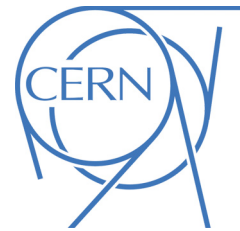




# ATLAS NOTE

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## 1 Electron Identification Studies for the Level 1 Trigger Upgrade

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### 5 Abstract

6 This note shows that it is very difficult to reject neutral pions from electrons at  
7 Level 1 trigger of the ATLAS trigger system. The lateral profiles of electrons and  
8 neutral pions are different when the interaction point of the colliding protons is at  
9  $z = 0$  and a good rejection criteria is achieved. Although this rejection criteria is  
10 stable against increasing pileup, it fails for a more realistic model of the luminous  
11 profile of the proton beam. A variable used at Level 2 trigger is also shown in this  
12 note to be unstable against increasing pileup.

## 1 Introduction

Throughout its successful operation, the LHC has had a nominal energy increase from  $\sqrt{s} = 1.8$  TeV in 2009 to  $\sqrt{s} = 7$  TeV in 2011 [1][2]. The luminosity has also increased from  $2.1 \times 10^{32} \text{cm}^{-2}\text{s}^{-1}$  in 2010 to approximately  $7 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$  in 2012 [3][4]. In 2014, we expect the LHC to collide protons at  $\sqrt{s} = 13$  TeV to 14 TeV after the upgrade [5]. In the following years the LHC will be performing precision measurements, in particular on the recently discovered candidate for the Higgs boson. This requires a major upgrade on luminosity because this Higgs candidate has a very low production cross section. By 2019 the LHC is expected to reach an instantaneous luminosity of approximately  $3 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ . This increase in luminosity will impact both the selection efficiency and the trigger rates for low  $p_T$  objects. An upgrade of the Level 1 trigger was proposed in which groups of cells called *supercells* are used instead of *Trigger Towers* [6].

In this study it is shown that it is not possible to reject neutral pions from electrons using  $\Delta\eta \times \Delta\phi = 0.025 \times 0.1$  super-cells. The longitudinal profiles of the electrons and the neutral pions are found to be too similar to be exploited for neutral pions rejection. A variable that relies on the differences between the lateral profiles of neutral pions and electrons to reject neutral pions is introduced. This variable is stable against increasing pileup and separates electrons from neutral pions in the ideal case when the interaction point is at  $z = 0$ , where it makes optimal use of the projective geometry of the calorimeter. It fails for a more realistic model of the luminous profile of the beam, which is no longer a  $\delta$ -function at  $z = 0$  but a Gaussian distribution with a width of approximately 5 cm. The variable currently used at Level 2 trigger that exploits the two maxima of energy deposited by neutral pions is shown to be less effective against increasing pileup, prompting more detailed studies in the future.

## 2 The ATLAS Trigger

The ATLAS Trigger system comprises three levels [7][8]. This study is restricted to the first level (L1). At this level, regions in the calorimeter are identified that have energy deposits larger than a predefined threshold. To maintain high processing speeds it is not possible to do this on a cell level and therefore exploit the full granularity of the calorimeter. Coarser regions of size  $\Delta\eta \times \Delta\phi = 0.1 \times 0.1$  (Trigger Towers, TT) in the electromagnetic section of the calorimeter (EM Cal) are used instead. The EM Cal has four layers and these are the Presampler (PS) and the first (Layer 1) up to the third layer (Layer 3). Layer 1 comprises strips which are narrower in  $\eta$  than the cells in Layer 2. Layer 2 has the largest radiation length of the EM Cal and therefore receives the largest fraction of energy from electromagnetic objects. Cells in the PS and Layer 2 have the same width in  $\eta$  ( $\Delta\eta = 0.025$ ) and the widest cells in  $\eta$  are in Layer 3 ( $\Delta\eta = 0.05$ ). Figure 1 shows the segmentation of the different layers for the barrel of the calorimeter. In this study we concentrate only on the barrel.

In Layer 2 one TT comprises  $4 \times 4$  cells in  $(\eta \times \phi)$ . The current L1 trigger algorithm first runs a sliding window to find a local maximum that comprises  $2 \times 2$  TTs in  $(\eta, \phi)$ . These  $2 \times 2$  tower regions shown in green in Figure 2 are called Clusters. The algorithm then computes the horizontal and the vertical sums of energy in this local maximum and labels the highest as the candidate energy for the cluster. It accepts the cluster if this energy is greater than the threshold energy, otherwise the cluster is rejected. The neighboring towers that surround the cluster make up the Isolation Ring (IR). A ratio of the cluster energy and the IR is a good variable to study the lateral profiles of different objects, and in particular can be used to separate EM objects against hadronic objects at trigger level.

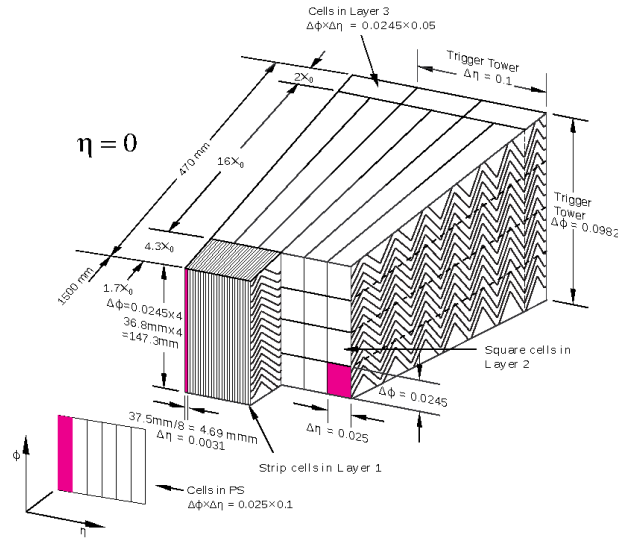


Figure 1: Different layers in the EM Cal.  $\eta = 0$  shows that this structure is for the barrel of the calorimeter. End caps have a different layout.

