

# PHYS 1441 – Section 004

## Lecture #2

*Monday, Jan. 26, 2004*

*Dr. Jaehoon Yu*

- Chapter one
  - Uncertainties and Significant Figures
  - Standards and units
  - Estimates
  - Unit conversions
- Chapter two
  - Fundamentals
  - Velocity and Speed (Average and instantaneous)
  - Acceleration



# Announcements

- Reading assignment #2: Read and follow through Appendix sections by Monday, Feb. 2
  - A-5, A-6, A-7, A-8 and A-9
- There will be a quiz on Wednesday, Jan. 28
- Homework Registration: 42/65 (15 of you submitted it)
  - You **must** download, print, solve and submit electronically your homework to obtain 100% credit for homework #1
  - Homework #1 due 1pm, Wednesday, Jan. 28
  - Roster will close Wednesday, Jan. 28
- E-mail distribution list (phys1441-004-spring04)
  - 18 of you subscribed as of 10am this morning
  - **5 points** extra credit if done by 6pm today, Jan. 26
  - **3 points** extra credit if done by 6pm Wednesday, Jan. 28
  - **1 point** extra credit if done by 6pm Monday, Feb. 2



PHYS 1441 sec 004C L&S ROLL	1/21/2004	Homework registration	e-mail
Last Name	First Name		
Amund	Isabel	1/23/2004	
Amund	Wyndell	1/23/2004	1/23/2004
2504	Barajas		
7025	Bascoadegan,	1/23/2004	1/23/2004
2301	Bergman,	1/23/2004	
3505	Bier,	1/23/2004	1/23/2004
488	Black,	1/23/2004	
2525	Blackmon,	1/23/2004	
59	Buckley,	1/23/2004	
1735	Caldwell,	1/23/2004	1/23/2004
372	Canby,	1/23/2004	
1450	Can,	1/23/2004	
5153	Chavez,	1/23/2004	1/23/2004
2304	Coker,	1/23/2004	1/23/2004
3453	Conley,	1/26/2004	1/26/2004
3200	Cooker,		
3994	Cramer,	1/23/2004	
5750	Crouse,	1/23/2004	
3032	Cumplan,		
5110	Do,	1/23/2004	
2525	Fitch,	1/23/2004	
4315	Floyd,		
5450	Gaskill,		1/26/2004
2534	Godfrey,		
3555	Gonzales,	1/23/2004	
3745	Gould,		
1555	Ha,		
1555	Hall,		
254	Hall II,	1/23/2004	
2555	Hille,		
5055	Lee,		
5455	Larkin,	1/23/2004	1/23/2004
5555	Le,	1/26/2004	
5555	Le,	1/26/2004	1/26/2004
4755	Lee,	1/23/2004	
4131	LeNg,	1/23/2004	
2214	McClister,	1/23/2004	1/24/2004
7545	McCammon,	1/23/2004	1/23/2004
1745	McCallister,	1/23/2004	1/23/2004
3235	Medina,	1/23/2004	
5573	Melendez,		
1535	Mella,		
4472	Mewby,	1/26/2004	
5171	Rankin,	1/26/2004	
5735	Parker,	1/23/2004	
5554	Patel,	1/23/2004	1/26/2004
5555	Paulk,	1/23/2004	
2515	Person,	1/23/2004	
4755	Perrin,		
4745	Pope,		
5105	Pride,		
2555	Quinn,	1/23/2004	1/23/2004
4504	Rab,		
3355	Rauk,		
1044	Ros,		
5435	Robinson,	1/26/2004	
2120	Sinner,	1/23/2004	
5155	Smith,	1/23/2004	
2300	Sterks,		
4505	Thompson,	1/26/2004	
5151	Vergara,	1/23/2004	1/23/2004
2551	Magliano,	1/26/2004	
2555	West,		
5755	Williams,	1/23/2004	1/23/2004

# Uncertainties

- Physical measurements have limited precision, however good it is, due to:

Stat. { – Number of measurements

Syst. { – Quality of instruments (meter stick vs micro-meter)  
– Experience of the person doing measurements  
– Etc

- In many cases, uncertainties are more important and difficult to estimate than the central (or mean) values

**Why and when do uncertainties matter?**



# Significant Figures

- Significant figures denote the precision of the measured values
  - Significant figures: non-zero numbers or zeros that are not place-holders
    - 34 has two significant digits, 34.2 has 3, 0.001 has one because the 0's before 1 are place holders, 34.100 has 5, because the 0's after 1 indicates that the numbers in these digits are indeed 0's.
    - When there are many 0's, use scientific notation:
      - $31400000 = 3.14 \times 10^7$
      - $0.00012 = 1.2 \times 10^{-4}$



# Significant Figures

- Operational rules:
  - Addition or subtraction: Keep the smallest number of decimal place in the result, independent of the number of significant digits:  $34.001 + 120.1 = 154.1$
  - Multiplication or Division: Keep the smallest significant figures in the result:  $34.001 \times 120.1 = 4083$ , because the smallest significant figures is 4.



