1443-501 Spring 2002 Lecture #8 Dr. Jaehoon Yu

- 1. Work and Kinetic Energy
- 2. Energy Loss in Automobile
- 3. Potential Energy
- 4. Conservative and Non-conservative Forces
- 5. Conservative Forces and Potential Energy

Work and Kinetic Energy

Work in physics is done only when a sum of forces exerted on an object made a motion to the object.

What does this mean?

However much tired your arms feel, if you were just holding an object without moving it you have not done any physical work.

 $K = \frac{1}{2}mv^2$

 $W = \sum F_i \cdot d = Fd\cos q$

 $W = K_f - K_i = \Delta K$

 $P = \frac{dW}{dt} = \vec{F} \cdot \frac{d}{dt} \left(\vec{s} \right) = \vec{F} \cdot \vec{v}$

Nm/s=Joule/s=Watt

Nm=Joule

Mathematically, work is written in scalar product of force vector and the displacement vector

Kinetic Energy is the energy associated with motion and capacity to perform work. Work requires change of energy after the completion Work-Kinetic energy theorem

Power is the rate of which work is performed.

Units of these quantities????

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Energy Loss in Automobile

Automobile uses only at 13% of its fuel to propel the vehicle.

| Why? |
|------|
|------|

67% in the engine:

1. Incomplete burning

2. Heat

3. Sound

16% in friction in mechanical parts

4% in operating other crucial parts such as oil and fuel pumps, etc

13% used for balancing energy loss related to moving vehicle, like air resistance and road friction to tire, etc



Example 7.14

A compact car has a mass of 800kg, and its efficiency is rated at 18%. Find the amount of gasoline used to accelerate the car from rest to 27m/s (~60mi/h). Use the fact that the energy equivalent of 1gal of gasoline is $1.3x10^8$ J.

First let's compute what the kinetic energy needed to accelerate the car from rest to a speed *v*.

Since the engine is only 18% efficient we must divide the necessary kinetic energy with this efficiency in order to figure out what the total energy needed is.

$$K_f = \frac{1}{2}mv^2 = \frac{1}{2} \times 800 \times (27)^2 = 2.9 \times 10^5 J$$

$$W_E = \frac{K_f}{\mathbf{e}} = \frac{1}{2\mathbf{e}}mv^2 = \frac{2.9 \times 10^5 J}{0.18} = 16 \times 10^5 J$$

Then using the fact that 1gal of gasoline can putout 1.3x10⁸J, we can compute the total volume of gasoline needed to accelerate the car to 60 mi/h.

$$V_{gas} = \frac{W_E}{1.3 \times 10^8 \, J \,/\,gal} = \frac{16 \times 10^5 \, J}{1.3 \times 10^8 \, J \,/\,gal} = 0.012 \, gal$$

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Kinetic Energy at High Speed

The laws of Newtonian mechanics is no longer valid for object moving at the speed close to that of light, c. It must be more generalized for these special cases. \rightarrow Theory of relativity.

The kinetic energy must be modified to reflect the fact that the object is moving very high speed.



What does this expression tell you?

The speed of an object cannot be faster than light in vacuum. ← Have not seen any particle that runs faster than light, yet.

However this equation must satisfy the Newtonian expression!!

$$K = mc^{2} \left(\frac{1}{\sqrt{1 - (\frac{v}{c})^{2}}} - 1 \right) = mc^{2} \left(1 + \frac{1}{2} \left(\frac{v}{c} \right)^{2} + \frac{3}{8} \left(\frac{v}{c} \right)^{4} + \dots - 1 \right)$$
$$= mc^{2} \left(1 + \frac{1}{2} \left(\frac{v}{c} \right)^{2} - 1 \right) = \frac{1}{2} mc^{2} \times \left(\frac{v}{c} \right)^{2} = \frac{1}{2} mv^{2}$$

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Potential Energy

Energy associated with a system of objects Stored energy which has Potential or possibility to work or to convert to kinetic energy

What does this mean?

In order to describe potential energy, U, a system must be defined.

The concept of potential energy can only be used under the special class of forces called, conservative forces which results in principle of <u>conservation of mechanical energy.</u>

What other forms of energies in the universe?



