0.12g per meter of length.



### **Operational Definition of Units: Ampere and Coulomb**

- The permeability of free space is defined to be exactly  $\mu_0 = 4\pi \times 10^{-7} \ T \cdot m/A$
- The unit of the current, ampere, is defined using the definition of the force between two wires each carrying 1A of current and separated by 1m

$$\frac{F}{l} = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{d} = \frac{4\pi \times 10^{-7} \ T \cdot m/A}{2\pi} \frac{1A \cdot 1A}{1m} = 2 \times 10^{-7} \ N/m$$

 So 1A is defined as: the current flowing each of two long parallel conductors 1m apart, which results in a force of exactly 2x10<sup>-7</sup>N/m.

- Coulomb is then defined as exactly 1C=1A s.
- We do it this way since the electric current can be measured more accurately and controlled more easily than the charge.

Thursday, July 2, 2020



# Ampére's Law

- What is the relationship between the magnetic field strength and the current?  $B = \frac{\mu_0 I}{2\pi r}$ 
  - Does this work in all cases?
    - Nope!
    - OK, then when?
    - Only valid for a long straight wire
- Then what would be the more generalized relationship between the current and the magnetic field for any shapes of the wire?
  - French scientist André Marie Ampére proposed such a relationship soon after Oersted's discovery



# Ampére's Law

- Let's consider an arbitrary closed path around the current as shown in the figure.
  - Let's split this path in small segments each of  $\Delta l$  long.
  - The sum of all the products of the length of each segment and the component of B parallel to that segment is equal to  $\mu_0$  times the net current  $I_{encl}$  that passes through the surface enclosed by the path

$$-\sum B_{||}\Delta l = \mu_0 I_{encl}$$

- In the limit  $\Delta \ell \rightarrow 0$ , this relation becomes

$$-\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{encl}$$



Thursday, July 2, 2020



Looks very similar to a law in the

electricity. Which law is it? (Poll13)

Area enclosed

by the path

# Verification of Ampére's Law

Ι

- Let's find the magnitude of B at a distance r away from a long straight wire w/ current *I* 
  - This is a verification of Ampere's Law
  - We can apply Ampere's law to a circular path of radius *r*.

$$\mu_0 I_{encl} = \oint \vec{B} \cdot d\vec{l} = \oint B \, dl = B \oint dl = 2\pi r B$$
  
Solving for  $\vec{B}$   $\vec{B} = \frac{\mu_0 I_{encl}}{2\pi r} = \frac{\mu_0}{2\pi} \frac{I}{r}$ 

- We just verified that Ampere's law works in a simple case
- Experiments verified that it works for other cases too
- The importance of this formula, however, is that it provides means to relate magnetic field to current

# Verification of Ampére's Law

- Since Ampere's law is valid in general, B in Ampere's law is not just due to the current  $I_{encl}$ .
- B is the field at each point in space along the chosen path due to all sources
  - Including the current *I* enclosed by the path but also due to any other sources
  - How do you obtain B in the figure at any point?
    - Vector sum of the field by the two currents
  - The result of the closed path integral in Ampere's law for green dashed path is still  $\mu_0 I_1$ . Why?
  - While B in each point along the path varies, the integral over the closed path still comes out the same whether there is the second wire or not.



## Example 28 – 6

**Field inside and outside a wire.** A long straight cylindrical wire conductor of radius R carries current *I* of uniform density in the conductor. Determine the magnetic field at (a) points outside the conductor (r>R) and (b) points inside the conductor (r<R). Assume that r, the radial distance from the axis, is much less than the length of the wire. (c) If R=2.0mm and *I*=60A, what is B

B r R

#### at r=1.0mm, r=2.0mm and r=3.0mm?

Since the wire is long, straight and symmetric, the field should be the same at any point the same distance from the center of the wire.

Since B must be tangential to circles around the wire, let's choose a circular path of the closed-path integral outside the wire (r>R). What is  $I_{encl}$ ?  $I_{encl} = I$ 

So using Ampere's law

$$\mu_0 I = \oint \vec{B} \cdot d\vec{l} = 2\pi r B$$
Solving for B
$$B = \frac{\mu_0}{2\pi} \frac{I}{r}$$
Thursday, July 2, 2020
PHYS 1444-001, Summer 2020
Dr. Jaehoon Yu

### Example 28 – 6 conť d

For r<R, the current inside the closed path is less than *I*. How much is it?  $2 - \sqrt{2}$ 

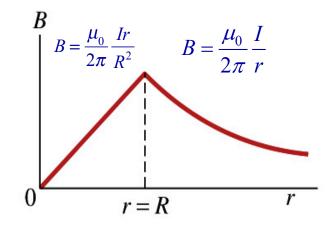
$$I_{encl} = I \frac{\pi r^2}{\pi R^2} = I \left(\frac{r}{R}\right)$$

So using Ampere's law

$$\mu_0 I\left(\frac{r}{R}\right)^2 = \oint \vec{B} \cdot d\vec{l} = 2\pi r B \quad \text{Solving for B} \quad B = \frac{\mu_0}{2\pi} \frac{I}{r} \left(\frac{r}{R}\right)^2 = \frac{\mu_0}{2\pi} \frac{Ir}{R^2}$$

What does this mean?

The field is 0 at r=0 and increases linearly as a function of the distance from the center of the wire up to r=R then decreases as 1/r beyond the radius of the conductor.



# Example 28 – 7

**Coaxial cable.** A coaxial cable is a single wire surrounded by a cylindrical metallic braid, as shown in the figure. The two conductors are separated by an insulator. The central wire carries current to the other end of the cable, and the outer braid carries the return current and is usually considered ground. Describe the magnetic field (a) in the space between the conductors and (b) outside the cable.

Insulating sleeve *I Cylindrical braid Solid wire* 

(a) The magnetic field between the conductors is the same as the long, straight wire case since the current in the outer  $B = \frac{\mu_0}{2\pi} \frac{I}{r}$  conductor does not impact the enclosed current.

(b) Outside the cable, we can draw a similar circular path, since we expect the field to have a circular symmetry. What is the sum of the total current inside the closed path?  $I_{encl} = I - I = 0$ . So there is no magnetic field outside a coaxial cable. In other words, the coaxial cable self-shields. The outer conductor also shields against an external electric field. Cleaner signal and less noise.

Thursday, July 2, 2020



PHYS 1444-001, Summer 2020 Dr. Jaehoon Yu