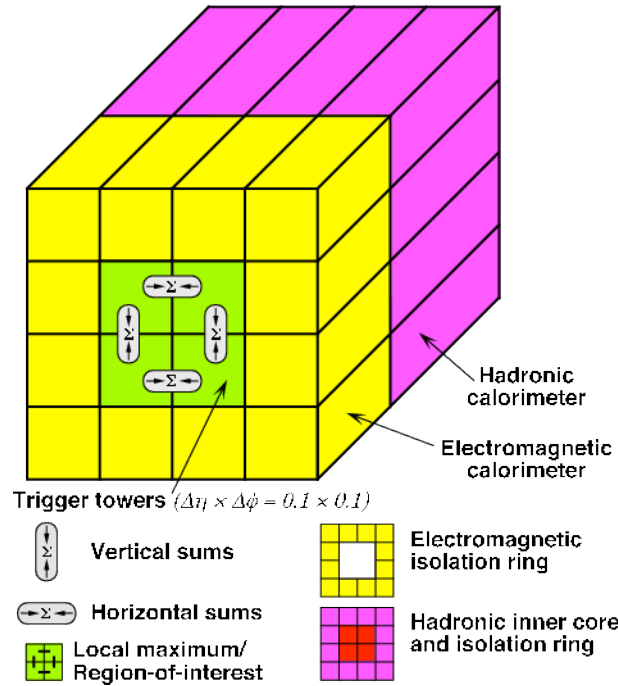


Figure 2: The L1 algorithm for electron- $\gamma$  identification.

### 58 3 Monte Carlo samples

59 The procedure for obtaining Monte Carlo samples is the following. Single, isolated electrons  
 60 or neutral pions are generated by an Athena package called ParticleGenerator [9] with a pre-  
 61 defined energy and direction in  $(\eta, \phi)$  in the EM Cal. For simplicity the chosen  $(\eta, \phi)$  direction  
 62  $(0.4125, 0.1125)$  is the center of a cell and Geant4 [10] is used to simulate the EM Cal. The out-  
 63 put of this simulation is digitized and subsequently reconstructed. D3PDs are made out of the  
 64 reconstructed data. Figure 3 illustrates the simulation chain used.

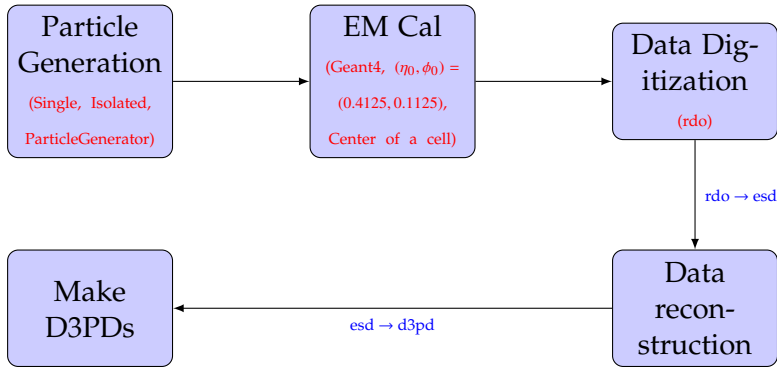


Figure 3: Flowchart of the sample generation chain.

65 Separate Monte Carlo samples were also made in which electrons and neutral pions were  
 66 generated over a range in  $\eta$  covering the width of a cell in Layer 2 ( $\Delta\eta = 0.025$ ) which is also the  
 67 width of a supercell. We will refer to samples generated in this manner as *scanned*  $\eta$  samples.  
 68 The samples generated as described in the preceding paragraph are *fixed*  $\eta$  samples.

69 ParticleGenerator by default assumes that the interaction point of the particles in the col-  
 70 linder can be described by a  $\delta$ -function at  $z = 0$ . This is the ideal situation. A more realistic  
 71 model describes the interaction point with a Gaussian distribution with RMS  $\approx 5$ cm. In this  
 72 note, we refer to this effect as *Vertex Smearing*.

## 73 4 Results

### 74 4.1 Longitudinal Profile

75 One variable  $\rho_{layer}$  that quantifies the depth profile of an object is the fraction of energy de-  
 76 posited in a layer of the calorimeter and the total energy deposited in all four layers. In this  
 77 study, the total energy is the energy deposited in the cluster with the most energy in the barrel  
 78 of the calorimeter.  $\rho_{layer}$  for a particular layer is then the ratio of the energy deposited in the  
 79 layer and cluster in question, and this total energy:

$$\rho_{layer} = \frac{\sum_{c \in cl, c \in layer} (E_c)}{E_{cl}}, \quad (1)$$

80 where  $layer \in \{0, 1, 2, 3\}$ ,  $cl$  is the cluster that contains the most energy and  $c$  represents  
 81 individual cells whose dimensions depend on the layer. For the PS and for Layer 3 Figure 4  
 82 shows that the deposited energy fraction is less than 5% for all studied particle energies. Most  
 83 of the energy is deposited in Layer 1 and Layer 2. This study therefore concentrates on Layer 1  
 84 and Layer 2.

85 Figure 5 (left) is an overlay of  $\rho_1$  and  $\rho_2$  for both electrons and pions for increasing electron  
 86 or pion energy. Since we are mostly interested with triggering for low  $p_T$  objects, we restrict our  
 87 analysis to objects with not more than 50 GeV. It is clear from Figure 5 that electrons and pions  
 88 exhibit similar longitudinal profiles. The plot on the right in the same Figure is a 2-dimensional  
 89 distribution of  $\rho_1$  vs.  $\rho_2$  for 20 GeV electrons and 20 GeV neutral pions. Both electrons and  
 90 pions show the expected anticorrelation in  $\rho_1$  and  $\rho_2$ ; there are no differences strong enough  
 91 to warrant a separation. Figure 6 shows an example distribution for 20 GeV objects in  $\rho_1$  (left)  
 92 and for  $\rho_2$  (right). No simple cuts can be made on both variables that will reject a significant  
 93 fraction of neutral pions without losing more than 5% of electrons.