Gravitational Potential

Potential energy given to an object by gravitational field in the system of Earth due to its height from the surface

When an object is falling, gravitational force, Mg, performs work on the object, increasing its kinetic energy. The potential energy of an object at a height y which is the potential to work is expressed as

Work performed on the object by the gravitational force as the brick goes from y_i to y_f is:

$$W_g = U_i - U_f$$
$$= mgy_i - mgy_f = -\Delta U_g$$

What does this mean?

Work by the gravitational force as the brick goes from y_i to y_f is negative of the change in the system's potential energy

m

m

y_f

y_i

т**д**

Example 8.1

A bowler drops bowling ball of mass 7kg on his toe. Choosing floor level as y=0, estimate the total work done on the ball by the gravitational force as the ball falls.

Let's assume the top of the toe is 0.03m from the floor and the hand was 0.5m above the floor.



 $U_{i} = mgy_{i} = 7 \times 9.8 \times 0.5 = 34.3 J$ $U_{f} = mgy_{f} = 7 \times 9.8 \times 0.03 = 2.06 J$ $\Delta U_{f} = -(U_{f} - U_{i}) = 32.24 J \cong 30 J$

b) Perform the same calculation using the top of the bowler's head as the origin.

What has to change?

First we must re-compute the positions of ball at the hand and of the toe.

Assuming the bowler's height is 1.8m, the ball's original position is –1.3m, and the toe is at –1.77m.

$$U_{i} = mgy_{i} = 7 \times 9.8 \times (-1.3) = -89.2 J$$

$$U_{f} = mgy_{f} = 7 \times 9.8 \times (-1.77) = -121 .4 J$$

$$\Delta U = -(U_{f} - U_{i}) = 32.2 J \approx 30 J$$

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Elastic Potential Energy

Potential energy given to an object by a spring or an object with elasticity in the system consists of the object and the spring without friction.



Conservative and Non-conservative Forces

The work done on an object by the gravitational force does not depend on the object's path.



When directly falls, the work done on the object is

When sliding down the hill of length I, the work is

 $W_{g} = F_{g-incline} \times l = mg \sin \boldsymbol{q} \times l$ $= mg (l \sin \boldsymbol{q}) = mgh$

 W_{g}

How about if we lengthen the incline by a factor of 2, keeping the height the same??

Still the same amount of work ©

 $W_g = mg$

= mgh

So the work done by the gravitational force on an object is independent on the path of the object's movements. It only depends on the difference of the object's initial and final position in the direction of the force.

The forces like gravitational or elastic forces are called conservative forces

If the work performed by the force does not depend on the path
 If the work performed on a closed path is 0.

More on Conservative and Non-conservative Forces

A potential energy can be associated with a conservative force

A work done on a object by a conservative force is the same as the potential energy difference between initial and final states

$$W_c = U_i - U_f = -\Delta U$$

So what is a conservative force?

The force that conserves mechanical energy.

OK. Then what are nonconservative forces?

Can you tell me what such forces are?

The work by these forces depends on the path.

Friction forces

Why are they non-

conservative forces?

What happen to the energy?

Because the longer the path of an object's movement, the more work the friction forces perform on it.

The force that does not conserve mechanical energy.

Kinetic energy converts to thermal energy and is not reversible.

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Conservative Forces and Potential Energy

The work done on an object by a conservative force is equal to the decrease in the potential energy of the system

$$W_c = \int_{x_i}^{x_f} F_x dx = -\Delta U$$

What else does this statement tell you?

The work done by a conservative force is equal to the negative of the change of the potential energy associated with that force.

Only the changes in potential energy of a system is physically meaningful!!

We can rewrite the above equation in terms of potential energy U

So the potential energy associated with a conservative force at any given position becomes

$$\Delta U = U_f - U_i = -\int_{x_i}^{x_f} F_x dx$$

$$U_f(x) = -\int_{x_i}^{x_f} F_x dx + U_i$$

Potential energy function

What can you tell from the potential energy function above?

Since U_i is a constant, it only shifts the resulting $U_f(x)$ by a constant amount. One can always change the initial potential so that U_i can be 0.