

# PHYS 1441 – Section 004

## Lecture #8

*Monday, Feb. 16, 2004*

*Dr. Jaehoon Yu*

- Chapter four: Newton's Laws of Motion
  - Newton's First Law of Motion
  - Newton's Second Law of Motion
  - Gravitational Force
  - Newton's Third Law of Motion
  - Solving problems using Newton's Laws
- Uniform circular motion

1<sup>st</sup> term exam in the class at 1pm, next Monday, Feb. 23!!



# Announcements

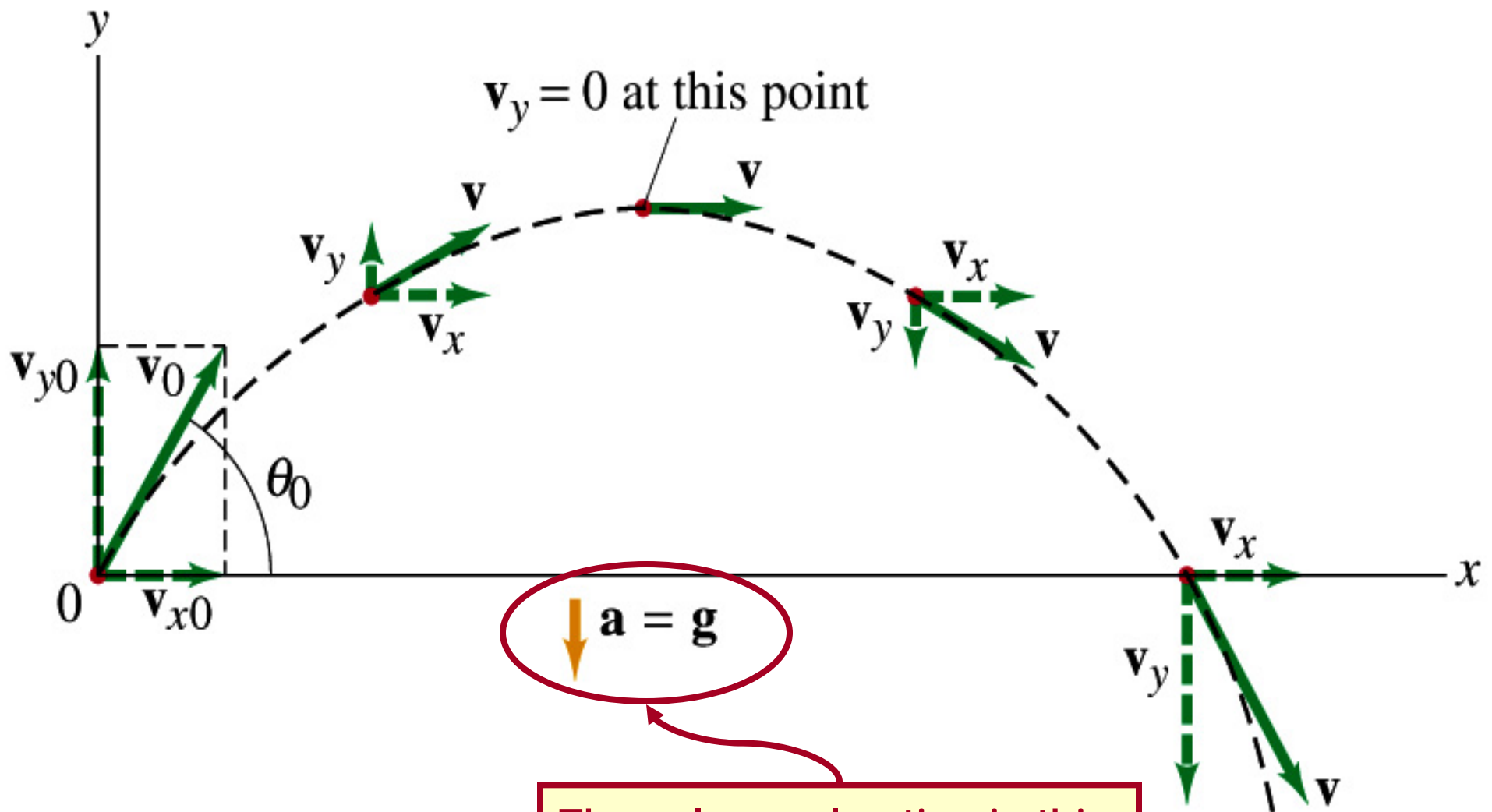
- Quiz
  - Average 53
    - Last time: 49
    - Got considerably better
  - Top score: 95
- 1<sup>st</sup> term exam
  - Chapter 1 – 5.3
  - Mixture of multiple choices and numeric problems
- Will drop the worst of the three term exams
  - Exams are not comprehensive
  - Exams constitute 45% of total
- E-mail:
  - Received 30 verifications → Thank you!
  - I still have 13 of you not registered for e-mail
    - Will issue -3 point if not done by next Monday, Feb. 23
    - - 5 points if not done by Monday, Mar. 1

Monday, Feb. 16, 2004



PHYS 1441-004, Spring 2004  
Dr. Jaehoon Yu

# Projectile Motion



The only acceleration in this motion. It is a constant!!