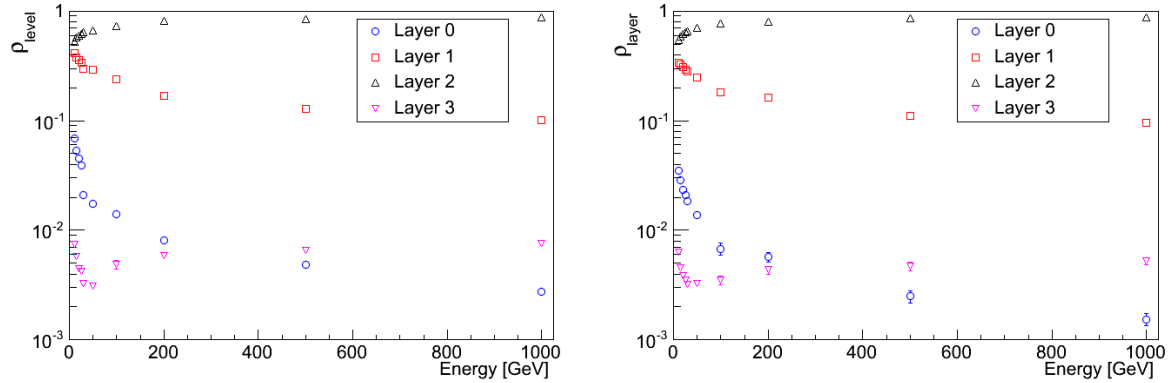


Figure 4: [Left]  $\rho_{layer}$  for electrons for all the layers of the EM Cal. [Right]  $\rho_{layer}$  for neutral pions for all the layers of the EM Cal.

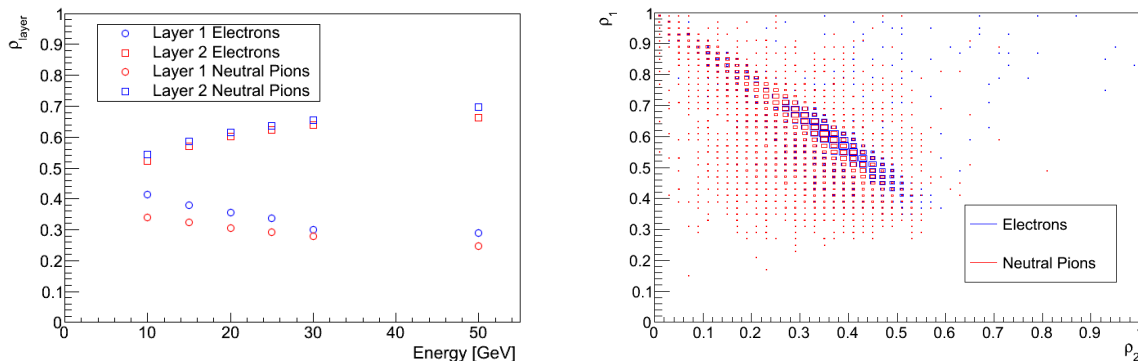


Figure 5: [Left] A comparison of neutral pions and electrons in  $\rho_1$  and  $\rho_2$  versus increasing incident energy. [Right]  $\rho_1$  versus  $\rho_2$  for electrons and neutral pions.

94 For further comparison between the fraction of energy deposited in Layer 1 and in Layer 2,  
 95 we introduce

$$\rho_{comp} = \frac{\rho_1}{\rho_2} \quad (2)$$

96 One advantage that  $\rho_{comp}$  has over the other possible variables is that it is less sensitive to  
 97 pileup because pileup offsets in  $\rho_1$  and in  $\rho_2$  cancel out. That minimizes uncertainties. Figure 7  
 98 is an overlay of  $\rho_{comp}$  for electrons and neutral pions versus their energy. Again, there are no  
 99 major differences that can enable separation between these two objects for energies less than  
 100 50 GeV.

101 Figure 8 shows  $\rho_{comp}$  for 20 GeV electrons and pions. Again, no simple cuts can be made  
 102 that will reduce background significantly and yet maintain less than 1% signal loss. Similar  
 103 studies at different and higher pileups show no differences as expected (Figure 8 right). Pileup  
 104 therefore does not affect  $\rho_{comp}$ . In the next section we will therefore study the possibility of  
 105 electron-neutral pion separation based on the lateral profiles.