# Needs for Standards and Units

- Basic quantities for physical measurements
  - Length, Mass, and Time
- Need a language that everyone can understand each other
  - Consistency is crucial for physical measurements
  - The same quantity measured by one must be comprehensible and reproducible by others
  - Practical matters contribute
- A system of unit called SI (*System Internationale*) established in 1960
  - Length in meters ( $m$ )
  - Mass in kilo-grams ( $kg$ )
  - Time in seconds ( $s$ )



# Definition of Base Units

SI Units	Definitions
$1 \text{ m (Length)} = 100 \text{ cm}$	One meter is the length of the path traveled by light in vacuum during a time interval of <u><math>1/299,792,458</math> of a second</u> .
$1 \text{ kg (Mass)} = 1000 \text{ g}$	It is equal to the mass of the international prototype of the kilogram, made of platinum-iridium in International Bureau of Weights and Measure in France.
$1 \text{ s (Time)}$	One second is the <u>duration of 9,192,631,770 periods of the radiation</u> corresponding to the transition between the two hyperfine levels of the ground state of the Cesium 133 ( $\text{C}^{133}$ ) atom.

- *There are prefixes that scales the units larger or smaller for convenience (see pg. 11)*
- *Units for other quantities, such as Kelvins for temperature, for easiness of use*





# Prefixes, expressions and their meanings

- deca (da):  $10^1$
- hecto (h):  $10^2$
- kilo (k):  $10^3$
- mega (M):  $10^6$
- giga (G):  $10^9$
- tera (T):  $10^{12}$
- peta (P):  $10^{15}$
- exa (E):  $10^{18}$
- deci (d):  $10^{-1}$
- centi (c):  $10^{-2}$
- milli (m):  $10^{-3}$
- micro ( $\mu$ ):  $10^{-6}$
- nano (n):  $10^{-9}$
- pico (p):  $10^{-12}$
- femto (f):  $10^{-15}$
- atto (a):  $10^{-18}$



# International Standard Institutes

- International Bureau of Weights and Measure  
<http://www.bipm.fr/>
  - Base unit definitions:  
[http://www.bipm.fr/enus/3\\_SI/base\\_units.html](http://www.bipm.fr/enus/3_SI/base_units.html)
  - Unit Conversions: [http://www.bipm.fr/enus/3\\_SI/](http://www.bipm.fr/enus/3_SI/)
- US National Institute of Standards and Technology (NIST) <http://www.nist.gov/>



# How do we convert quantities from one unit to another?

$$\text{Unit 1} = \text{Conversion factor} \times \text{Unit 2}$$

1 inch	2.54	cm
1 inch	0.0254	m
1 inch	$2.54 \times 10^{-5}$	km
1 ft	30.3	cm
1 ft	0.303	M
1 ft	$3.03 \times 10^{-4}$	km
1 hr	60	minutes
1 hr	3600	seconds
And many	More	Here....



# Examples 1.3 & 1.4

- Ex 1.3: A silicon chip has an area of  $1.25 \text{ in}^2$ . Express this in  $\text{cm}^2$ .

What do we need to know?

$$\begin{aligned}
 1.25 \text{ in}^2 &= 1.25 \text{ in}^2 \times \left( \frac{2.54 \text{ cm}}{1 \text{ in}} \right)^2 \\
 &= 1.25 \text{ in}^2 \times \left( \frac{6.45 \text{ cm}^2}{1 \text{ in}^2} \right) \\
 &= 1.25 \times 6.45 \text{ cm}^2 = 8.06 \text{ cm}^2
 \end{aligned}$$

- 
- Ex 1.4: Where the posted speed limit is 65 miles per hour (mi/h or mph), what is this speed (a) in meters per second (m/s) and (b) kilometers per hour (km/h)?

$$1 \text{ mi} = (5280 \text{ ft}) \left( \frac{12 \text{ in}}{1 \text{ ft}} \right) \left( \frac{2.54 \text{ cm}}{1 \text{ in}} \right) \left( \frac{1 \text{ m}}{100 \text{ cm}} \right) = 1609 \text{ m} = 1.609 \text{ km}$$

$$(a) \quad 65 \text{ mi/h} = (65 \text{ mi}) \left( \frac{1609 \text{ m}}{1 \text{ mi}} \right) \left( \frac{1}{1 \text{ h}} \right) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) = 29.1 \text{ m/s}$$

$$(b) \quad 65 \text{ mi/h} = (65 \text{ mi}) \left( \frac{1.609 \text{ km}}{1 \text{ mi}} \right) \left( \frac{1}{1 \text{ h}} \right) = 104 \text{ km/h}$$