# Maximum Range and Height

- What are the conditions that give maximum height and range of a projectile motion?

$$h = \left( \frac{v_i^2 \sin^2 \theta_i}{2g} \right)$$

This formula tells us that the maximum height can be achieved when  $\theta_i = 90^\circ$ !!!

$$R = \left( \frac{v_i^2 \sin 2\theta_i}{g} \right)$$

This formula tells us that the maximum range can be achieved when  $2\theta_i = 90^\circ$ , i.e.,  $\theta_i = 45^\circ$ !!!

# Force

We've been learning kinematics; describing motion without understanding what the cause of the motion was. Now we are going to learn dynamics!!

~~FORCES~~ are what cause an object to move

Can someone tell me what FORCE is?

The above statement is not entirely correct. Why?

Because when an object is moving with a constant velocity no force is exerted on the object!!!

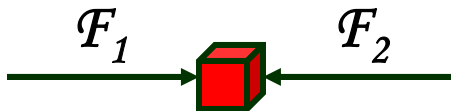
FORCES are what cause any changes in the velocity of an object!!

What does this statement mean?

When there is force, there is change of velocity.  
Forces cause acceleration.

What happens there are several forces being exerted on an object?

Forces are vector quantities, so vector sum of all forces, the NET FORCE, determines the motion of the object.



NET FORCE,  
 $F = F_1 + F_2$

When net force on an object is 0, it has constant velocity and is at its equilibrium!!

# More Force

There are various classes of forces

*Contact Forces: Forces exerted by physical contact of objects*

*Examples of Contact Forces: Baseball hit by a bat, Car collisions*

*Field Forces: Forces exerted without physical contact of objects*

*Examples of Field Forces: Gravitational Force, Electro-magnetic force*

*What are possible ways to measure strength of Force?*

*A calibrated spring whose length changes linearly with the exerted force.*

*Forces are vector quantities, so addition of multiple forces must be done following the rules of vector additions.*



# Newton's First Law and Inertial Frames

Aristotle (384-322BC): *A natural state of a body is rest. Thus force is required to move an object. To move faster, one needs higher force.*

Galileo's statement on natural states of matter: *Any velocity once imparted to a moving body will be rigidly maintained as long as the external causes of retardation are removed!!*

Galileo's statement is formulated by Newton into the **1<sup>st</sup> law of motion (Law of Inertia)**: *In the absence of external forces, an object at rest remains at rest and an object in motion continues in motion with a constant velocity.*

What does this statement tell us?

- When no force is exerted on an object, the acceleration of the object is 0.
- Any isolated object, the object that does not interact with its surroundings, is either at rest or moving at a constant velocity.
- Objects would like to keep its current state of motion, as long as there is no force that interferes with the motion. This tendency is called the Inertia.

A frame of reference that is moving at constant velocity is called an ***Inertial Frame***



# Mass

Mass: *A measure of the inertia of a body Or quantity of matter*

1. Independent of the object's surroundings: The same no matter where you go.
2. Independent of method of measurement: The same no matter how you measure it.

*The heavier an object gets the bigger the inertia!!*

*It is harder to make changes of motion of a heavier object than the lighter ones.*

*The same forces applied to two different masses result in different acceleration depending on the mass.*

$$\frac{m_1}{m_2} \equiv \frac{a_2}{a_1}$$

*Note that mass and weight of an object are two different quantities!!*

*Weight of an object is the magnitude of gravitational force exerted on the object.*

*Not an inherent property of an object!!!*

*Weight will change if you measure on the Earth or on the moon.*





# Newton's Second Law of Motion

*The acceleration of an object is directly proportional to the net force exerted on it and is inversely proportional to the object's mass.*

*How do we write the above statement in a mathematical expression?*

$$\sum_i \vec{F}_i = m\vec{a}$$

*Since it's a vector expression, each component should also satisfy:*

$$\sum_i F_{ix} = ma_x$$

$$\sum_i F_{iy} = ma_y$$

$$\sum_i F_{iz} = ma_z$$

*From the above vector expression, what do you conclude the dimension and unit of force are?*

*The unit of force in SI is*  $[Force] = [m][a] = \text{kg} \cdot \text{m} / \text{s}^2$