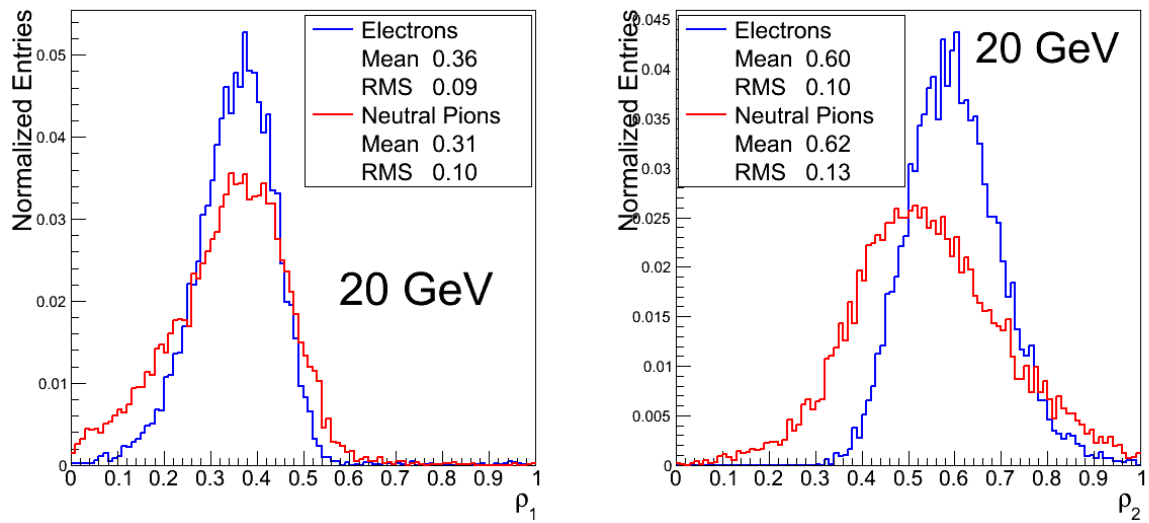


Figure 6: [Left]  $\rho_1$  distribution for 20 GeV electrons and neutral pions. [Right]  $\rho_2$  distribution for 20 GeV electrons and neutral pions.

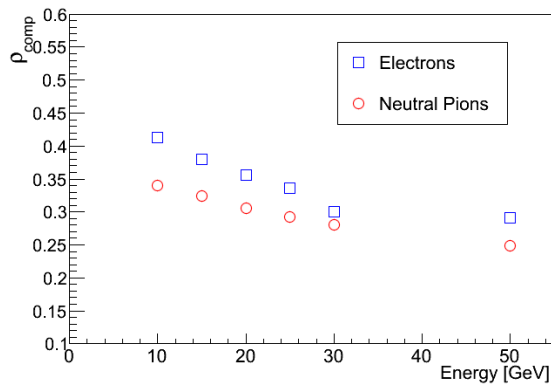


Figure 7:  $\rho_{comp}$  versus the incident energy of electrons and neutral pions.

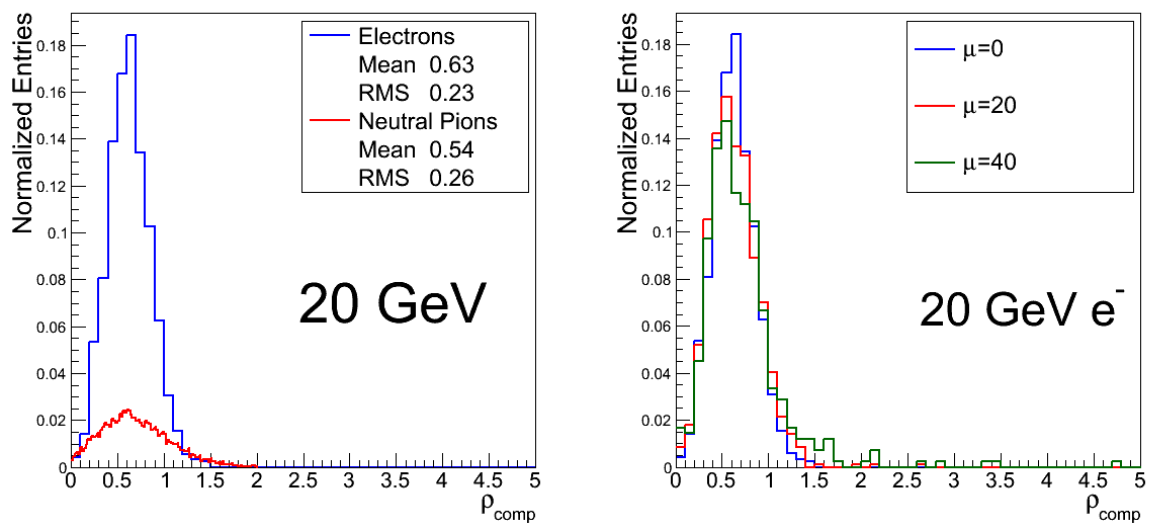


Figure 8: [Left]  $\rho_{comp}$  distribution for 20 GeV electrons and neutral pions. [Right]  $\rho_{comp}$  distribution for 20 GeV electrons at different pileups.

## 106 4.2 Lateral Profile

107 The electron- $\gamma$  identification algorithms used offline and those used for the Level 2 trigger have  
 108 access to full granularity. Offline algorithms are used as a benchmark for any differences be-  
 109 tween the lateral profiles of the electrons and the neutral pions. These differences can therefore  
 110 offer some insight onto rejection techniques for triggering. In Layer 1, one variable that quan-  
 111 tifies this is the number of strips that have both energy hits above a certain threshold and the  
 112 same  $\phi$  position as the strip with the most energy. Figure 9 (left) shows this variable versus the  
 113 energy of electrons and neutral pions. The threshold energy here is 1% of the energy contained  
 114 in the cluster with the most energy. For low energy objects, and hence for low  $p_T$  objects, a  
 115 separation between electrons and neutral pions can be easily deduced since for objects with  
 116 energy less than 30 GeV the profile for neutral pions is on average one strip wider. Figure 9  
 117 (right) shows an example distribution for 20 GeV objects. Since in Layer 1 the supercells are 8  
 118 strips wide (Figure 1), we can deduce from Figure 9 (right) that the energy shower in Layer 1  
 119 is contained in at most two neighboring supercells for the no-pileup case ( $\mu = 0$ ). For 20 GeV  
 120 electrons Figure 10 shows that at higher pileup the electron profile does not change <sup>1</sup>. This  
 121 implies that neutral pions at higher pileup also have a wider energy shower.

