

# PHYS 1441 – Section 004

## Lecture #12

*Monday, Mar. 8, 2004*

*Dr. Jaehoon Yu*

- Potential Energies  
gravitational and elastic
- Conservative and Non-conservative Forces
- Conservation of Mechanical Energy
- Work Done by Non-conservative forces
- Power



# Announcements

- Homework site was back up on Wednesday evening.
  - The due for homework #6 was extended to 5pm Thursday.
  - Due for homework #7 is till this Wednesday
- There will be a quiz on March 10
  - Sections 5.6 – 6.10



# Work and Kinetic Energy

*Work in physics is done only when the sum of forces exerted on an object made a motion to the object.*

*What does this mean?*

*However much tired your arms feel, if you were just holding an object without moving it you have not done any physical work.*

*Mathematically, work is written in a product of magnitudes of the net force vector, the magnitude of the displacement vector and the angle between them,.*

$$W = \left| \sum (\vec{F}_i) \right| \left| \vec{d} \right| \cos \theta$$

*Kinetic Energy is the energy associated with motion and capacity to perform work. Work causes change of energy after the completion* ← Work-Kinetic energy theorem

$$K = \frac{1}{2}mv^2$$

$$\sum W = K_f - K_i = \Delta K$$

*Nm=Joule*

# Potential Energy

*Energy associated with a system of objects → Stored energy which has Potential or possibility to work or to convert to kinetic energy*

*What does this mean?*

*In order to describe potential energy,  $\mathcal{U}$ , a system must be defined.*

*The concept of potential energy can only be used under the special class of forces called, conservative forces which results in principle of conservation of mechanical energy.*

$$E_M \equiv KE_i + PE_i = KE_f + PE_f$$

*What are other forms of energies in the universe?*

*Mechanical Energy*

*Chemical Energy*

*Biological Energy*

*Electromagnetic Energy*

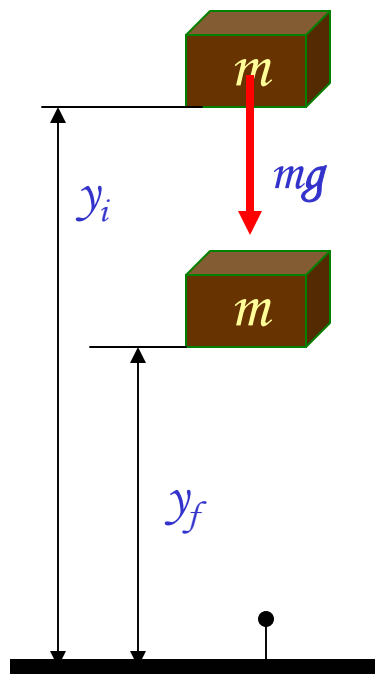
*Nuclear Energy*

*These different types of energies are stored in the universe in many different forms!!!*

*If one takes into account ALL forms of energy, the total energy in the entire universe is conserved. It just transforms from one form to the other.*

# Gravitational Potential Energy

*Potential energy given to an object by gravitational field in the system of Earth due to its height from the surface*



*When an object is falling, gravitational force,  $Mg$ , performs work on the object, increasing its kinetic energy. The potential energy of an object at a height  $y$  which is the potential to work is expressed as*

$$U_g = \left| \vec{F}_g \right| \left| \vec{y} \right| \sin \theta = \left| \vec{F}_g \right| \left| \vec{y} \right| = mgy \quad U_g \equiv mgy$$

*Work performed on the object by the gravitational force as the brick goes from  $y_i$  to  $y_f$  is:*

$$W_g = U_i - U_f \\ = mgy_i - mgy_f = -\Delta U_g$$

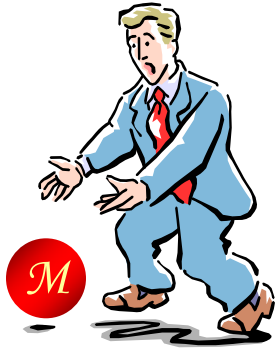
*What does this mean?*

*Work by the gravitational force as the brick goes from  $y_i$  to  $y_f$  is negative of the change in the system's potential energy*

**→ Potential energy was lost in order for gravitational force to increase the brick's kinetic energy.**

# Example for Potential Energy

A bowler drops bowling ball of mass 7kg on his toe. Choosing floor level as  $y=0$ , estimate the total work done on the ball by the gravitational force as the ball falls.



Let's assume the top of the toe is 0.03m from the floor and the hand was 0.5m above the floor.

$$U_i = mgy_i = 7 \times 9.8 \times 0.5 = 34.3J \quad U_f = mgy_f = 7 \times 9.8 \times 0.03 = 2.06J$$

$$W_g = -\Delta U = -(U_f - U_i) = 32.24J \cong 30J$$

b) Perform the same calculation using the top of the bowler's head as the origin.

What has to change?

First we must re-compute the positions of ball at the hand and of the toe.