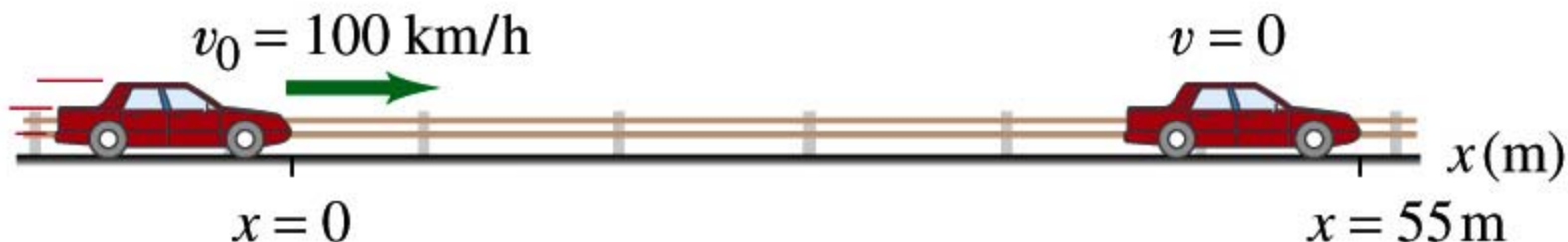
*For ease of use, we define a new derived unit called, a Newton (N)*

$$1 \text{ N} \equiv 1 \text{ kg} \cdot \text{m} / \text{s}^2 \approx \frac{1}{4} \text{ lbs}$$



# Example 4.2

What constant net force is required to bring a 1500kg car to rest from a speed of 100km/h within a distance of 55m?



What do we need to know to figure out the force?

**Acceleration!!**

What are given? Initial speed:  $v_{xi} = 100 \text{ km/h} = 28 \text{ m/s}$  Final speed:  $v_{xf} = 0 \text{ m/s}$

Displacement:  $\Delta x = x_f - x_i = 55 \text{ m}$

This is a one dimensional motion. Which kinetic formula do we use to find acceleration?

$$v_{xf}^2 = v_{xi}^2 + 2a_x(x_f - x_i)$$

**Acceleration**  $\rightarrow$

$$a_x = \frac{v_{xf}^2 - v_{xi}^2}{2(x_f - x_i)} = \frac{-(28 \text{ m/s})^2}{2(55 \text{ m})} = -7.1 \text{ m/s}^2$$

Thus, the force needed to stop the car is

$$F_x = ma_x = 1500 \text{ kg} \times (-7.1 \text{ m/s}^2) = -1.1 \times 10^4 \text{ N}$$

Given the force how far does the car move till it stops?

$$\Delta x = x_f - x_i = \frac{v_{xf}^2 - v_{xi}^2}{2a_x} = \frac{m(v_{xf}^2 - v_{xi}^2)}{2ma_x} = \frac{m(v_{xf}^2 - v_{xi}^2)}{2F_x}$$

- Linearly proportional to the mass of the car
- Squarely proportional to the speed of the car
- Inversely proportional to the force by the brake

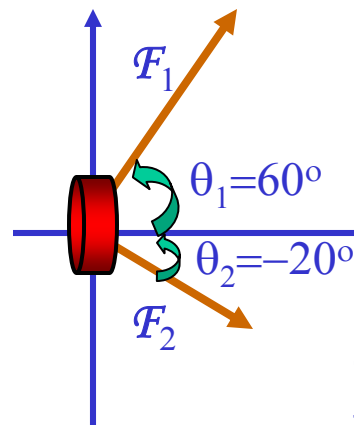
Monday, Feb. 16, 2004



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# Example for Newton's 2<sup>nd</sup> Law of Motion

Determine the magnitude and direction of acceleration of the puck whose mass is 0.30kg and is being pulled by two forces,  $F_1$  and  $F_2$ , as shown in the picture, whose magnitudes of the forces are 8.0 N and 5.0 N, respectively.



Components  
of  $F_1$

$$F_{1x} = |\vec{F}_1| \cos \theta_1 = 8.0 \times \cos(60^\circ) = 4.0 \text{ N}$$

$$F_{1y} = |\vec{F}_1| \sin \theta_1 = 8.0 \times \sin(60^\circ) = 6.9 \text{ N}$$

Components  
of  $F_2$

$$F_{2x} = |\vec{F}_2| \cos \theta_2 = 5.0 \times \cos(-20^\circ) = 4.7 \text{ N}$$

$$F_{2y} = |\vec{F}_2| \sin \theta_2 = 5.0 \times \sin(-20^\circ) = -1.7 \text{ N}$$