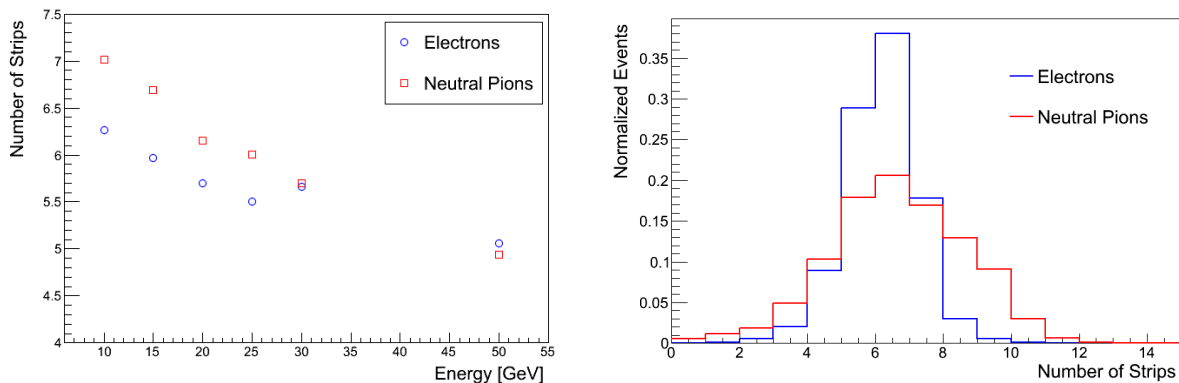


Figure 9: [left] Mean number of strips with hits  $> 1\%$  of cluster energy vs.  $e^-/\pi^0$  energy. [right] Mean number of strips with hits  $> 1\%$  of cluster energy at 20GeV for electrons and neutral pions

### 122 4.2.1 $R_\eta^{(1)}$

123 For online neutral pion rejection we introduce

$$R_\eta^{(1)} = \frac{E_0}{E_1 + E_0 + E_{-1}} \quad (3)$$

124 where  $E_0$  is the energy deposited in the supercell with the most energy and  $E_{\pm l}$  is the en-  
 125 ergy deposited in  $\pm l$  supercells around the supercell in  $\eta$  with the most energy. We use three  
 126 supercells here since the energy shower is contained in at most two supercells (Figure 9 (right)).  
 127 The left plot in Figure 11 shows how  $R_\eta^{(1)}$  for electrons differs from that of neutral pions for in-  
 128 creasing energies and the one on the right in the same Figure shows the distribution for 20 GeV  
 129 electrons and neutral pions as an example. Distributions shown in Figure 11 are from Monte

<sup>1</sup>The Monte-Carlo samples used for electrons in Figure 9 (right) are not the same as those used for  $\mu = 0$  in Figure 10. This explains why the distributions are not identical.

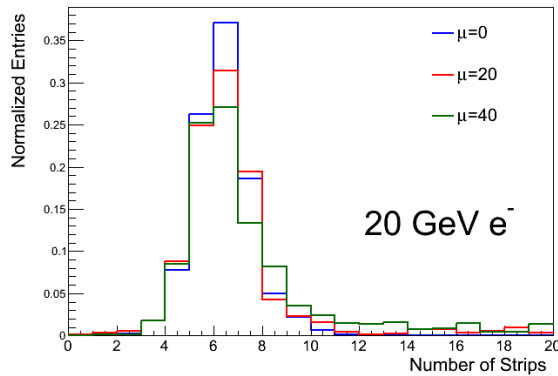


Figure 10: Number of strips with hits  $> 1\%$  of cluster energy at different pileups, for 20 GeV electrons

130 Carlo samples with vertex smearing turned off and fixed  $\eta$ . For low  $p_T$  objects, a good separation  
 131 can be achieved between electrons and neutral pions. For 20 GeV objects when vertex  
 132 smearing is turned off, a rejection criteria based on  $R_\eta^{(1)}$  can reject more than 50% of neutral  
 133 pions while losing less than 5% of the total electrons.

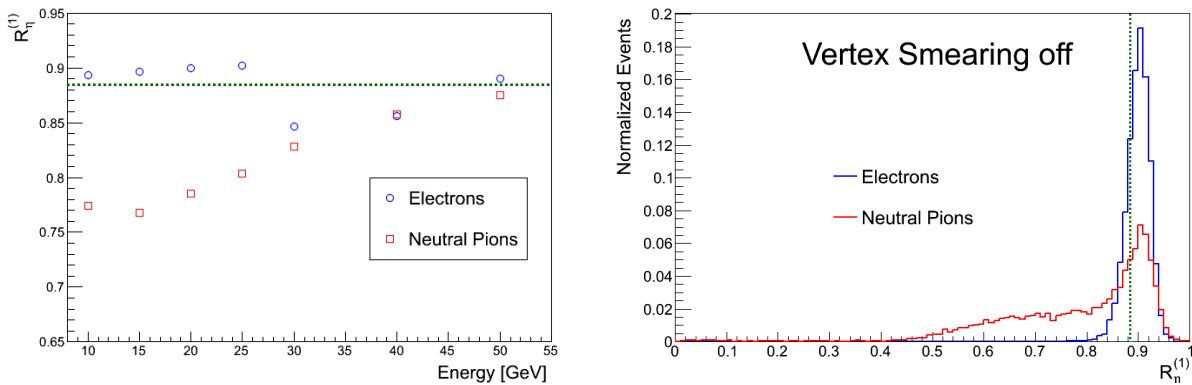


Figure 11: [Left]  $R_\eta^{(1)}$  versus the incident energy of electrons and neutral pions when vertex smearing is turned off and fixed  $\eta$ . [Right]  $R_\eta^{(1)}$  for 20 GeV electrons and neutral pions when vertex smearing is off and  $\eta$  is fixed.