Assuming the bowler's height is 1.8m, the ball's original position is -1.3m, and the toe is at -1.77m.

$$U_i = mgy_i = 7 \times 9.8 \times (-1.3) = -89.2J \quad U_f = mgy_f = 7 \times 9.8 \times (-1.77) = -121.4J$$

$$W_g = -\Delta U = -(U_f - U_i) = 32.2J \cong 30J$$

# Elastic Potential Energy

*Potential energy given to an object by a spring or an object with elasticity in the system consists of the object and the spring without friction.*

*The force spring exerts on an object when it is distorted from its equilibrium by a distance  $x$  is*

$$F_s = -kx$$

*The work performed on the object by the spring is*

$$W_s = \int_{x_i}^{x_f} (-kx) dx = \left[ -\frac{1}{2}kx^2 \right]_{x_i}^{x_f} = -\frac{1}{2}kx_f^2 + \frac{1}{2}kx_i^2 = \frac{1}{2}kx_i^2 - \frac{1}{2}kx_f^2$$

*The potential energy of this system is*

$$U_s \equiv \frac{1}{2}kx^2$$

*What do you see from the above equations?*

*The work done on the object by the spring depends only on the initial and final position of the distorted spring.*

*Where else did you see this trend?*

*The gravitational potential energy,  $U_g$*

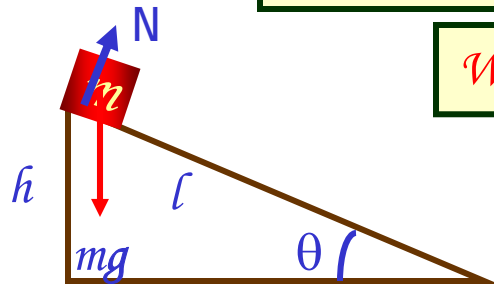
*So what does this tell you about the elastic force?*

*A conservative force!!!*



# Conservative and Non-conservative Forces

*The work done on an object by the gravitational force does not depend on the object's path.*



*When directly falls, the work done on the object is*

$$W_g = mgh$$

*When sliding down the hill of length  $l$ , the work is*

$$W_g = F_{g-\text{incline}} \times l = mg \sin \theta \times l$$

$$W_g = mg (l \sin \theta) = mgh$$

*How about if we lengthen the incline by a factor of 2, keeping the height the same??*

*Still the same amount of work 😊*

$$W_g = mgh$$

*So the work done by the gravitational force on an object is independent on the path of the object's movements. It only depends on the difference of the object's initial and final position in the direction of the force.*

*The forces like gravitational or elastic forces are called conservative forces*

1. *If the work performed by the force does not depend on the path*
2. *If the work performed on a closed path is 0.*

*Total mechanical energy is conserved!!*

$$E_M \equiv KE_i + PE_i = KE_f + PE_f$$

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# More Conservative and Non-conservative Forces

*A potential energy can be associated with a conservative force*

*A work done on a object by a conservative force is the same as the potential energy change between initial and final states*

$$W_c = U_i - U_f = -\Delta U$$

*So what is a conservative force?*

*The force that conserves mechanical energy.*

*OK, Then what is a non-conservative force?*

*The force that does not conserve mechanical energy.  
The work by these forces depends on the path.*

*Can you give me an example?*

*Friction*

*Why is it a non-conservative force?*

*Because the longer the path of an object's movement, the more work the friction forces perform on it.*

*What happens to the mechanical energy?*

*Kinetic energy converts to thermal energy and is not reversible.*

*Total mechanical energy is not conserved but the total energy is still conserved. It just exists in a different form.*

$$E_T \equiv E_M + E_{Other}$$

$$KE_i + PE_i = KE_f + PE_f + W_{Friction}$$

# Conservative Forces and Potential Energy

*The work done on an object by a conservative force is equal to the decrease in the potential energy of the system*

$$W_c = -\Delta U$$

*What else does this statement tell you?*

*The work done by a conservative force is equal to the negative of the change of the potential energy associated with that force.*

*Only the changes in potential energy of a system is physically meaningful!!*

*We can rewrite the above equation in terms of potential energy  $\mathcal{U}$*

$$W_c = -\Delta U = -U_f + U_i$$

*So the potential energy associated with a conservative force at any given position becomes*

$$U_f(x) = -W_c + U_i$$

*Potential energy function*

*What can you tell from the potential energy function above?*

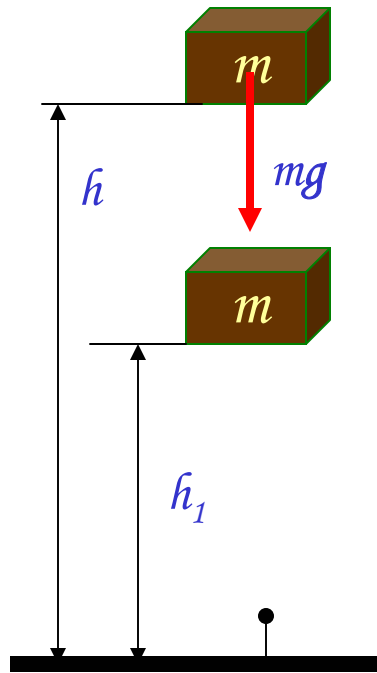
*Since  $\mathcal{U}_i$  is a constant, it only shifts the resulting  $\mathcal{U}_f(x)$  by a constant amount. One can always change the initial potential so that  $\mathcal{U}_i$  can be 0.*



# Conservation of Mechanical Energy

*Total mechanical energy is the sum of kinetic and potential energies*

$$E \equiv K + U$$



Let's consider a brick of mass  $m$  at a height  $h$  from the ground

*What is its potential energy?*

$$U_g = mgh$$

*What happens to the energy as the brick falls to the ground?*

$$\Delta U = U_f - U_i$$

*The brick gains speed*

*By how much?*

$$v = gt$$

*So what?*

*The brick's kinetic energy increased*

$$K = \frac{1}{2}mv^2 = \frac{1}{2}mg^2t^2$$

*And?*

*The lost potential energy converted to kinetic energy*

$$= mgh$$

What does this mean?

*The total mechanical energy of a system remains constant in any isolated system of objects that interacts only through conservative forces:*

*Principle of mechanical energy conservation*

$$E_i = E_f$$

$$K_i + \sum U_i = K_f + \sum U_f$$

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