Components of  
total force  $F$

$$F_x = F_{1x} + F_{2x} = 4.0 + 4.7 = 8.7 \text{ N} = ma_x$$

$$F_y = F_{1y} + F_{2y} = 6.9 - 1.7 = 5.2 \text{ N} = ma_y$$

Magnitude and  
direction of  
acceleration  $a$

$$a_x = \frac{F_x}{m} = \frac{8.7}{0.3} = 29 \text{ m/s}^2 \quad a_y = \frac{F_y}{m} = \frac{5.2}{0.3} = 17 \text{ m/s}^2 \quad |\vec{a}| = \sqrt{(a_x)^2 + (a_y)^2} = \sqrt{(29)^2 + (17)^2} = 34 \text{ m/s}^2$$

$$\theta = \tan^{-1}\left(\frac{a_y}{a_x}\right) = \tan^{-1}\left(\frac{17}{29}\right) = 30^\circ$$

Acceleration  
Vector  $a$

$$\vec{a} = a_x \hat{i} + a_y \hat{j} = (29\hat{i} + 17\hat{j}) \text{ m/s}^2$$

# Gravitational Force and Weight

Gravitational Force,  $F_g$

*The attractive force exerted  
on an object by the Earth*

$$\vec{F}_G = m\vec{a} = m\vec{g}$$

Weight of an object with mass M is

$$W = |\vec{F}_G| = M|\vec{g}| = Mg$$

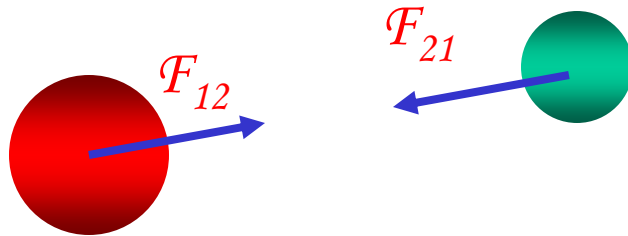
*Since weight depends on the magnitude of gravitational acceleration,  $g$ , it varies depending on geographical location.*

*By measuring the forces one can determine masses. This is why you can measure mass using spring scale.*



# Newton's Third Law (Law of Action and Reaction)

*If two objects interact, the force,  $F_{21}$ , exerted on object 1 by object 2 is equal in magnitude and opposite in direction to the force,  $F_{12}$ , exerted on object 2 by object 1.*



$$\vec{F}_{12} = -\vec{F}_{21}$$

*The action force is equal in magnitude to the reaction force but in opposite direction. These two forces always act on different objects.*

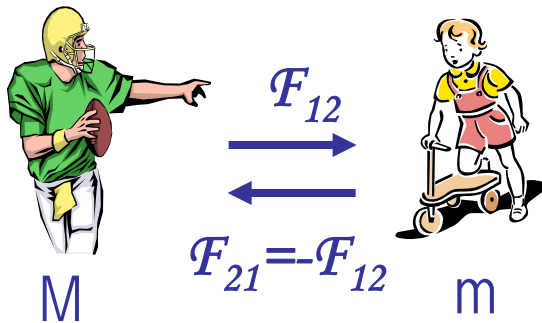
*What is the reaction force to the force of a free fall object?*

~~*The force exerted by the ground when it completed the motion.*~~

*Stationary objects on top of a table has a reaction force (normal force) from table to balance the action force, the gravitational force.*

# Example of Newton's 3<sup>rd</sup> Law

A large man and a small boy stand facing each other on **frictionless ice**. They put their hands together and push against each other so that they move apart. a) Who moves away with the higher speed and by how much?



$$\vec{F}_{12} = -\vec{F}_{21} \quad |\vec{F}_{12}| = |\vec{F}_{21}| = F$$

$$\vec{F}_{12} = m \vec{a}_b \quad F_{12x} = ma_{bx} \quad F_{12y} = ma_{by} = 0$$

$$\vec{F}_{21} = M \vec{a}_M \quad F_{21x} = Ma_{Mx} \quad F_{21y} = Ma_{My} = 0$$

$$\vec{F}_{12} = -\vec{F}_{21} \quad |\vec{F}_{12}| = |\vec{F}_{21}| = F \quad a_{bx} = \frac{F}{m} = \frac{M}{m} a_{Mx}$$

$$v_{Mxf} = v_{Mxi} + a_{Mx}t = a_{Mx}t$$

$$v_{bxf} = v_{bxi} + a_{bx}t = a_{bx}t = \frac{M}{m} a_{Mx}t = \frac{M}{m} v_{Mxf}$$

$$\therefore v_{bxf} > v_{Mxf} \text{ if } M > m \text{ by the ratio of the masses}$$

b) Who moves farther while their hands are in contact?

Given in the same time interval, since the boy has higher acceleration and thereby higher speed, he moves farther than the man.

$$x_b = v_{bxf}t + \frac{1}{2}a_{bx}t^2 = \frac{M}{m}v_{Mxf}t + \frac{M}{2m}a_{Mx}t^2$$

$$x_b = \frac{M}{m} \left( v_{Mxf}t + \frac{1}{2}a_{Mx}t^2 \right) = \frac{M}{m}x_M$$