134 Figure 12 shows how the distribution for  $R_\eta^{(1)}$  changes for 20 GeV electrons and neutral pions  
 135 when vertex smearing is turned on. When vertex smearing is turned on, projection onto a single  
 136 supercell deteriorates for a fraction of events. This is evident from a tail that develops for the  
 137 electron  $R_\eta^{(1)}$  distribution. The change in the tail is not apparent for neutral pions because their  
 138 distribution is spread out even without vertex smearing. The result of this is a loss of separation  
 139 between electrons and neutral pions when vertex smearing is turned on. Since the the model  
 140 with vertex smearing is more realistic, we restrict our analysis to that.

141 Figure 13 shows  $R_\eta^{(1)}$  when electrons or neutral pions are scanned over a  $\Delta\eta = 0.025$  range,  
 142 which is the width of a supercell in  $\eta$ . As expected, scanning over  $\eta$  does not restore the separation  
 143 between electrons and neutral pions. There are also no major differences between scanning  
 144 and fixing  $\eta$ , so restrict our studies to the case when  $\eta$  is fixed.

145 The algorithm that calculates  $R_\eta^{(1)}$  first identifies the supercell with the highest energy in  
 146 Layer 2 and then uses the same  $(\eta, \phi)$  position to identify the supercell with the highest energy



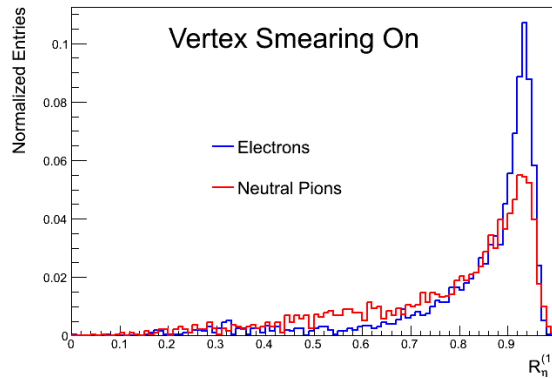


Figure 12:  $R_\eta^{(1)}$  for 20 GeV electrons and neutral pions when vertex smearing is on and  $\eta$  is fixed.

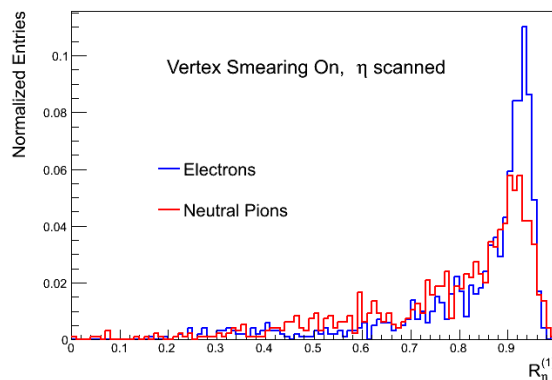


Figure 13:  $R_\eta^{(1)}$  for 20 GeV electrons and neutral pions when vertex smearing is on and  $\eta$  is scanned.

147 in Layer 1. This approach correctly identifies the supercell with the highest energy in Layer 1  
 148 when vertex smearing is turned off, but when the vertex smearing is turned on it is possible  
 149 to wrongly identify this supercell. Rather than using collider coordinates  $(\eta, \phi)$  to identify cells  
 150 and supercells, we label each cell and supercell with two individual indices  $(i\eta, i\phi)$ . The variable

$$\Delta\eta = i\eta_{H1} - i\eta_{H2}, \quad (4)$$

151 quantifies how aligned the supercells are in Layer 1 and Layer 2, where  $i\eta_{Hj}^2$  is the  $\eta$  index  
 152 for the supercell in layer  $j$  with the highest energy. The left plot in Figure 14 shows how  $\Delta\eta$   
 153 changes when vertex smearing is on. When vertex smearing is off, using the supercell in layer  
 154 2 as the seed correctly identifies the highest-energy supercell in layer 1. When vertex smearing  
 155 is turned on, this algorithm fails for a fraction of events so it becomes important to seed from  
 156 Layer 1. The right plot in Figure 14 shows  $R_\eta^{(1)}$  when the highest-energy supercell is seeded  
 157 from Layer 1, and when vertex smearing is turned on. Since almost all the energy is deposited  
 158 in two neighboring supercells, the highest-energy one included, when the correct supercell is  
 159 identified  $R_\eta^{(1)}$  is always greater than or equal to 0.5. The fraction of events that a supercell is  
 160 incorrectly identified when seeding from Layer 2 is so small that correcting the seed does not  
 161 yield a visible improvement in separation between electrons and neutral pions.

<sup>2</sup>This index is weighted with energy.  $i\eta_{Hj} = \frac{\sum_k E_k \times i\eta_k}{\sum_k E_k}$  where  $k \in \{0, \pm 1\}$  identifies the supercells, 0 being the highest-energy supercells and  $\pm 1$  is for the neighboring supercells.

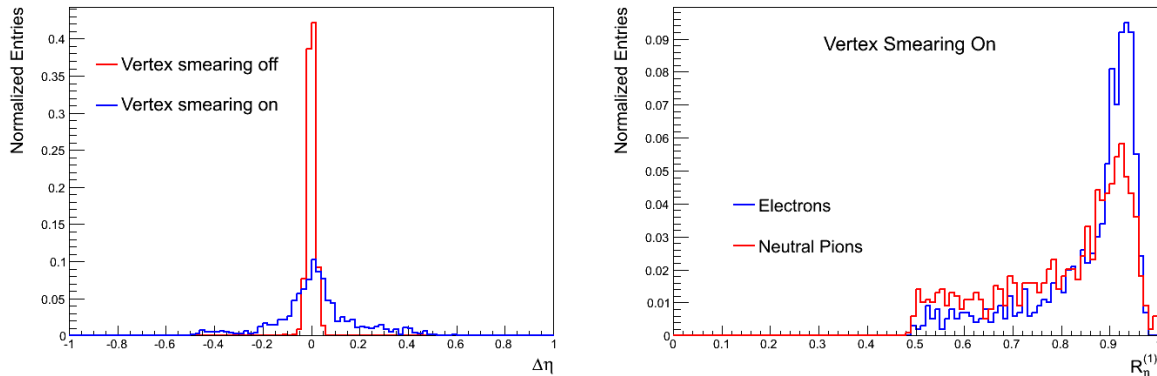


Figure 14: [Left]  $\Delta\eta$  for electrons when vertex smearing is turned on and off. [Right]  $R_\eta^{(1)}$  when seeding the highest-energy supercell from Layer 1 instead of Layer 2. Vertex smearing is also turned on.