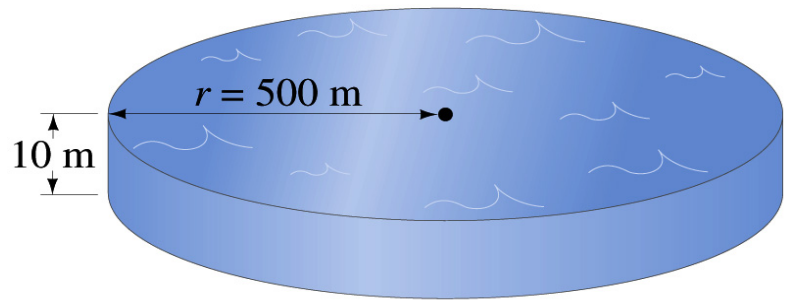
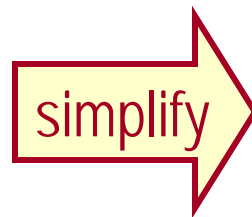
# Estimates & Order-of-Magnitude Calculations

- Estimate = Approximation
  - Useful for rough calculations to determine the necessity of higher precision
  - Usually done under certain assumptions
  - Might require modification of assumptions, if higher precision is necessary
- Order of magnitude estimate: Estimates done to the precision of 10s or exponents of 10s;
  - Rapid estimating
  - Three orders of magnitude:  $10^3=1,000$
  - Round up for Order of magnitude estimate;  $8 \times 10^7 \sim 10^8$
  - Similar terms: "Ball-park-figures", "guesstimates", etc



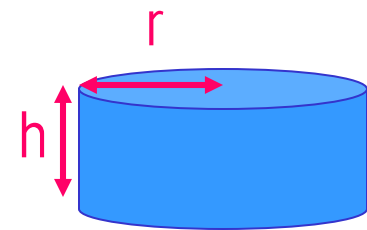
# Example 1.5

Estimate how much water is in a lake in the figure which is roughly circular, about 1km across, and you guess it to have an average depth of about 10m.



Volume of a cylinder

$$V = h \times A$$
$$= h \times \pi r^2$$



What is the radius of the circle?    Half the distance across...     $1\text{km}/2 = 1000\text{m}/2 = 500\text{m}$

$$V = h \times \pi r^2 = 10\text{m} \times \pi (500\text{m})^2 = 7850000 \cong 8 \times 10^6 \text{m}^3 \cong 10^7 \text{m}^3$$

# Dimension and Dimensional Analysis

- An extremely useful concept in solving physical problems
- Good to write physical laws in mathematical expressions
- No matter what units are used the base quantities are the same
  - *Length* (distance) is length whether meter or inch is used to express the size: Usually denoted as  $[L]$
  - The same is true for *Mass* ( $[M]$ ) and *Time* ( $[T]$ )
  - One can say “Dimension of Length, Mass or Time”
  - Dimensions are used as algebraic quantities: Can perform algebraic operations, addition, subtraction, multiplication or division



# Dimension and Dimensional Analysis

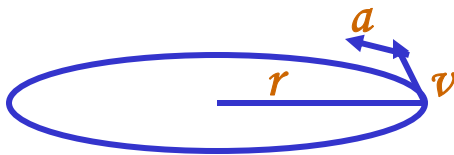
- One can use dimensions only to check the validity of one's expression: Dimensional analysis
  - Eg: Speed  $[v] = [L]/[T] = [L][T^{-1}]$ 
    - *Distance ( $L$ ) traveled by a car running at the speed  $V$  in time  $T$*
    - $L = V \star T = [L/T] \star [T] = [L]$
- More general expression of dimensional analysis is using exponents: eg.  $[v] = [L^n T^m] = [L][T^{-1}]$   
*where  $n = 1$  and  $m = -1$*





# Examples

- Show that the expression  $[v] = [at]$  is dimensionally correct
  - Speed:  $[v] = L/T$
  - Acceleration:  $[a] = L/T^2$
  - Thus,  $[at] = (L/T^2) \times T = LT^{(-2+1)} = LT^{-1} = L/T = [v]$
- Suppose the acceleration  $a$  of a circularly moving particle with speed  $v$  and radius  $r$  is proportional to  $r^n$  and  $v^m$ . What are  $n$  and  $m$ ?



$$a = kr^n v^m$$

Dimensionless  
constant

Length

Speed

$$L^1 T^{-2} = (L)^n \left( \frac{L}{T} \right)^m = L^{n+m} T^{-m}$$

$$-m = -2 \Rightarrow m = 2$$

$$n + m = n + 2 = 1 \Rightarrow n = -1$$

$$a = kr^{-1} v^2 = \frac{v^2}{r}$$

Monday, Jan. 26, 2004



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Dr. Jaehoon Yu

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# Some Fundamentals

- Kinematics: Description of Motion without understanding the cause of the motion
- Dynamics: Description of motion accompanied with understanding the cause of the motion
- Vector and Scalar quantities:
  - Scalar: Physical quantities that require magnitude but no direction
    - Speed, length, mass, etc
  - Vector: Physical quantities that require both magnitude and direction
    - Velocity, Acceleration, Force, Momentum
    - It does not make sense to say “I ran with velocity of 10miles/hour.”
- Objects can be treated as point-like if their sizes are smaller than the scale in the problem
  - Earth can be treated as a point like object (or a particle) in celestial problems
  - Any other examples?