#### 162 4.2.2 $E_r$ for Level 2

163 Although the energy deposit from neutral pions is often found to have two maxima because  
 164 of the  $\pi^0 \rightarrow \gamma\gamma$  decay, these two maxima are normally within one supercell in  $\eta$ . It is therefore  
 165 not possible to exploit this property to separate them from electrons at Level 1 trigger using  
 166 supercells. At Level 2 the variable

$$E_r = \frac{E_{max} - E_{smax}}{E_{max} + E_{smax}} \quad (5)$$

167 is used, where  $E_{max}$  is the energy deposited in the strip that receives the most energy and  
 168  $E_{smax}$  is the energy deposited in the strip that receives the second largest energy deposit. Since  
 169 electrons normally have one maximum of energy deposition,  $E_r$  is expected to be close to 1;  
 170 for neutral pions the distribution is expected to be more spread out. Figure 15 shows a good  
 171 separation achieved at level 2 trigger using this variable. The plot on the right in Figure 15  
 172 shows that  $E_r$  is stable after turning vertex smearing on. This shows that at full granularity, it  
 173 is possible to separate electrons from neutral pions at Level 2 trigger. Figure 16 shows that  $E_r$   
 174 is also stable after introducing scanning. As pointed out before, there are no major differences  
 175 between scanning over  $\eta$  and not scanning over  $\eta$ .

176 Figure 17 shows the electron efficiency when  $E_r$  is used at Level 2 trigger and when  $R_\eta^{(1)}$   
 177 is used at Level 1.  $E_r$  is stable against vertex smearing. At Level 2  $E_r$  can reject 60% neutral  
 178 pions while losing not more than 2% electrons (top left). When vertex smearing is turned on,  
 179 60% neutral pions can also be rejected while losing not more than 2% even when  $\eta$  is scanned  
 180 (bottom left).  $R_\eta^{(1)}$  deteriorates when vertex smearing is turned on (top right). The deterioration  
 181 of  $R_\eta^{(1)}$  is consistent also when  $\eta$  is scanned (bottom right).

182 Figure 18 shows the electron efficiency when  $E_r$  is used at different pileups. It is clear that  
 183 rejection of neutral pions from electrons is significantly reduced at higher pileups when using  
 184  $E_r$ . This warrants further investigation in future studies.

## 185 5 Summary and Conclusions

186 In order to keep exploring new physics at the LHC using the ATLAS detector we need to up-  
 187 grade its trigger system so that it can accommodate low  $p_T$  objects that come from rare events. In-  
 188 creasing the granularity of trigger from Trigger Towers to supercells is one of the ways that the

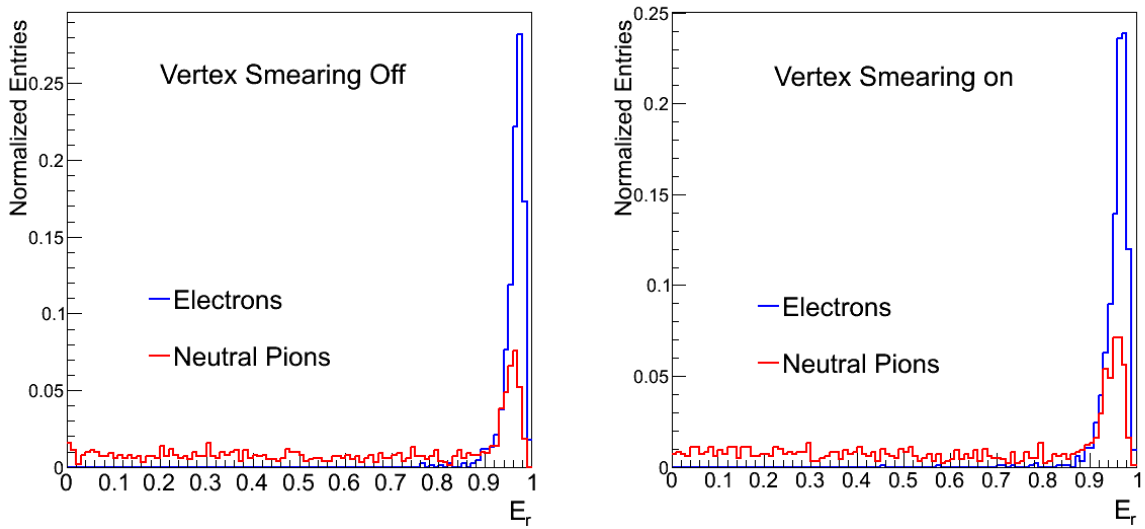


Figure 15: [Left]  $E_r$  when vertex smearing is turned off. [Right]  $E_r$  when vertex smearing is turned on.

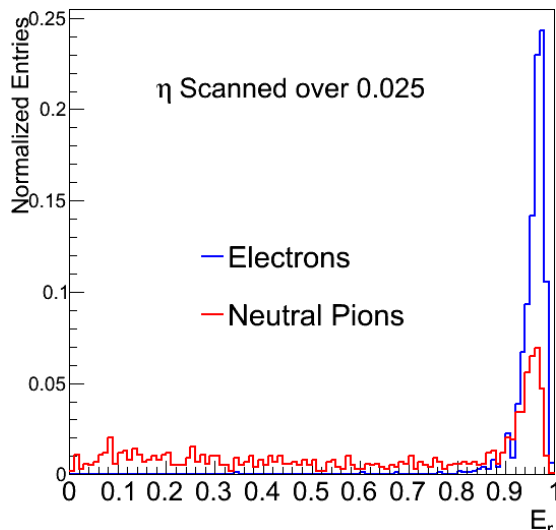


Figure 16:  $E_r$  is not affected by scanning. Good separation between electrons and neutral pions is achieved both when  $\eta$  is fixed and when it is scanned over a range.

189 Level 1 trigger can be improved. Using supercells in Layer 1 of the electromagnetic calorimeter  
 190 however does not achieve a separation of electrons from neutral pions. In the ideal case when  
 191 the interaction point of the colliding protons is at  $z = 0$   $R_\eta^{(1)}$  can achieve a good separation be-  
 192 tween electrons and neutral pions. In a more realistic case when the luminous profile of the  
 193 colliding beams is more spread out this separation is greatly reduced. Although the variable  
 194  $E_r$ , used at Level 2 trigger to reject neutral pions from electrons is stable against spreading out  
 195 the luminous profile of the beam, it becomes inefficient as pileup increases and will likely be  
 196 unusable in Phase-I upgrade conditions ( $\mu = 80$ ) and beyond. Further studies therefore have to  
 197 be done to improve not only the Level 1 trigger of ATLAS but also the Level 2 trigger.

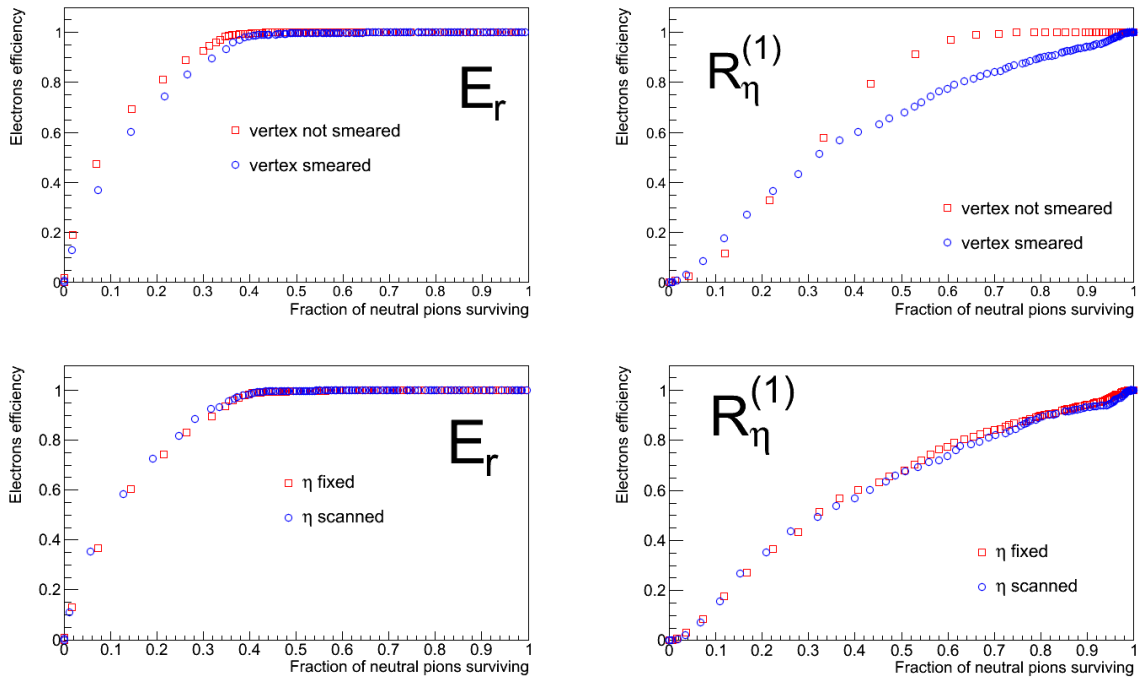


Figure 17: [Top Left] Electron efficiency versus the fractions of neutral pions surviving using  $E_r$  with and without vertex smearing. [Top Right] Electron efficiency versus the fraction of neutral pions surviving using  $R_\eta^{(1)}$  with and without vertex smearing. [Bottom Left] Electron efficiency versus the fractions of neutral pions surviving using  $E_r$  with fixed and scanned  $\eta$ , when vertex smearing is turned on. [Bottom Right] Electron efficiency versus the fractions of neutral pions surviving using  $R_\eta^{(1)}$  with fixed and scanned  $\eta$ , when vertex smearing is turned on.

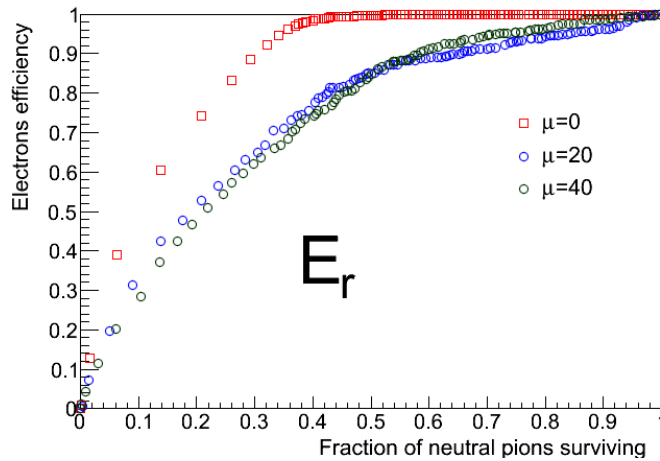


Figure 18:  $E_r$  becomes ineffective at high pileups.

## 198 6 Acknowledgements

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